

Understanding jet modifications at the LHC

Konrad Tywoniuk

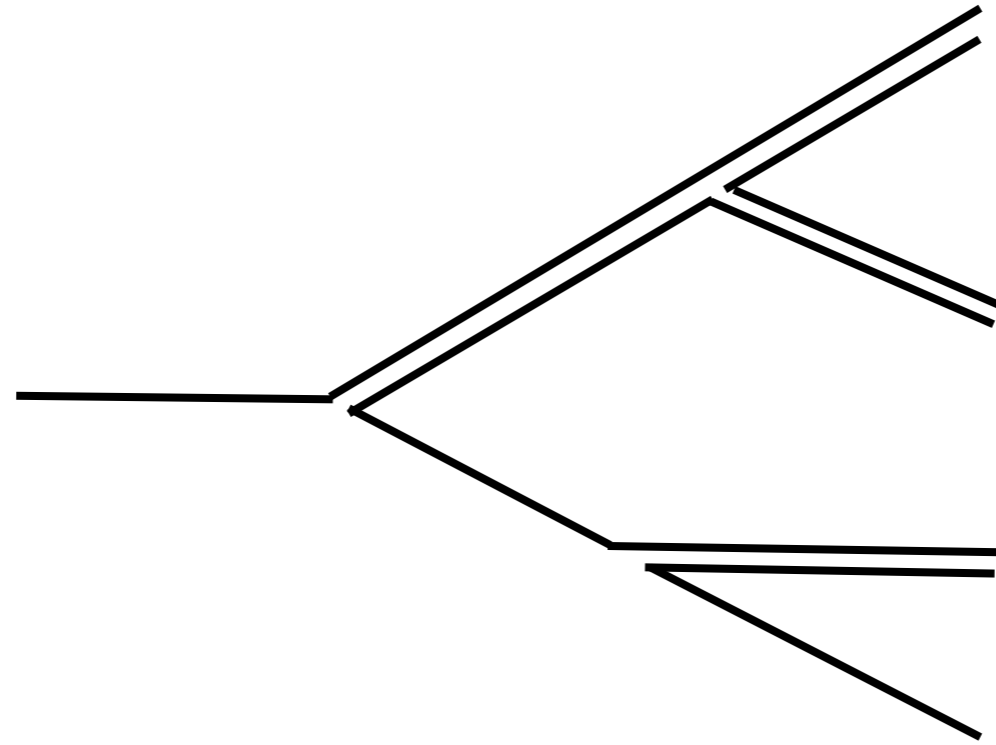
h3QCD, ECT* Trento, 17-21 June 2013

Overview

- PART I: Coherence effects & resolution
 - what interacts with the medium: color transparency
 - the simplest case: space-time picture
 - PART II: Phenomenological analysis
 - jet energy loss in medium
 - intra-jet modifications
 - out-of-cone energy flow
- [...work in progress]

In collaboration with: C.A. Salgado, J. Casalderrey-Solana, Y. Mehtar-Tani

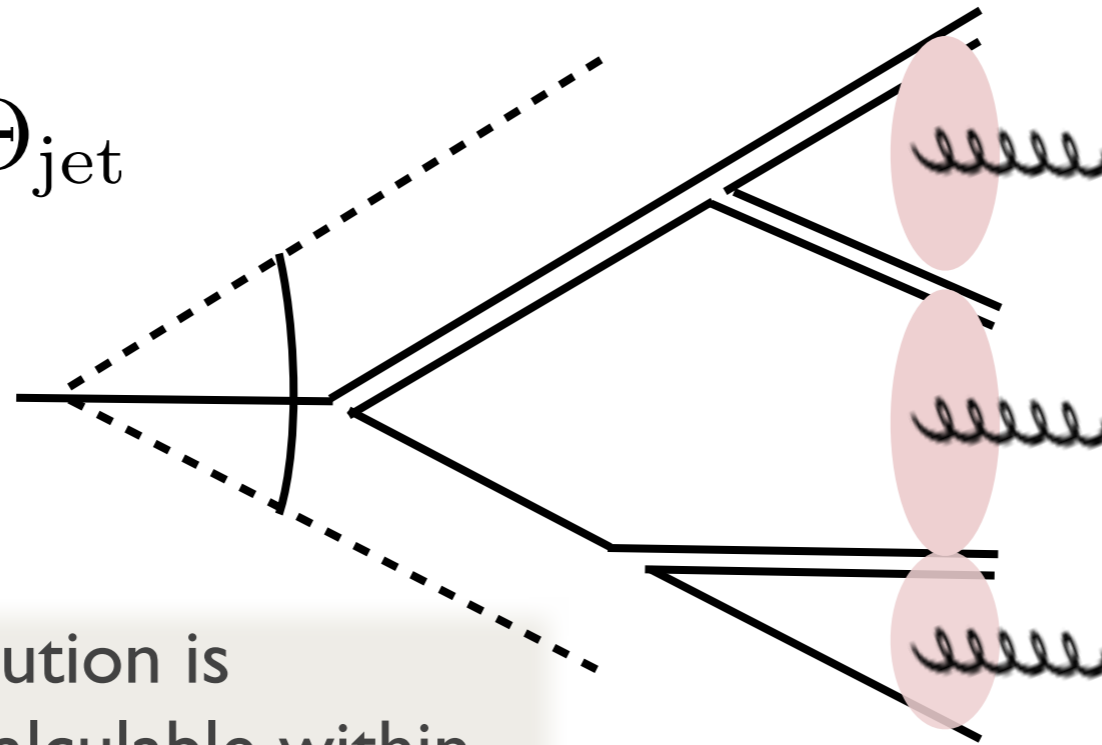
Jet "quenching" in HIC



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$$M_{\perp} = E \Theta_{\text{jet}}$$

$$Q_0 \sim \Lambda_{\text{QCD}}$$

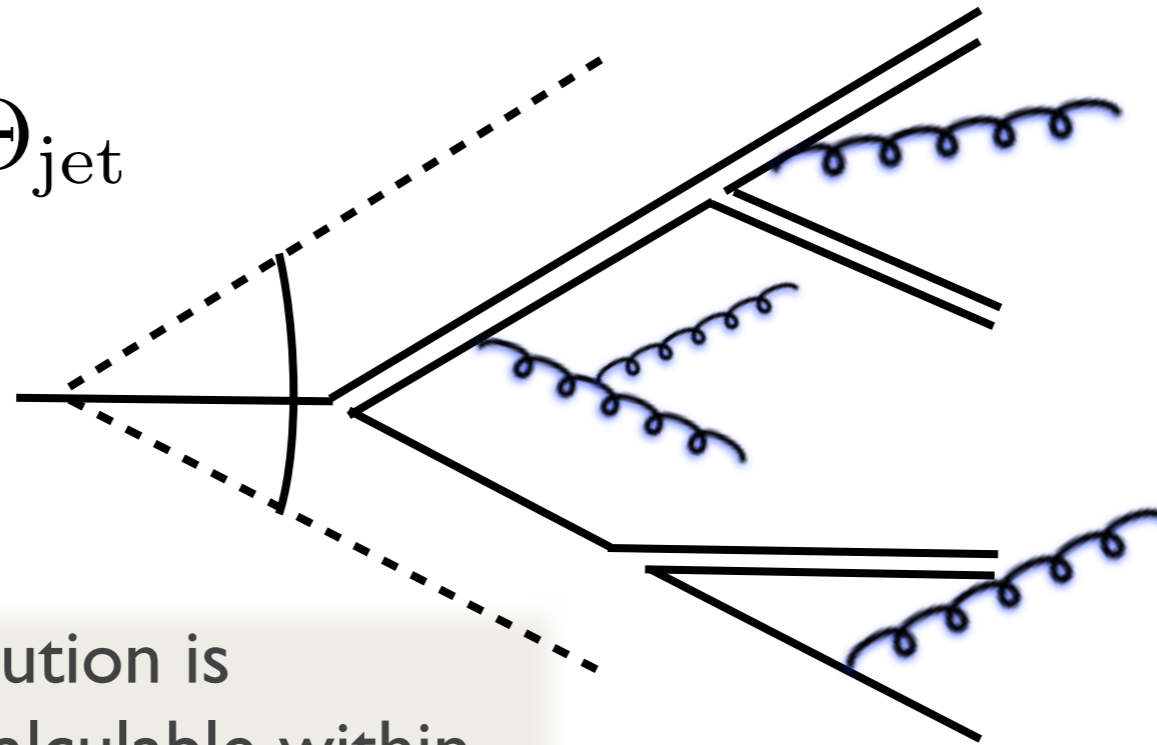


- vacuum jet evolution is systematically calculable within pQCD (large- N_c)
- resummation of soft and collinear divergences
- time-like evolution: angular ordering

Jet "quenching" in HIC

$$M_{\perp} = E \Theta_{\text{jet}}$$

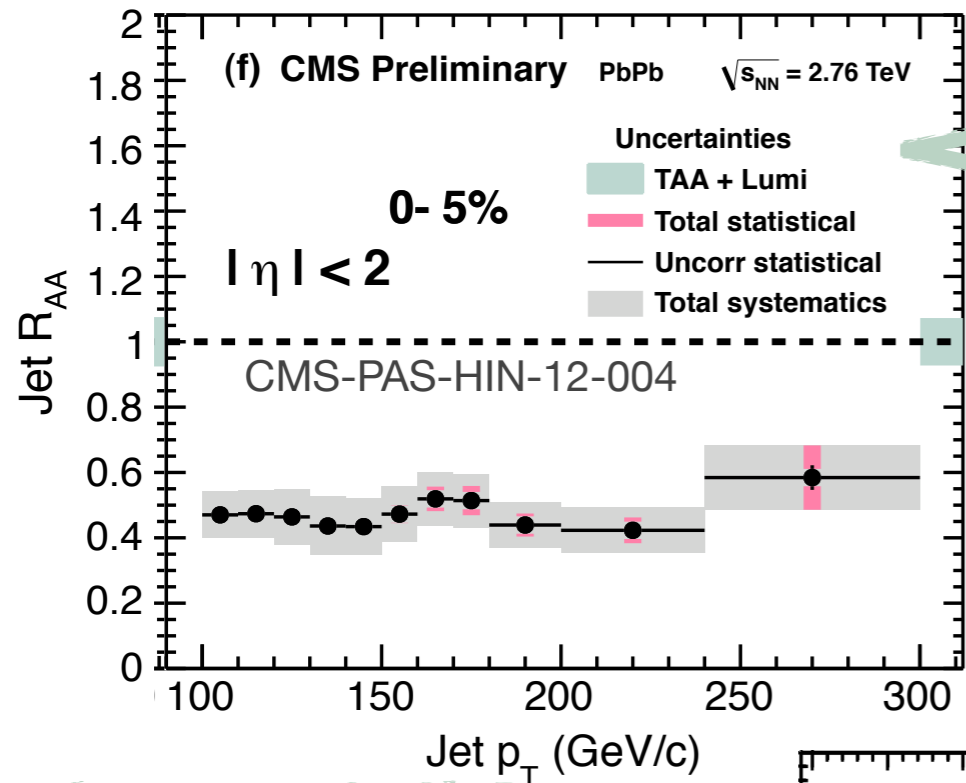
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- vacuum jet evolution is systematically calculable within pQCD (large- N_c)
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- transverse mom broadening
- induced energy-loss
- resolution power of the medium
- space-time picture

