

Universality of Multi-Particle Production in the CGC Framework

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Based on arxiv:1210.1141 in collaboration with C. Marquet, A. Stasto, B. Xiao

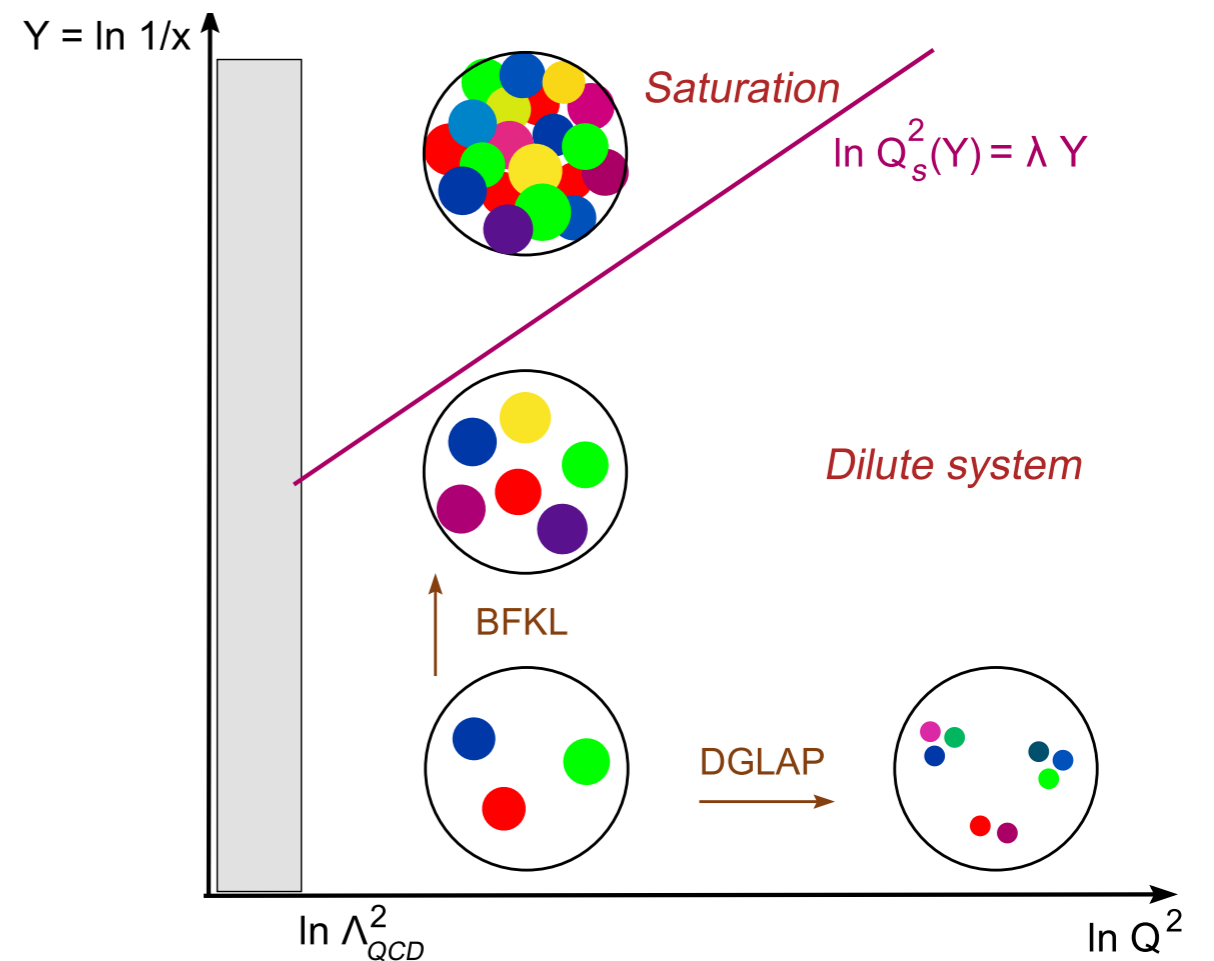
h3QCD Workshop
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Motivation