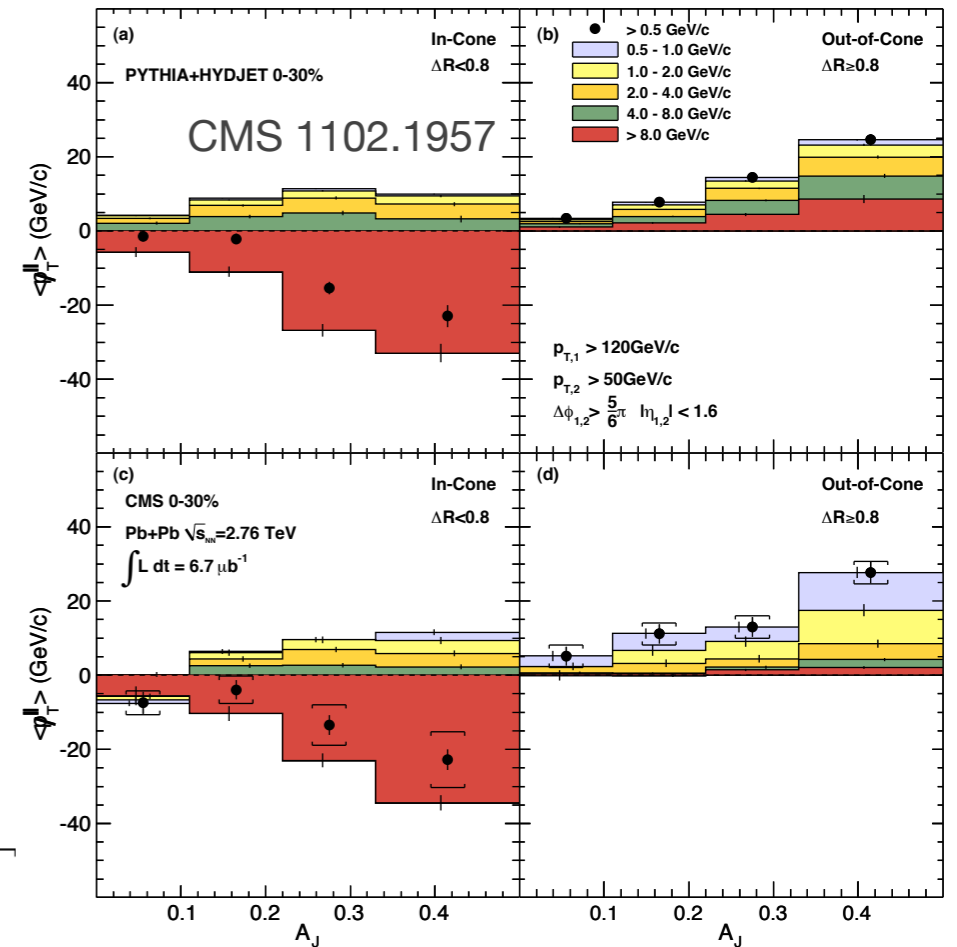
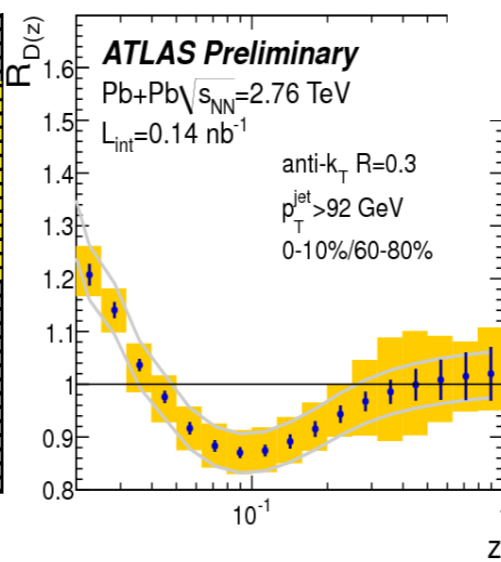
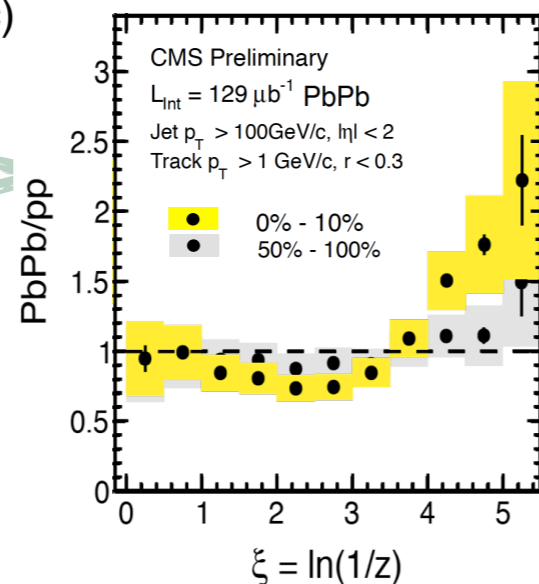
Experimental signatures



jet rate is suppressed

CMS-PAS-HIN-12-013
 ATLAS-CONF-2012-115

dip & softening of the jet long fragmentation function

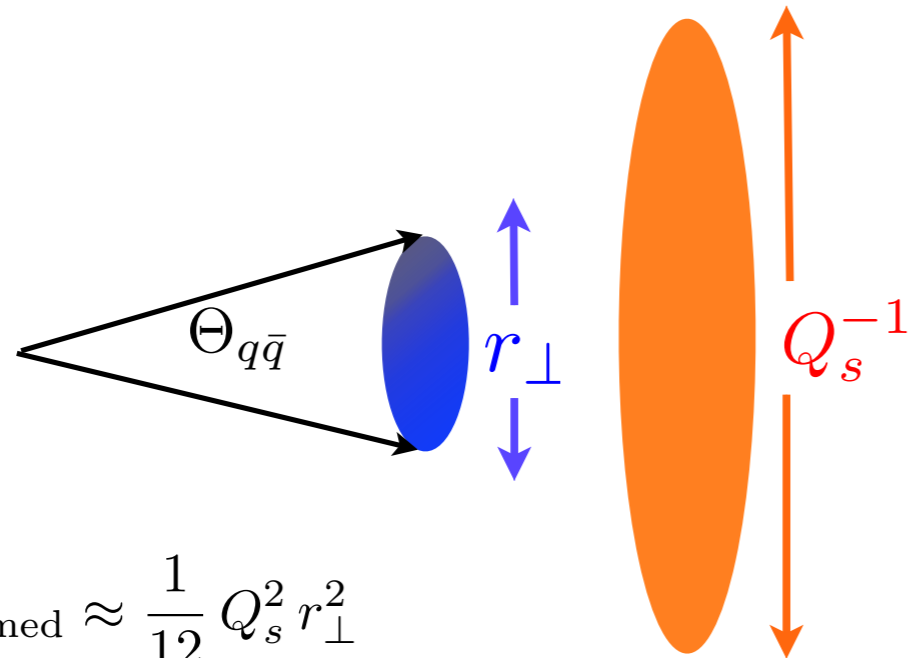


a significant fraction of the jet energy is found at large angles

The antenna in medium

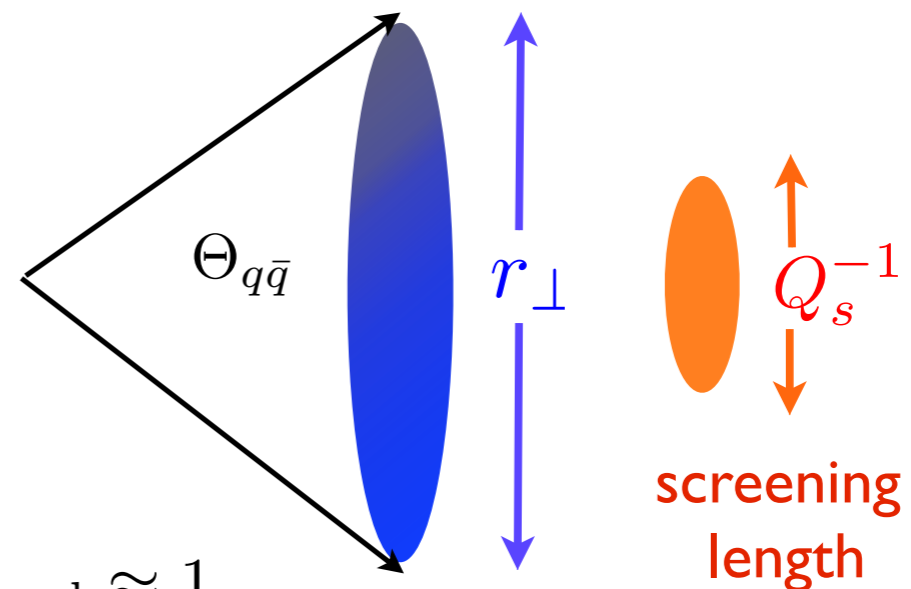
HARD SCALES FROM THE MEDIUM:

- $r_{\perp} < Q_s^{-1}$ (Dipole regime)



$$\Delta_{\text{med}} \approx \frac{1}{12} Q_s^2 r_{\perp}^2$$

- $r_{\perp} > Q_s^{-1}$ (Decoh. regime)



$$\Delta_{\text{med}} \approx 1$$

$$\Delta_{\text{med}} \approx 1 - \exp\left[-\frac{1}{12} Q_s^2 r_{\perp}^2\right]$$

the decoherence parameter

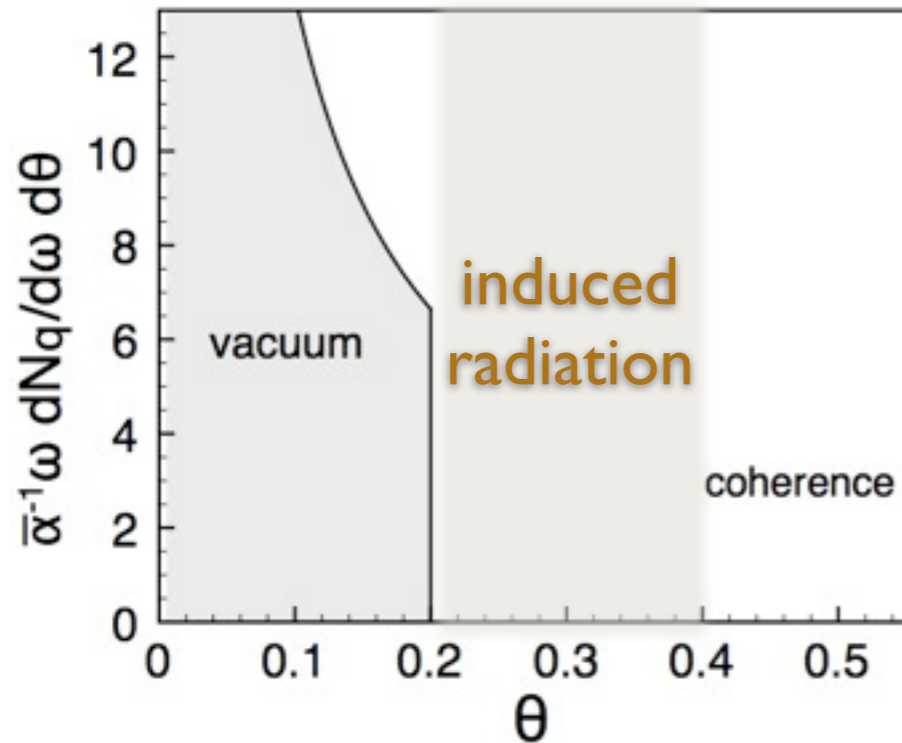
$$r_{\perp} = \theta_{q\bar{q}} L$$

Q_s : characteristic momentum
scale of the medium

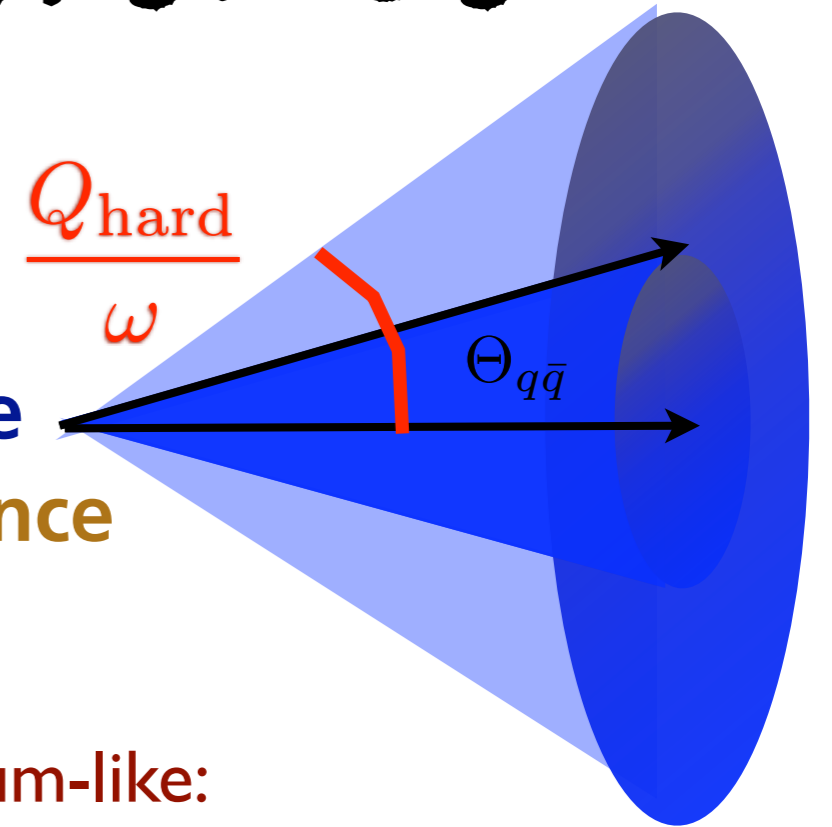
Mehtar-Tani, Salgado, KT 1009.2965; 1102.4317; 1112.5031; 1205.57397

Casalderrey-Solana, Iancu 1105.1760

Onset of decoherence



$\Delta_{\text{med}} \rightarrow 0$ **Coherence**
 $\Delta_{\text{med}} \rightarrow 1$ **Decoherence**



In $\omega \rightarrow 0$ limit, only vacuum-like:

$$dN_q^{\text{tot}} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{\sin \theta}{1 - \cos \theta} \frac{d\theta}{d\theta} [\Theta(\cos \theta - \cos \theta_{q\bar{q}}) + \Delta_{\text{med}} \Theta(\cos \theta_{q\bar{q}} - \cos \theta)] .$$

$$Q_{\text{hard}} = \max(r_{\perp}^{-1}, Q_s)$$

$$k_{\perp} < Q_{\text{hard}}$$

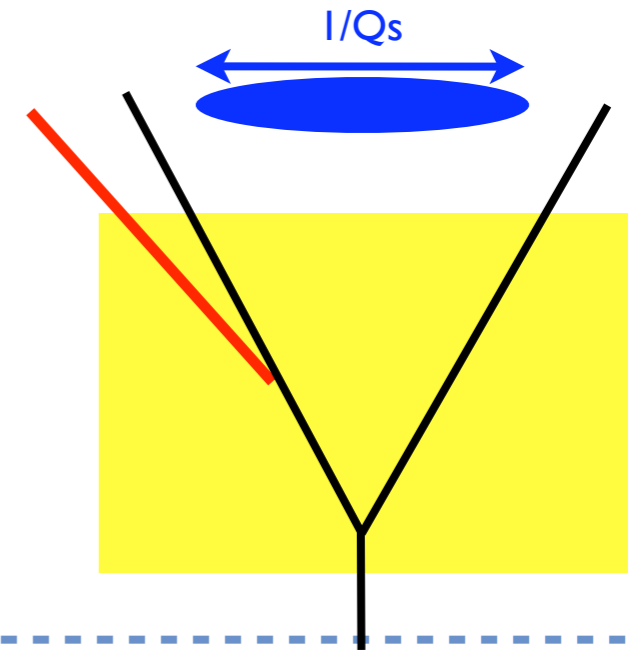
- decoherence opens phase space at large angles $\theta_{\text{max}} = Q_{\text{hard}}/\omega$
- jet spectrum unmodified at small angles

$$Q_{\text{hard}} = \max(r_{\perp}^{-1}, Q_s)$$

One emitter



Two emitters



vacuum coherence
(at large angles)

weak AAO, $\propto \Delta_{\text{med}} < l$

AO completely broken,
radiation up to $k_{\perp} \sim Q_s$

“medium-induced”

radiation as total
charge

radiation as
independent charges

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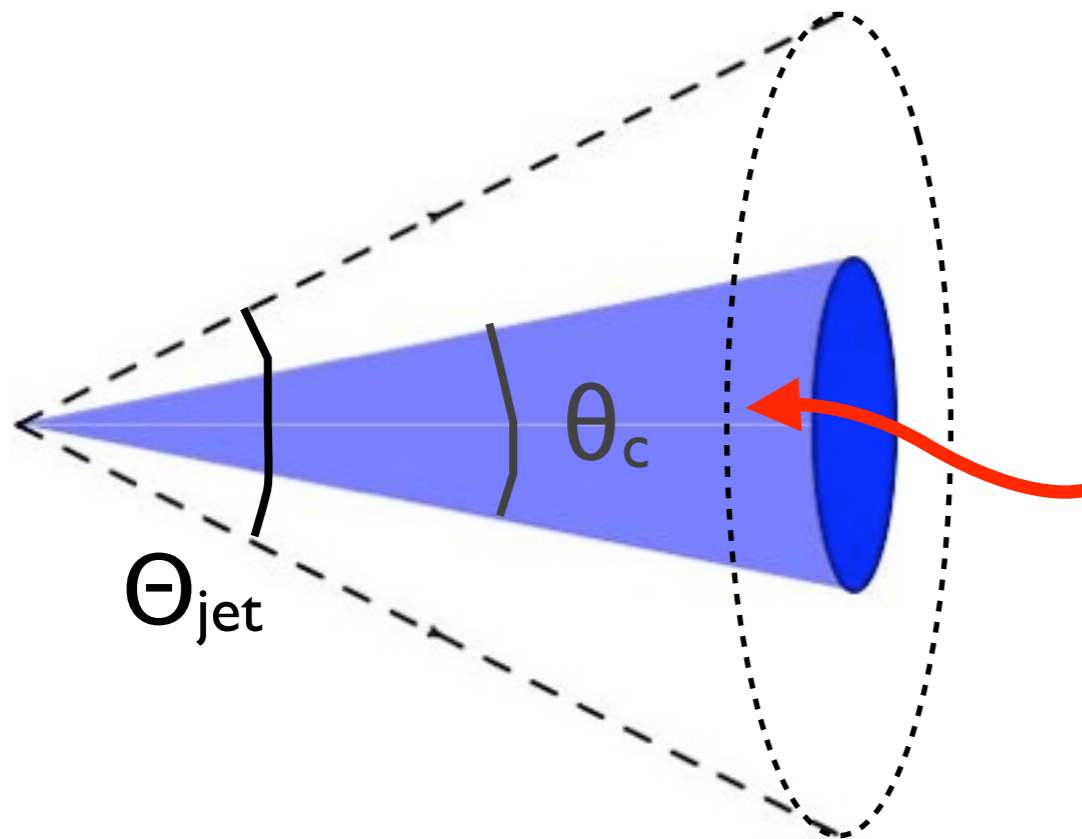
→ importance of medium-resolved sub-jets!

Resolving jet substructure

Generic scaling will involve the medium length L .

In terms of angles: $\Delta_{\text{med}} = 1 - e^{-\Theta_{\text{jet}}^2 / \theta_c^2}$

$\theta_c = 1 / \sqrt{\hat{q} L^3}$ jet definition ($\Theta_{\text{jet}} = R$)!



Coherent inner 'core'

- branchings occurring **inside the medium** with $\theta < \theta_c$
- modes with $\lambda_{\perp} < Q_s^{-1}$ ($k_{\perp} > Q_s$)
- $t_f < L \rightarrow Q_s^2 L < \omega < E$
- the core loses energy coherently

In central collisions: $\Theta_{\text{jet}} > \theta_c$

Casalderrey-Solana, Mehtar-Tani, Salgado, KT 1210.7765

Resolved effective charges

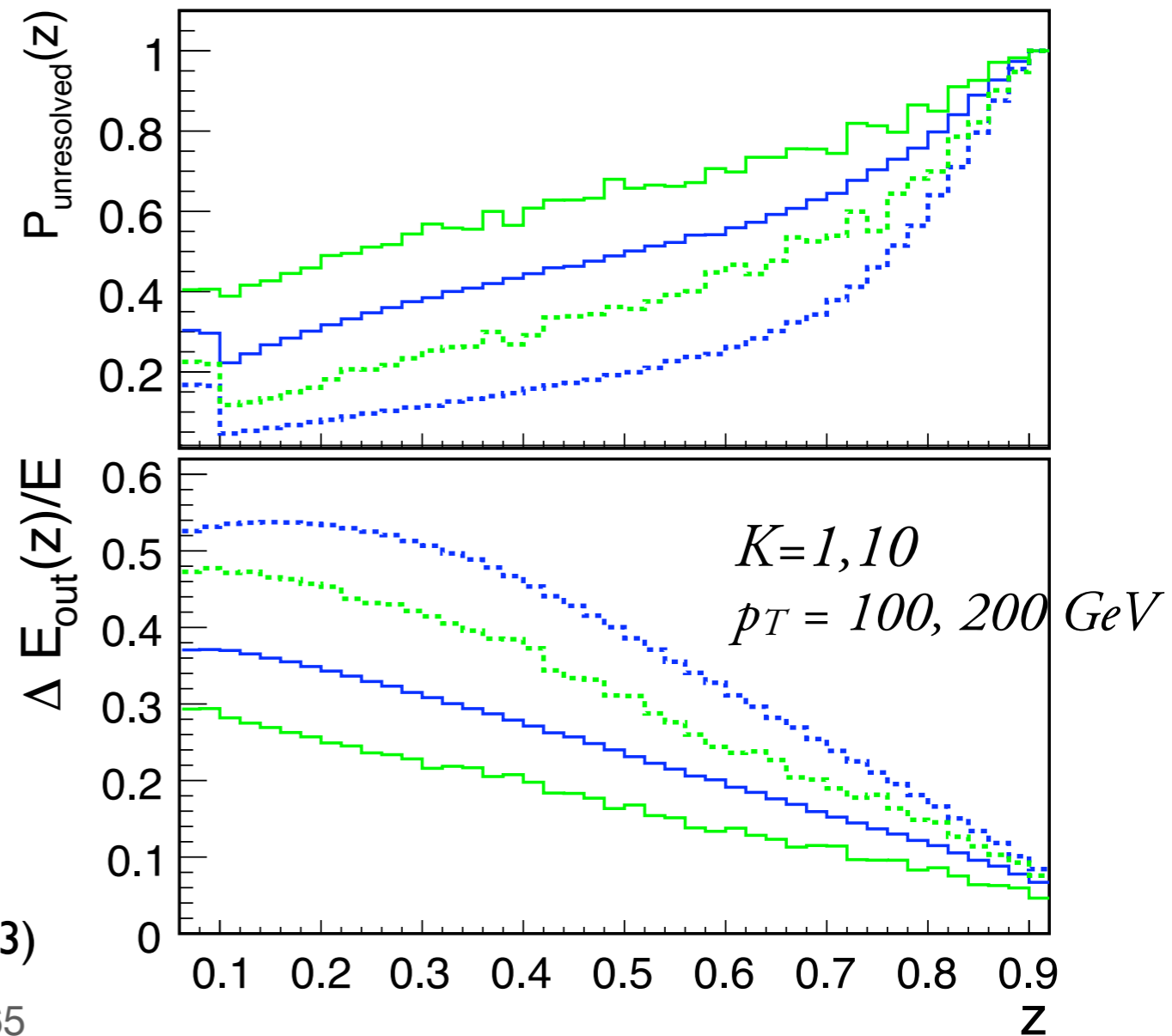
- study the magnitude of the medium resolution @ LHC
- substructure analysis with θ_c
- often we only have **one effective fragment** within R!
- contains most of the jet energy (**jet core**)

$$\hat{q}(\tau) = 2K\varepsilon^{3/4}(\tau)$$

PYTHIA 8.150 + 3D hydro + Fastjet (anti-kt, R = 0.3)

Casalderrey-Solana, Mehtar-Tani, Salgado, KT 1210.7765

Hydro from: T. Hirano, P. Huovinen, and Y. Nara,
Phys.Rev. C84, 011901; Phys.Rev. C83, 021902



:: probability of only finding one leading subjet in the presence of a fragment with mom frac z