- Probe the low- x degrees of freedom of hadronic (nuclear) matter
- Look for saturation effects
- Fundamental to understand the early stages of heavy ion collisions

Basics of CGC

- Low- x degrees of freedom considered as classical field due to large occupation numbers
- Properly take into account non-linear effects at high densities
- Energy dependence computed perturbatively (JIMWLK)

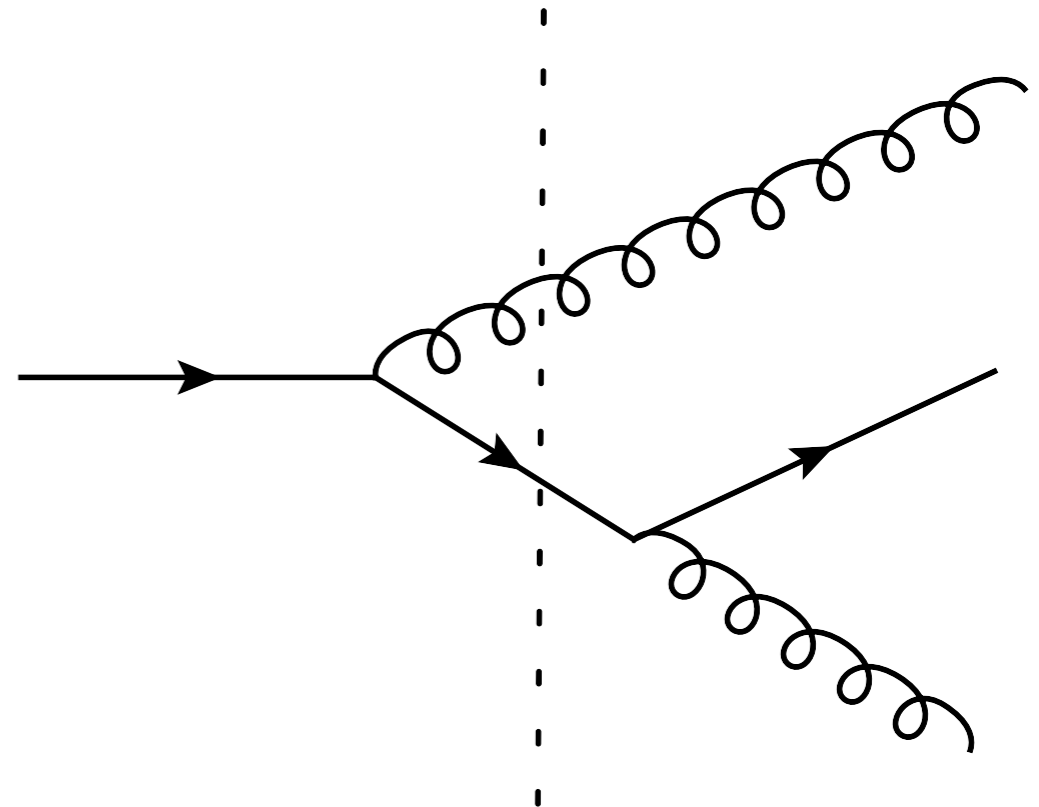


Probing High Density Regime

- Dilute projectile probing a dense target (DIS, pA collisions)
- Use the eikonal approximation to account for the multiple scatterings of a fast moving parton in a background field (in a covariant gauge)
- Calculate observables in a fixed background field, then average over field configurations with an appropriate weighting functional
- Medium effects are visible through the field correlators

Particle Production

- High energy parton splits
- Whole system interacts coherently with high energy target
- Interaction looks instantaneous due to Lorentz contraction
- Final particles can have any rapidity