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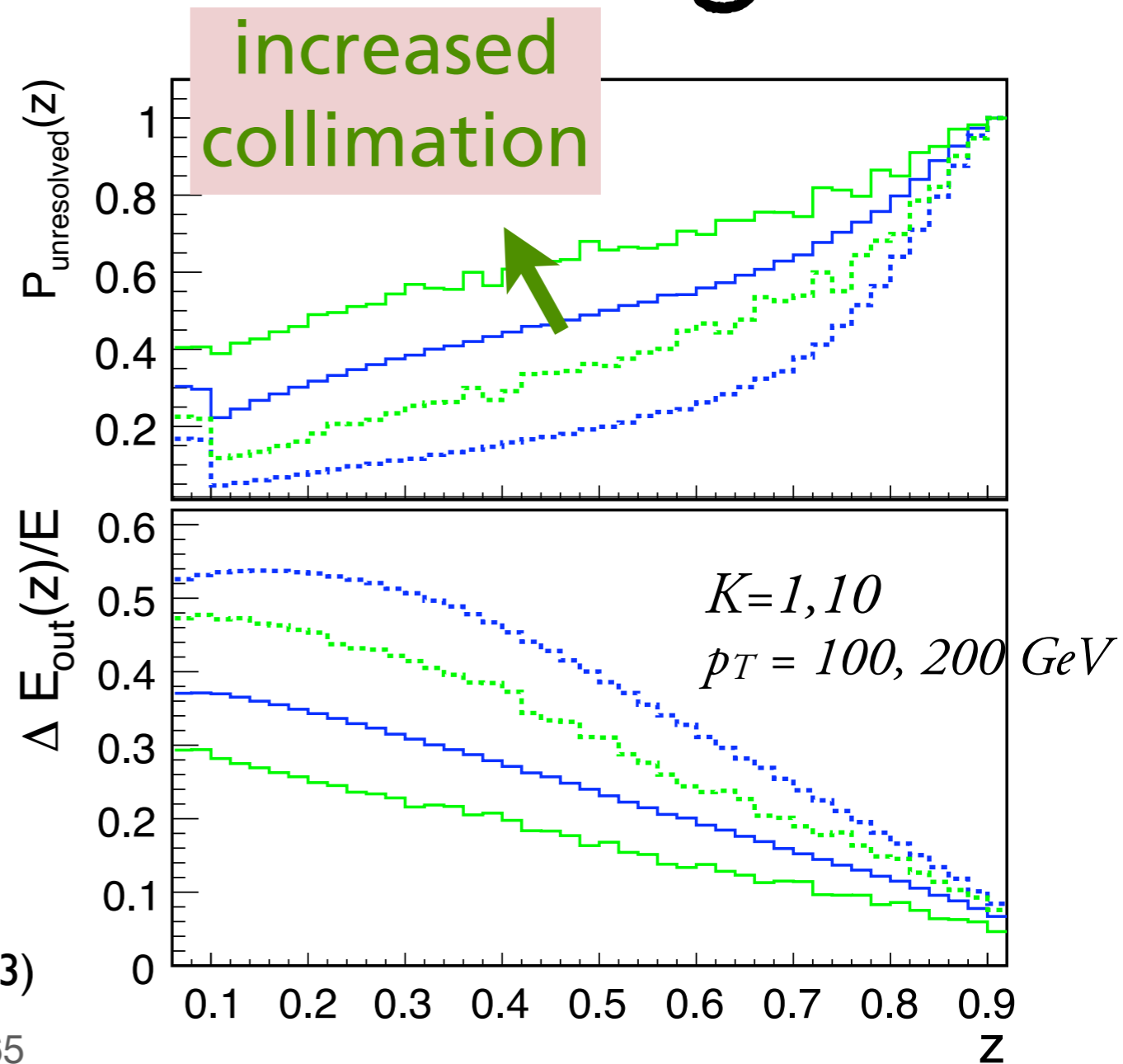
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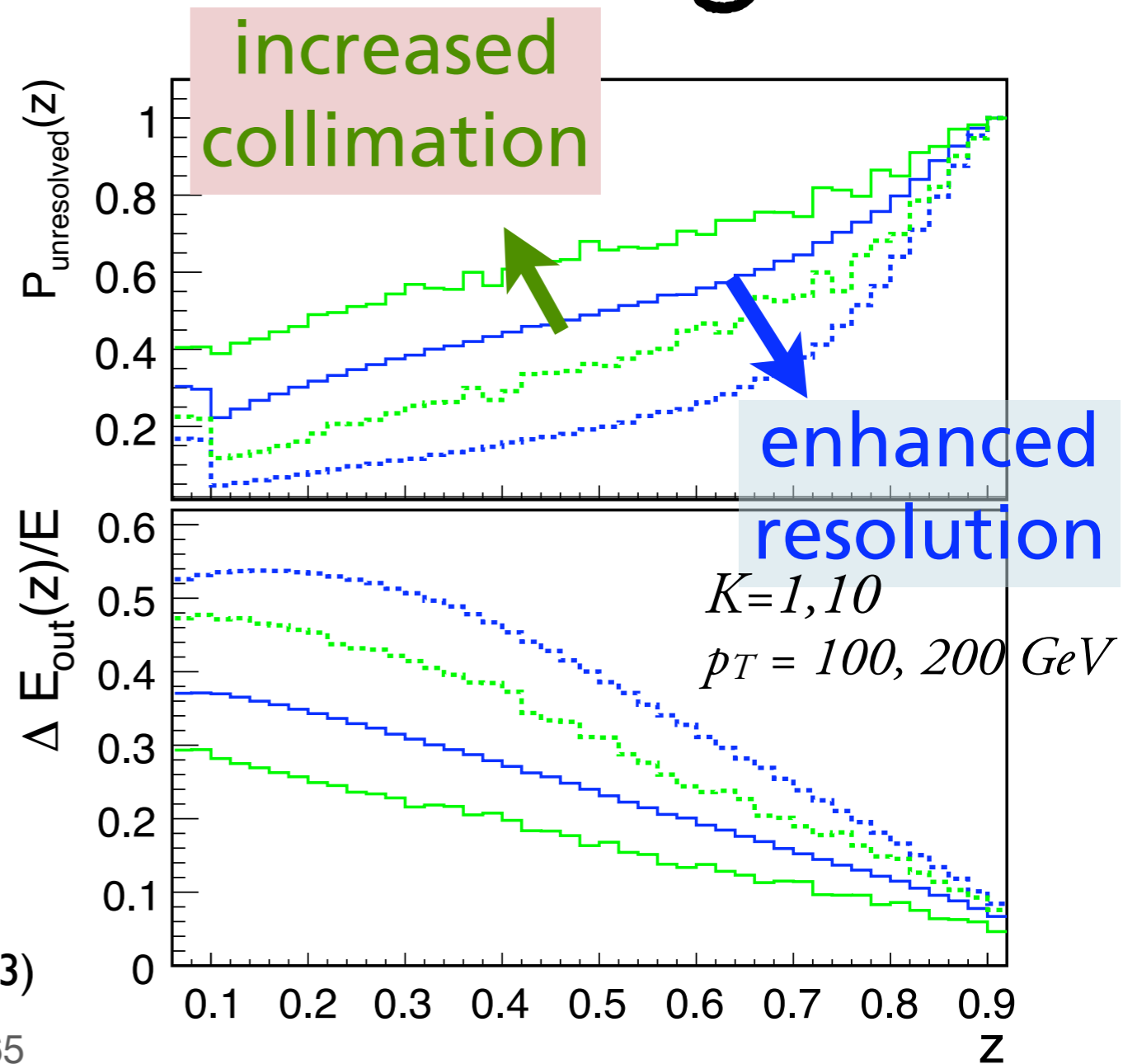
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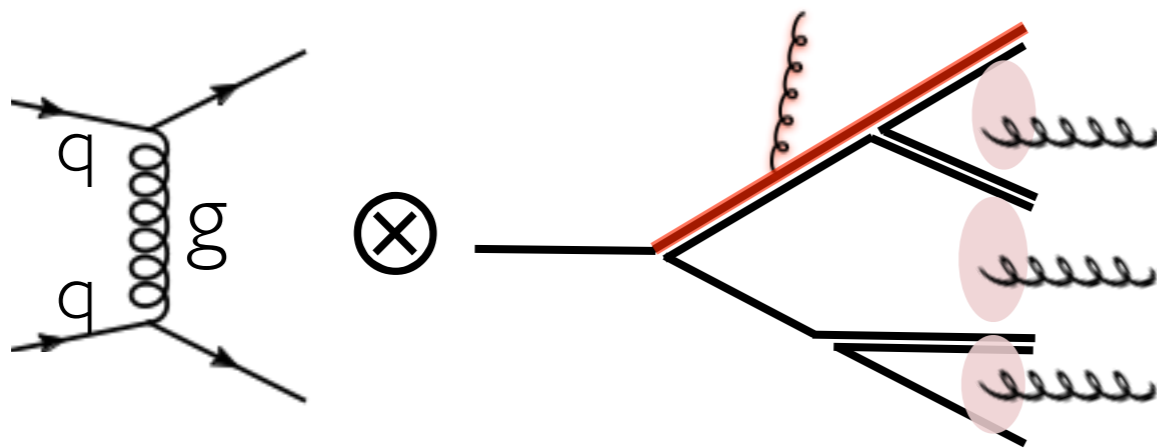
:: probability of only finding one leading subjet in the presence of a fragment with mom frac z

→ the objects interacting and radiating in the medium are really resolved subjects (multiparticle states) and not single partons...

Factorization of energy loss

Very often we have only a leading (unresolved) subjet that carries most of the momentum of the full jet :: **color transparency**.

A “factorization” for leading medium-resolved subjet:

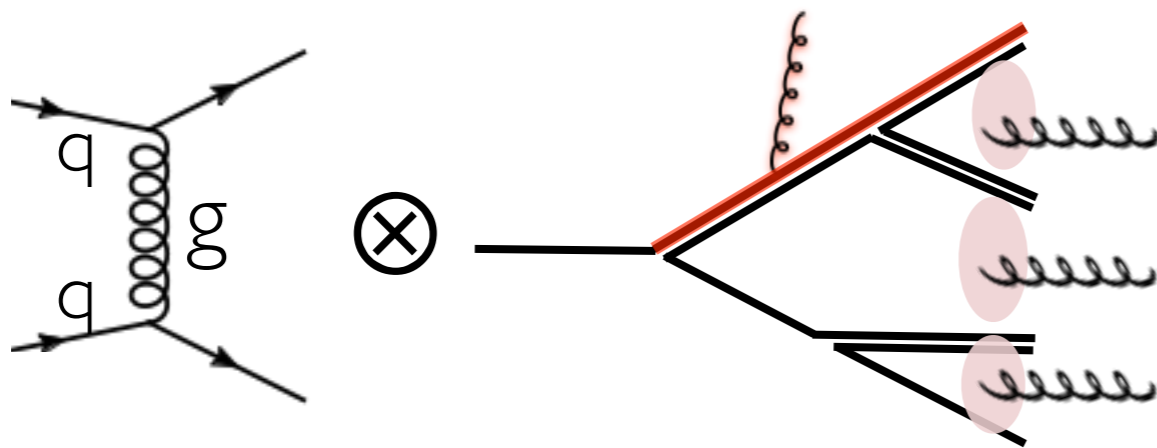


- separation in angles & separation in time :: **only the total charge radiates**
- allows to separate the treatment of the two different processes

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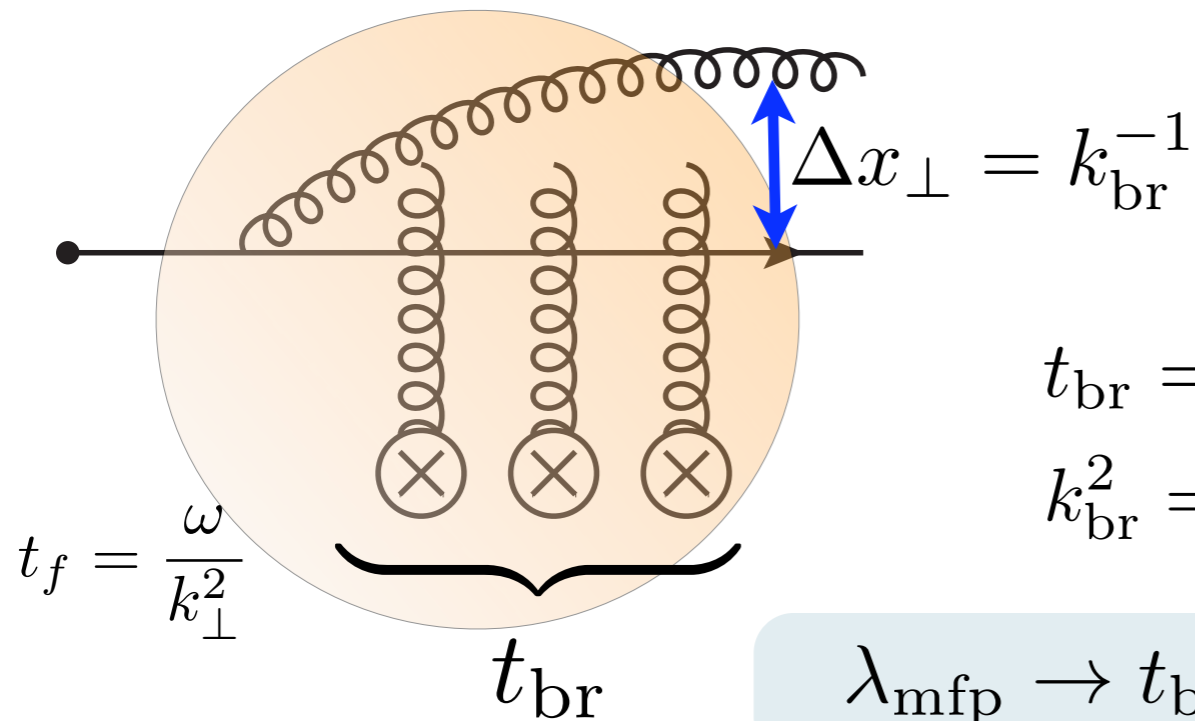
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jet produced with given p_T , $D_0(x) = \delta(1-x) \Rightarrow$ **total charge/ancestor particle lose energy** \Rightarrow vacuum showering (with reduced energy) starts

The ‘quenching factor’ for jets:

$$Q(p_{\perp})^{\text{jet}} = \int_0^1 dz D(z, \tau) \frac{d\sigma^{\text{jet,vac}}(p_{\perp}/z)}{dp_{\perp}} \bigg/ \frac{d\sigma^{\text{jet,vac}}(p_{\perp})}{dp_{\perp}}$$

Induced radiation



Decoherence :: the virtual gluon fluctuates until it reaches the size $\Delta x_{\perp}^2 \sim (\tilde{q}\Delta t)^{-1}$ where it can be resolved by the medium.

$$\left. \begin{aligned} t_{\text{br}} &= \lambda_{\text{mfp}} N_{\text{coh}} \\ k_{\text{br}}^2 &= \mu^2 N_{\text{coh}} \end{aligned} \right\} \begin{aligned} t_{\text{br}} &= \sqrt{\omega/\hat{q}} \\ k_{\text{br}}^2 &= \sqrt{\hat{q}\omega} \end{aligned}$$

$\lambda_{\text{mfp}} \rightarrow t_{\text{br}} \quad ::$ Landau-Pomeranchuk-Migdal effect

Bethe-Heitler regime

$$t_{\text{br}} \sim \lambda_{\text{mfp}}$$

$$\omega_{\text{BH}} = \lambda^2 \hat{q} \sim \lambda m_D^2$$

Factorization regime

$$t_{\text{br}} \sim L$$

$$\omega_c = \hat{q} L^2$$

LPM regime

$$\omega_{\text{BH}} \ll \omega \ll \omega_c$$

Baier, Dokshitzer, Mueller, Peigné, Schiff (1997-2000), Zakharov (1996),
Wiedemann (2000), Gyulassy, Levai, Vitev (2000), Arnold, Moore, Yaffe (2001)

The rate-equation

Multiple emission regime

- independent emission
- possible in large media
- very soft radiation at large angles!

$$\omega_{\text{BH}} \ll \omega \ll \bar{\alpha}^2 \omega_c$$

$$\theta \gg \theta_{\text{br}} \equiv (\hat{q}/\omega^3)^{1/4}$$

Blaizot, Dominguez, Iancu, Mehtar-Tani 1209.4585

$$\frac{\partial}{\partial \tau} D(x, \tau) = \int_{\mathcal{C}} dz \mathcal{F}(z, x; \tau) \left[\sqrt{\frac{z}{x}} D\left(\frac{z}{x}, \tau\right) - \frac{z}{\sqrt{x}} D(x, \tau) \right]$$

Jeon, Moore hep-ph/0309332

Baier, Mueller, Schiff, Son hep-ph/0009237

Blaizot, Iancu, Mehtar-Tani 1301.6102

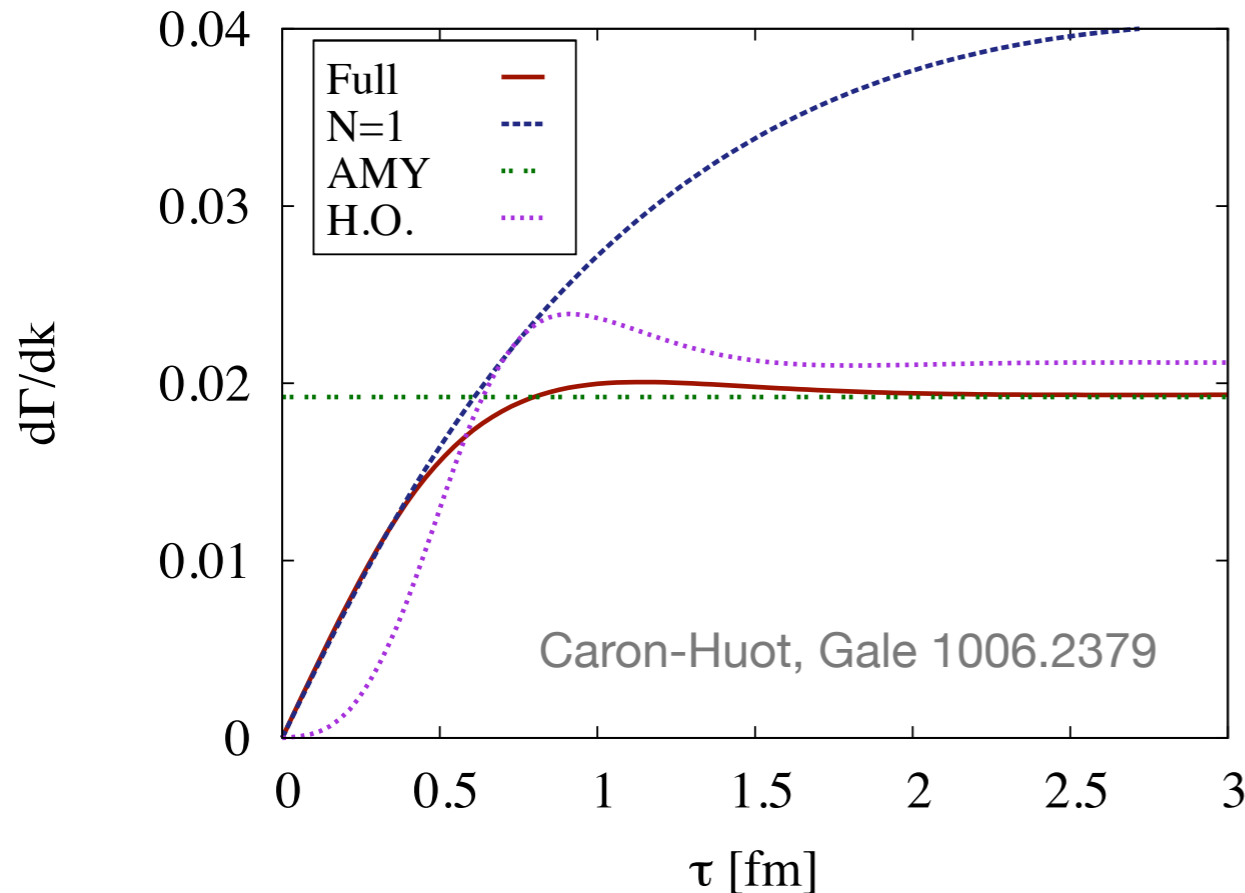
$$\tau = \bar{\alpha} \sqrt{\frac{\omega_c}{E}}$$

Analytical solution (infinite length):

$$D_0(x, \tau) = \frac{\tau}{\sqrt{x}(1-x)^{3/2}} e^{-\pi \frac{\tau^2}{1-x}}$$

- keeps track of the leading + all the fragments
- **probabilistic interpretation**
- **turbulent flow**: no intrinsic accumulation of energy
- spectrum is self-replicating :: **scaling**

Finite-size effects



- including finite-size effects in the ‘harmonic oscillator’ approximation
- could be improved by including the full rate or interpolate between N=1 and HO

$$z \frac{dI^{\text{ind}}}{dz} = \frac{\alpha_s}{2\pi} z P_{gg}(z) \ln \left| \cos(1+i) \sqrt{\frac{\hat{q}_{\text{eff}} L^2}{z(1-z)p^+}} \right| \Rightarrow z \frac{dI^{\text{ind}}}{dz dL}$$

$$k_{\text{br}}^2 = \sqrt{z(1-z)p_0^+ \hat{q}_{\text{eff}}} \quad \hat{q}_{\text{eff}} = \hat{q} \left[(1-z)N_c - zC_R \right]$$

Regularization

$$\frac{d^2 \mathcal{P}}{dz d\tau} = \frac{1}{2} \frac{\mathcal{F}(z, x; \tau)}{\sqrt{x}}$$

$$x_c = \omega_c / p_0^+ \quad \tau \equiv \bar{\alpha} \sqrt{2x_c}$$

$$\mathcal{F}(z, x; \tau) = \tilde{P}_{gg}(z) \mathcal{K}(z) \frac{\sinh \sigma(z, x; \tau) - \sin \sigma(z, x; \tau)}{\cosh \sigma(z, x; \tau) + \cos \sigma(z, x; \tau)}$$

$$\sigma(z, x; \tau) = \frac{\mathcal{K}(z)}{\bar{\alpha} \sqrt{x}} \tau$$

$$\tilde{P}_{gg}(z) = \frac{(1 - z(1 - z))^2}{[z(1 - z)]_{\epsilon_1}}$$

$$\mathcal{K}(z) = \sqrt{\frac{1 - z(1 - z)}{[z(1 - z)]_{\epsilon_2}}}$$

$$t_{\text{br}} \sim \lambda_{\text{mfp}} \Rightarrow \omega_{\text{BH}} = \lambda_{\text{mfp}}^2 \hat{q} \\ \sim m_D^2 \lambda_{\text{mfp}}$$

$$k_{\perp} \sim k_{\text{br}} < \omega$$

$$\Downarrow \\ \omega < \hat{q}^{1/3}$$

$$\lambda_{\text{mfp}} > 1/m_D \Rightarrow \omega_{\text{BH}} > \hat{q}^{1/3}$$

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$$\Downarrow$$

$$\omega < \hat{q}^{1/3}$$

$$\lambda_{\text{mfp}} > 1/m_D \Rightarrow \omega_{\text{BH}} > \hat{q}^{1/3}$$

reg1: $\frac{1}{(1 - z)_{\epsilon}} = \frac{\xi(\xi - x)}{(\xi - x + x_{\text{BH}})^2}$ 'strong'