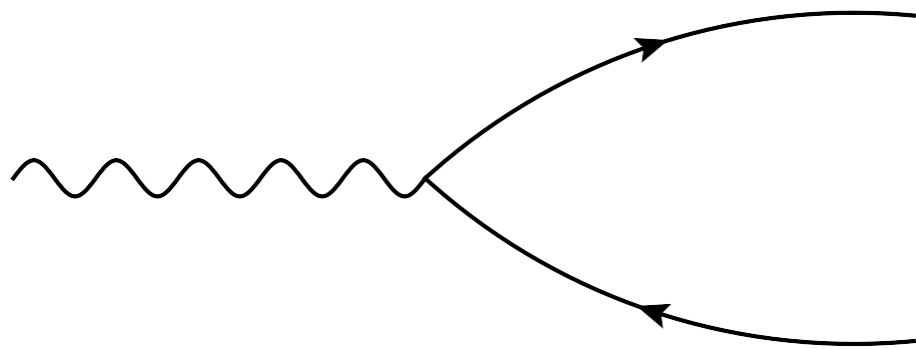
Known Results

- DIS total cross section
- One-particle observables
 - SIDIS
 - Single-hadron production in pA collisions
 - Vector meson photoproduction
- Two-particle observables
 - Di-hadron production in DIS
 - Di-hadron production in pA collisions
 - Quark channel
 - Gluon channel

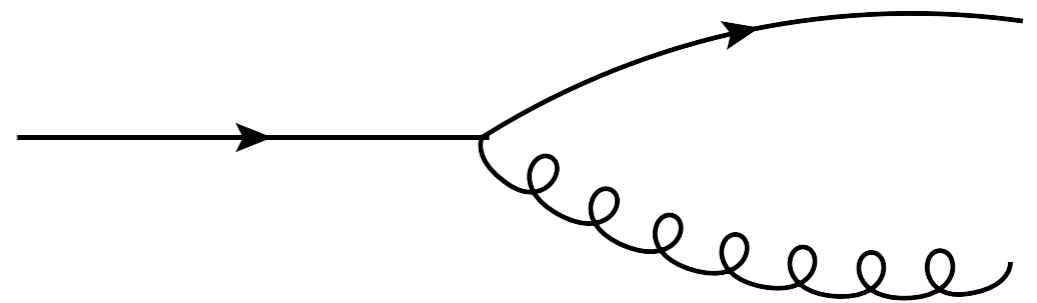
See talks by Heikki Mantysaari
and Julien Laidet

Wilson Lines

At the amplitude level:



$$1 - U(x_1)U^\dagger(x_2)$$

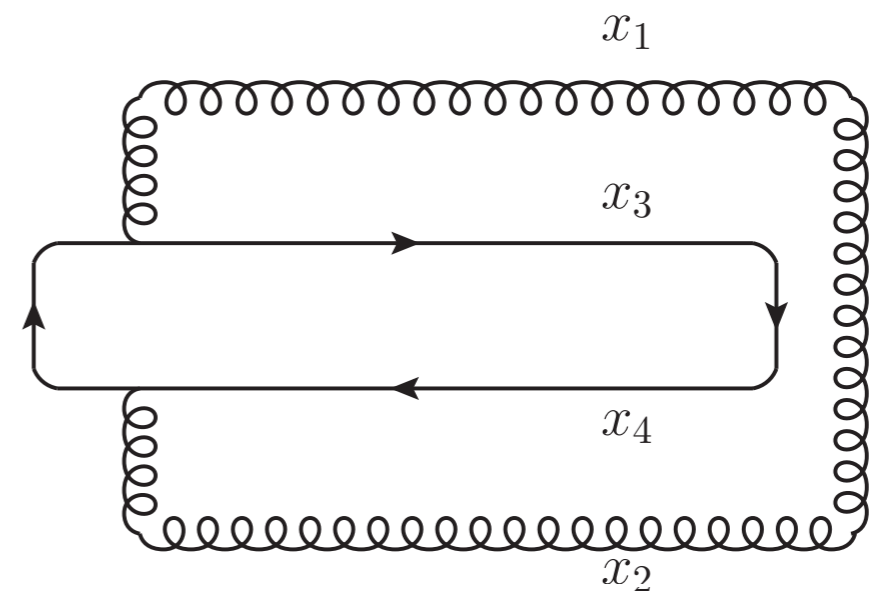
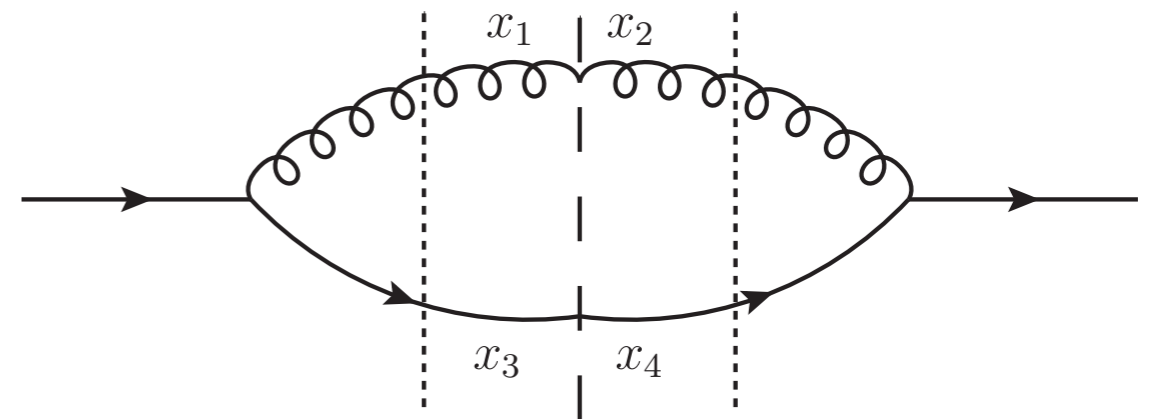