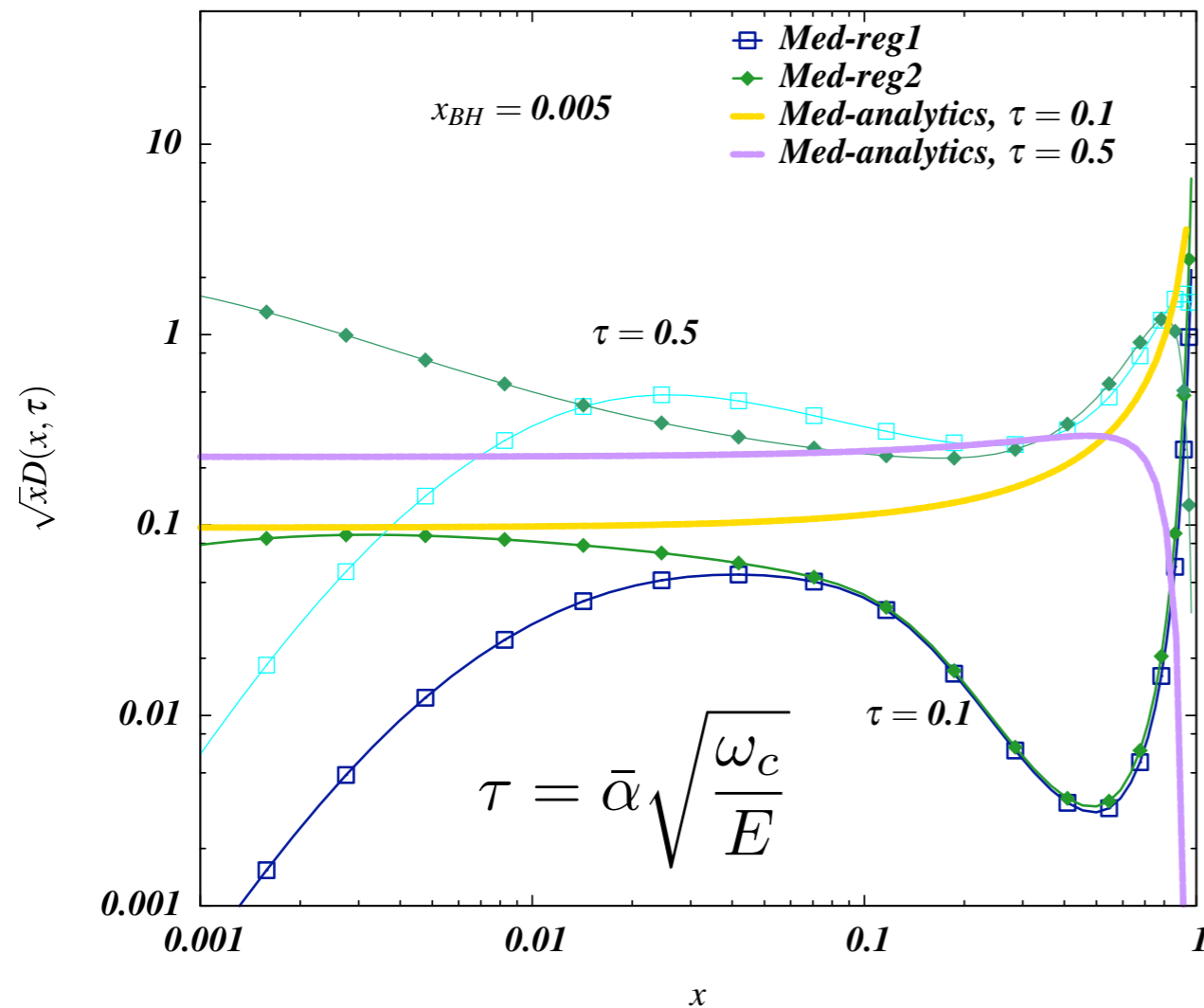
reg2: $\frac{1}{(1 - z)_{\epsilon}} = \frac{\xi}{\xi - x + x_{\text{BH}}}$ 'smooth'

$$x_{\text{BH}} = \omega_{\text{BH}} / E$$

$$\xi = x/z$$

→ apply it only to the medium κ

Evolution equation



Blaizot, Iancu, Mehtar-Tani 1301.6102
 [...work in progress]

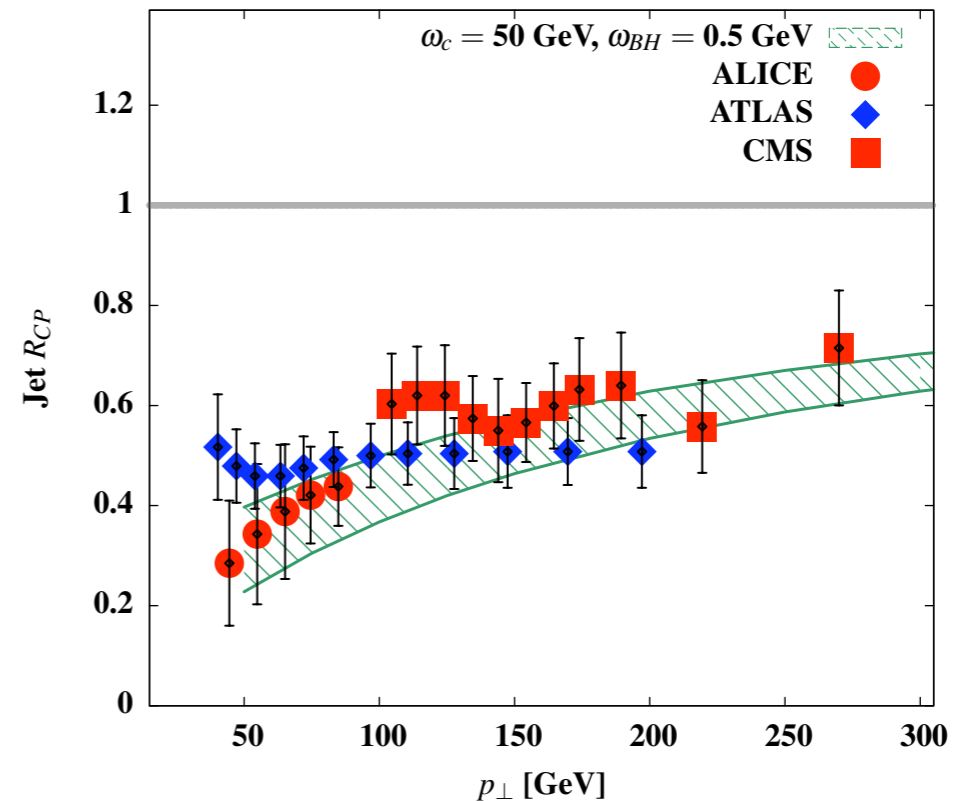
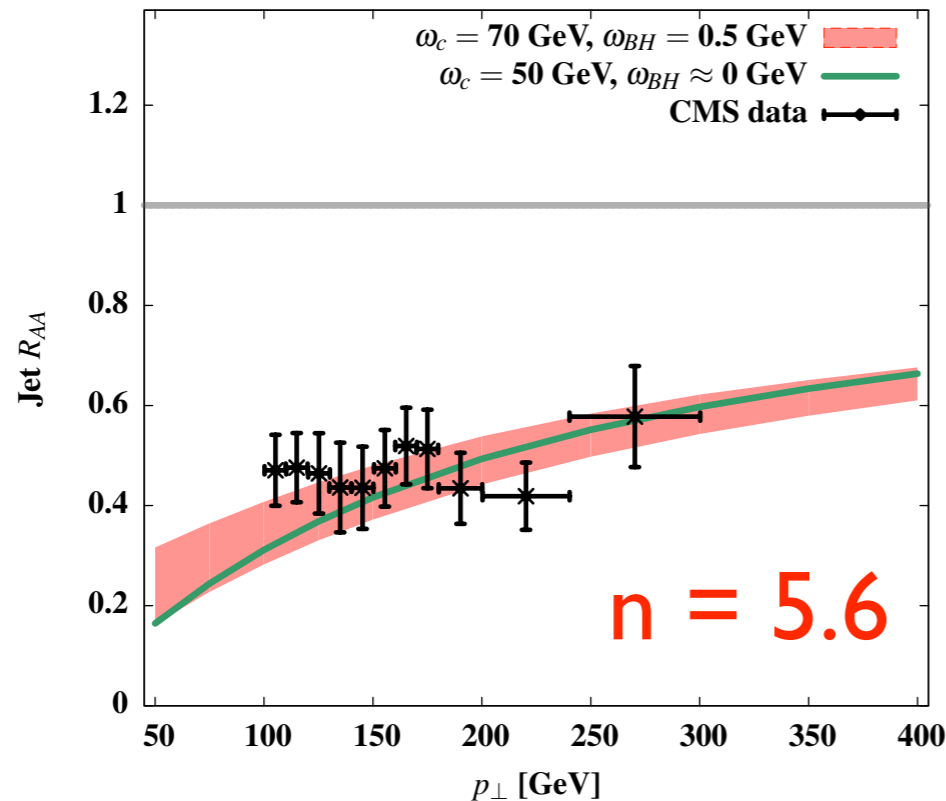
- rapid depletion of leading probe into soft fragments
- finite-size and regularization play a significant role
- slows down the evolution
- important for phenomenological analysis

Analytical solution (infinite length):

$$D_0(x, \tau) = \frac{\tau}{\sqrt{x}(1-x)^{3/2}} e^{-\pi \frac{\tau^2}{1-x}}$$

Jet suppression

Calculating quenching factor for “leading sub-jet”



- sensitivity to regularization prescription
- low- p_T sensitive to **sub-leading resolved subjets**
- baseline: need more **realistic collision geometry**

$$\hat{q} \sim 1 - 2 \frac{\text{GeV}^2}{\text{fm}}$$

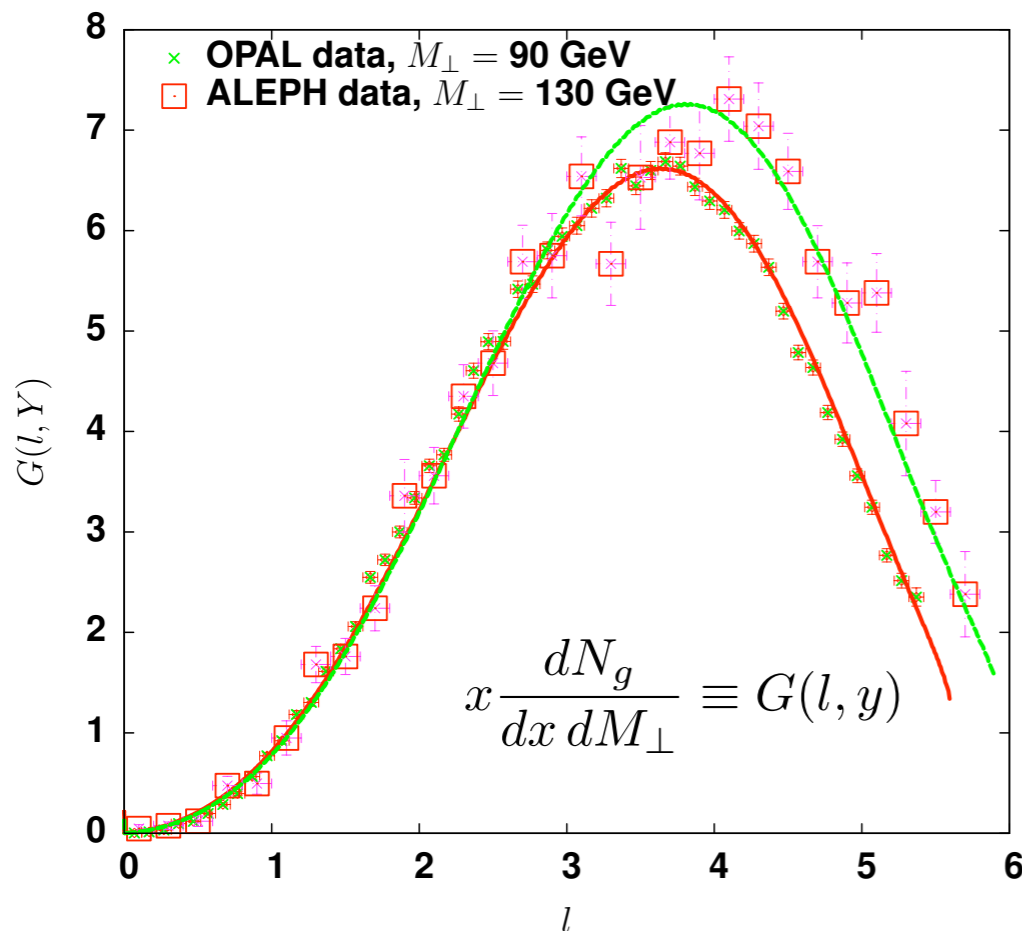
$\omega_c = 70 \text{ GeV}$
 $L \sim 4 \text{ fm}$

MLLA evolution

$$G(l, y) = \delta(l) + \int_0^l dl' \int_0^y dy' \gamma_0^2(l' + y') [1 - a\delta(l - l')] G(l', y')$$

$$l = \ln(1/x) \quad y = \ln(xM_\perp/Q_0) \equiv Y - l$$

$$\gamma_0(\alpha_s) = \sqrt{2N_c\alpha_s/\pi}$$



- LPHD (K factor)

- including mass effect: $E_h = \sqrt{p_h^2 + m_h^2}$

- good description of e^+e^- data

- iterative procedure ($\alpha_s = \text{const}$):

$$G^{(0)}(l, y) = \delta(l)$$

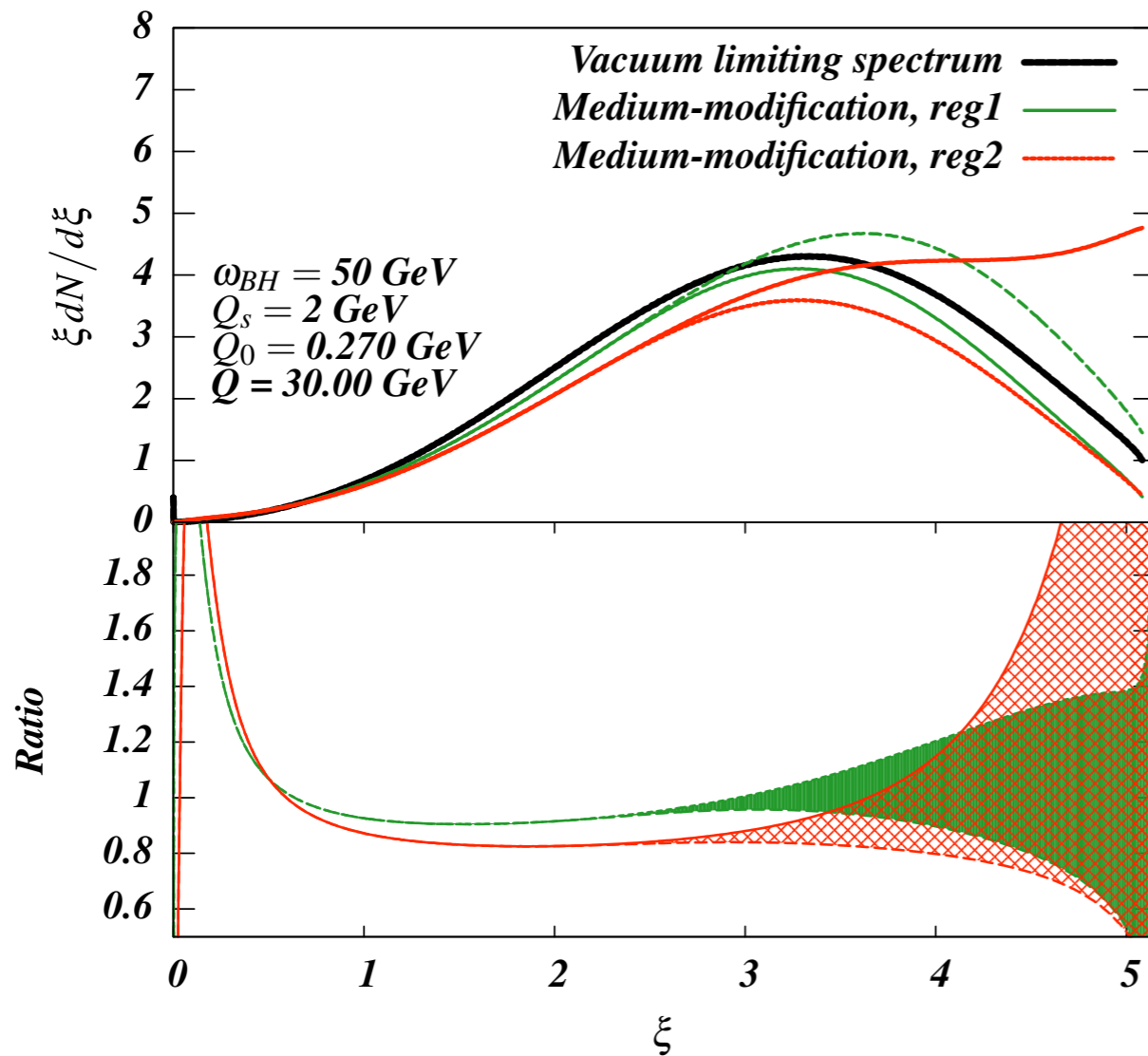
:: initial condition

$$G^{(1)}(l, y) = \gamma_0^2 y [1 - a\delta(l)]$$

$$G^{(2)}(l, y) = \gamma_0^2 y \left[\frac{1}{2} \gamma_0^2 l y - a\gamma_0^2 y + a^2 \delta(l) \right]$$

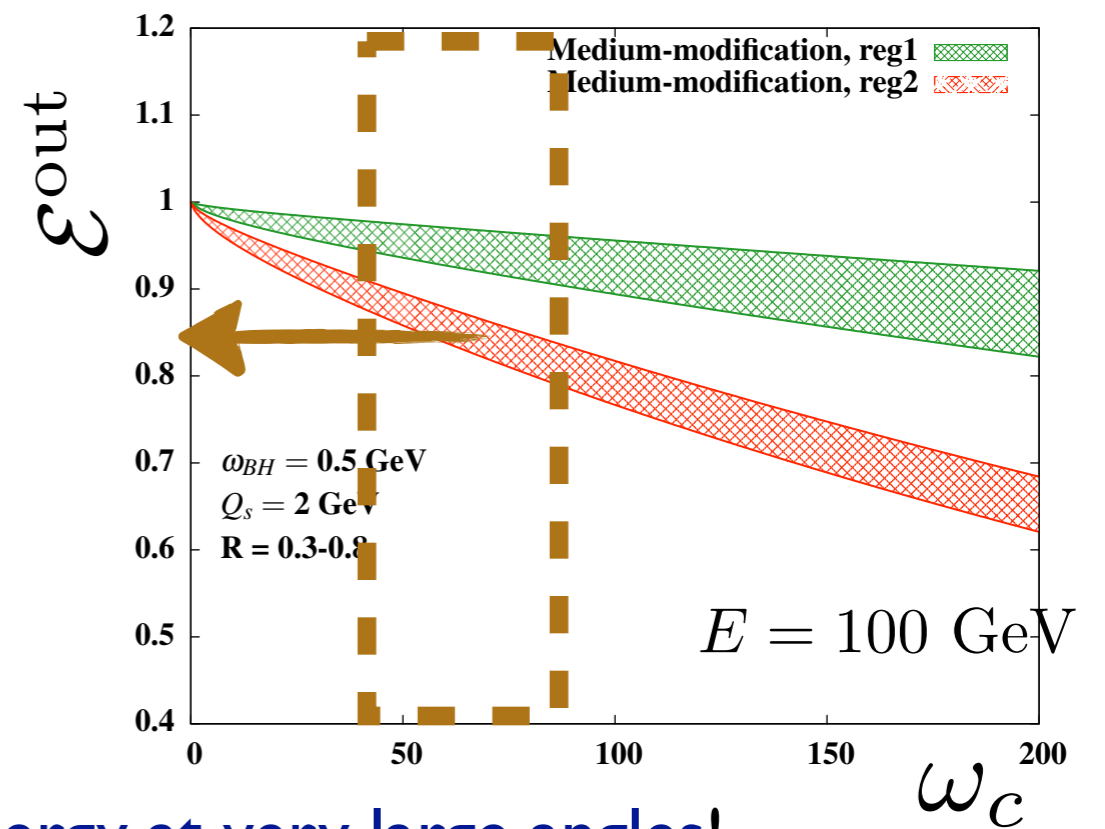
Dokshitzer, Khoze, Mueller, Troyan "Basics of pQCD"
Ramos hep-ph/0605083

Broadening effect



$$D(x, \theta < \Theta_{jet}) = \int^{\Theta_{jet}} \frac{d^2 \mathbf{k}}{(2\pi)^2} \mathcal{P}(\mathbf{k}) D(x),$$

$$\theta \lesssim \theta_c = \left[1 - \exp\left(-\frac{x^2 M_T^2}{Q_s^2}\right) \right] D(x)$$



- strong sensitivity in the **soft sector**
- broadening a powerful effect: **missing energy at very large angles!**

Antiangular component

$$dN_{q,\gamma^*}^{\text{tot}} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{\sin \theta}{1 - \cos \theta} \frac{d\theta}{d\theta} [\Theta(\cos \theta - \cos \theta_{q\bar{q}}) + \Delta_{\text{med}} \Theta(\cos \theta_{q\bar{q}} - \cos \theta)] .$$

$$k_{\perp} < Q_{\text{hard}}$$

DLA accuracy ($a=0$) :: affects only 2nd emission

Estimating the phase space for AAO emission:

$$\int_{\Gamma_{\text{med}}} \frac{dz}{z} \frac{d\theta'}{\theta'} = \int_{\Gamma_{\text{vac}}} \frac{dz}{z} \frac{d\theta'}{\theta'} + \Delta_{\text{med}} \int_x^{\frac{Q_{\text{hard}}}{M_{\perp}}} \frac{dz}{z} \int_{\Theta_{\text{jet}}}^{\frac{Q_{\text{hard}}}{xE}} \frac{d\theta'}{\theta'}$$

$$l_{\text{max}} = \log \frac{Q_{\text{hard}}}{xM_{\perp}} = \lambda_2 - Y + l$$

$$y_{\text{max}} = \log \frac{Q_{\text{hard}}}{Q_0} = \lambda_2$$

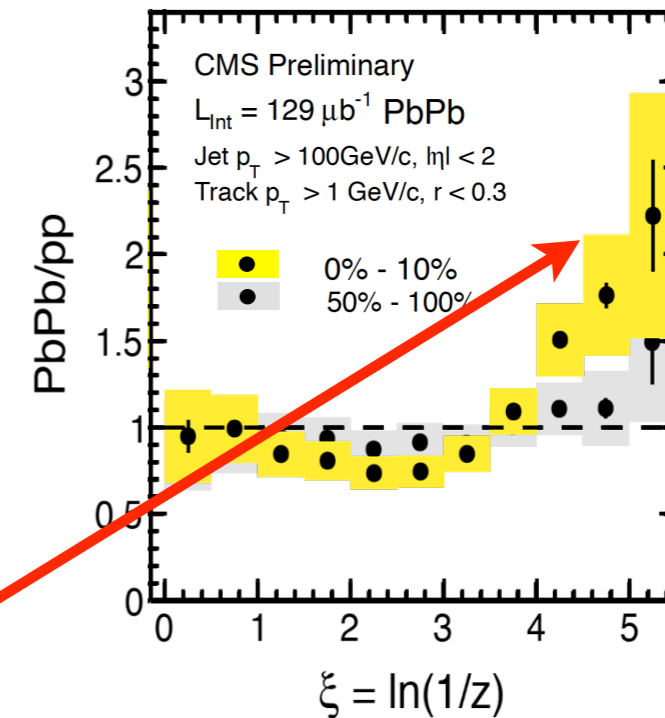
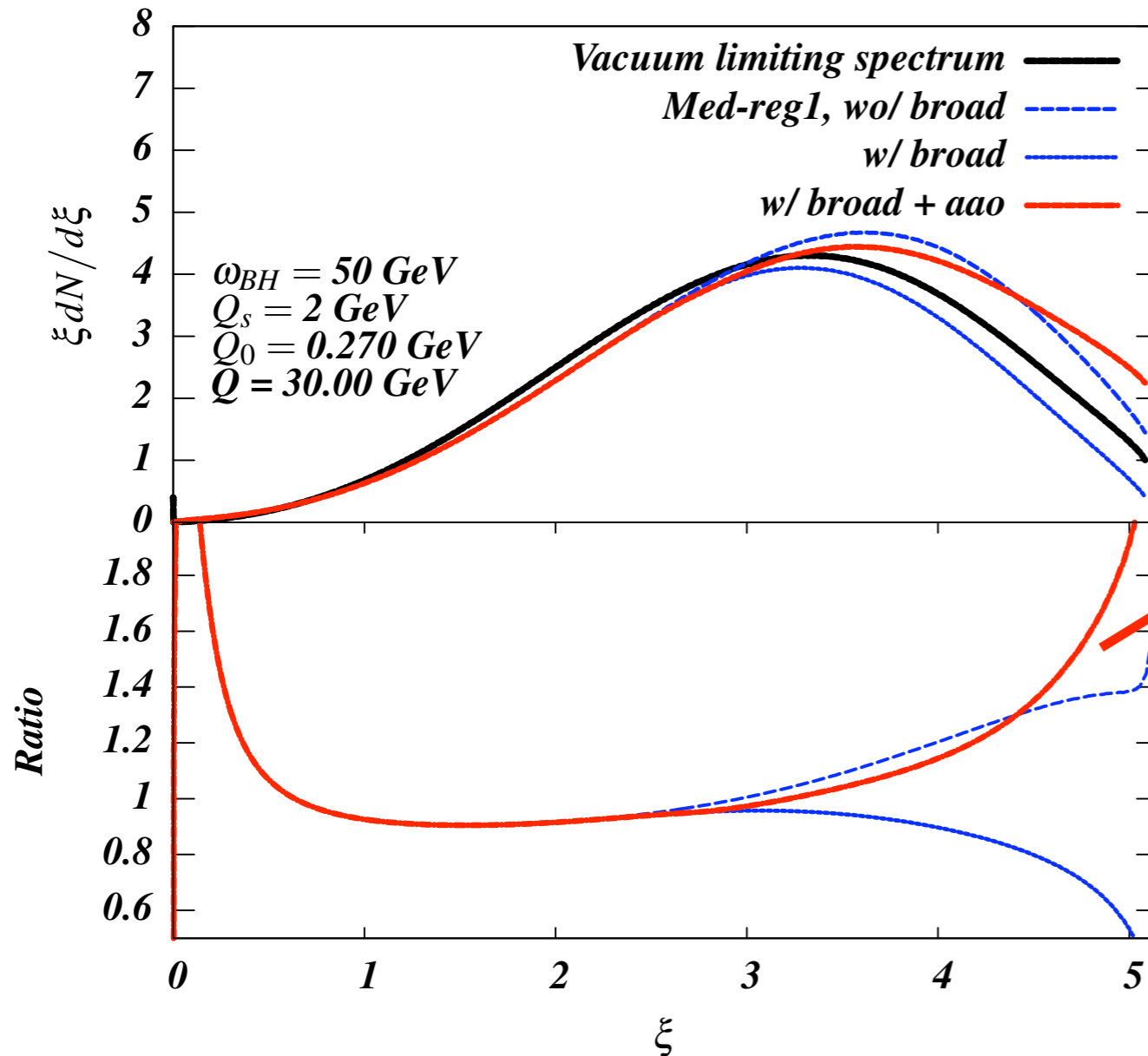
$$y_{\text{min}} = \log \frac{xE\theta_0}{Q_0} = Y - l$$

$$G^{(2)}(l, y) \Big|_{a=0} = G_{\text{vac}}^{(2)}(l, y) \Big|_{a=0} + \frac{1}{2} \overbrace{\Delta_{\text{med}} \gamma_0^4}^{\text{constants}} (l + \lambda_2 - Y)(\lambda_2^2 - (Y - l)^2),$$

↪ allows to continue resumming the vacuum emissions!

Full modification

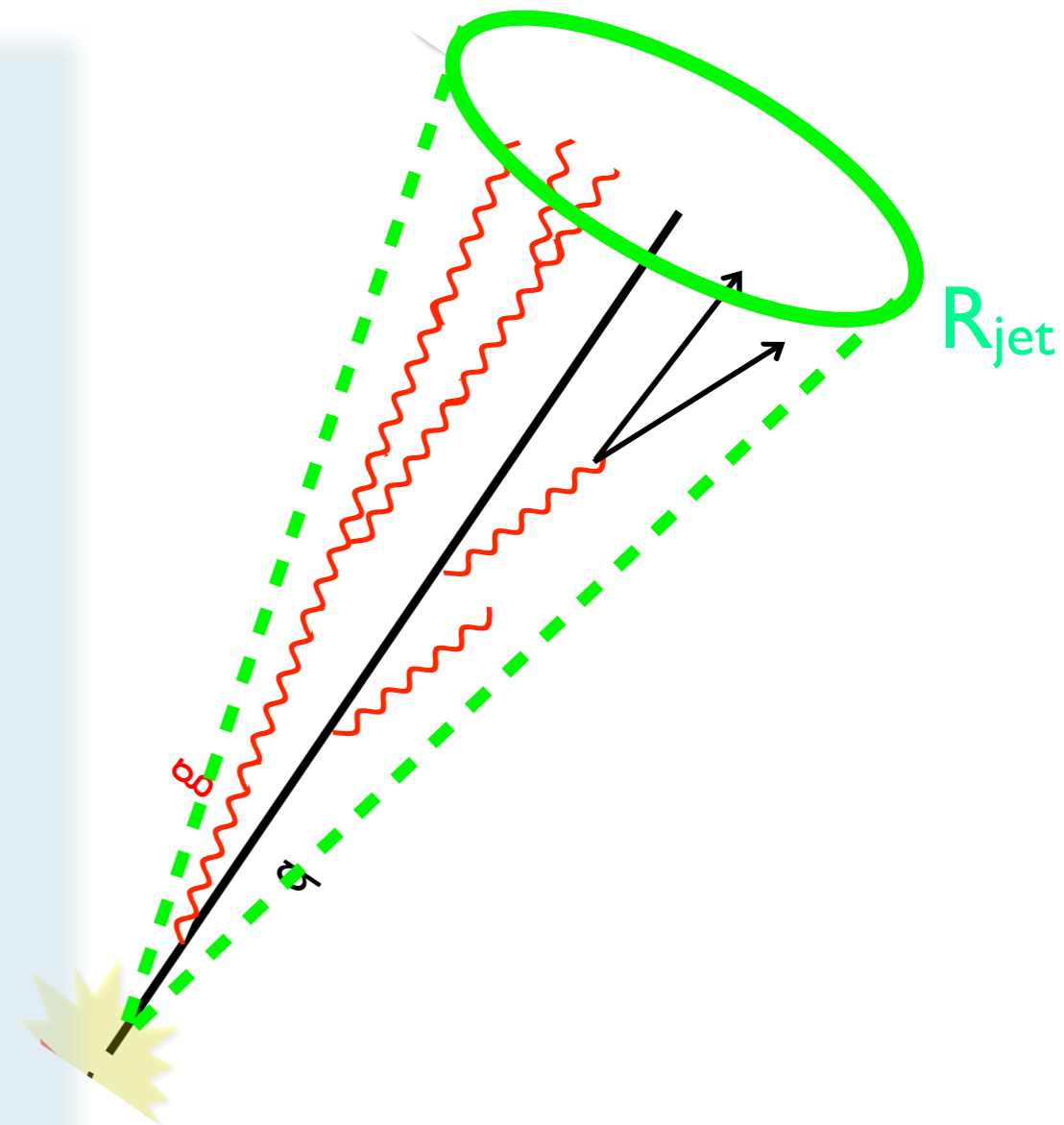
CMS-PAS-HIN-12-013



- AAO valid for soft gluons with **long formation times** → add them on top of modified spectrum
- low-x enhancement inside the cone is delicate :: not sensitive to resolution scales
- sensitive to the **decoherence parameter** (in reality a dynamic quantity)

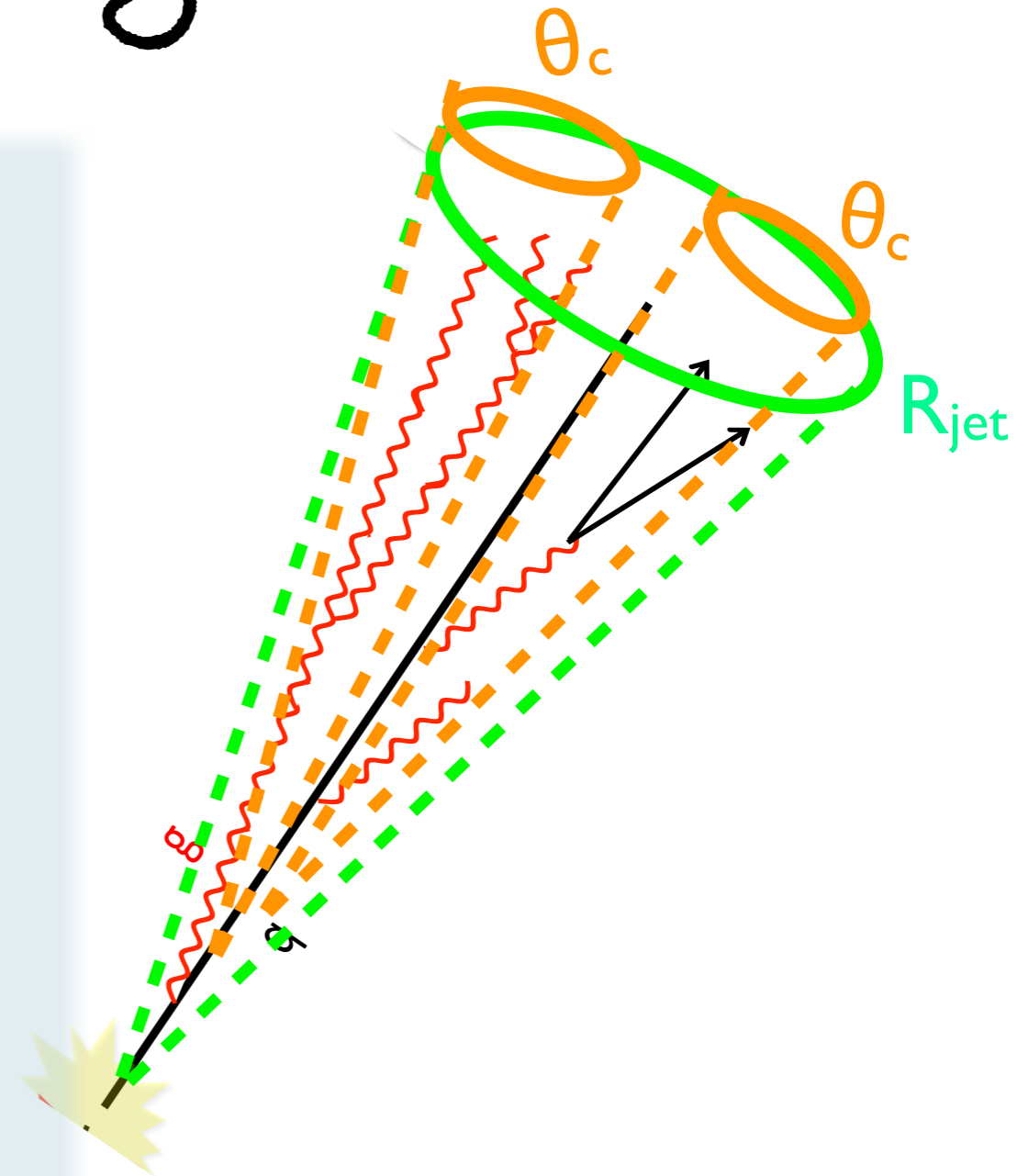
Summary

- three observables (**inclusive jet suppression, modification of the fragmentation function, out-of-cone energy**) constrain mechanisms of “jet quenching”
- color transparency :: **resolved subjets**
- decoherent radiation inside the jet cone :: **a crucial component**
- induced large-angle radiation + broadening :: **transport out of cone**
- good understanding of the data



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backup

Resolved effective charges