$$U(v)T^a - \tilde{U}_{ab}(x_2)T^b U(x_1)$$

Color Structure

At the cross section level:

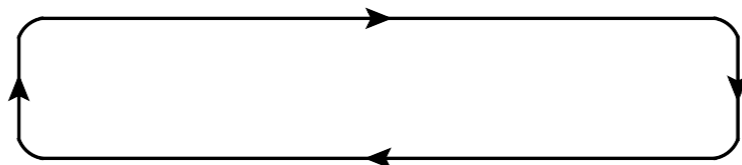
- Color conservation implies average is performed over an overall color singlet object



$$\text{Tr}(T^b T^a U(x_3) U^\dagger(x_4)) \tilde{U}_{ac}(x_1) \tilde{U}_{bc}^\dagger(x_2)$$

Inclusive Observables

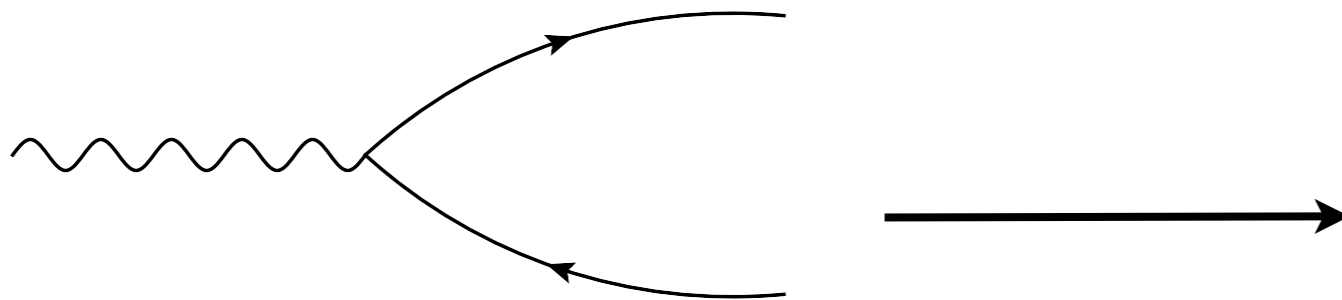
- Integrating over transverse momentum puts the particle at the same transverse coordinate in the amplitude and conjugate amplitude
- Real-virtual cancelations take place
- Total cross sections and single-particle observables can be described with only dipole amplitudes



Two-Particle Observables

- Having two independent momenta in the final state leads to four independent transverse coordinates
- Cross sections involve traces of four Wilson lines at different coordinates

Di-hadron in DIS:

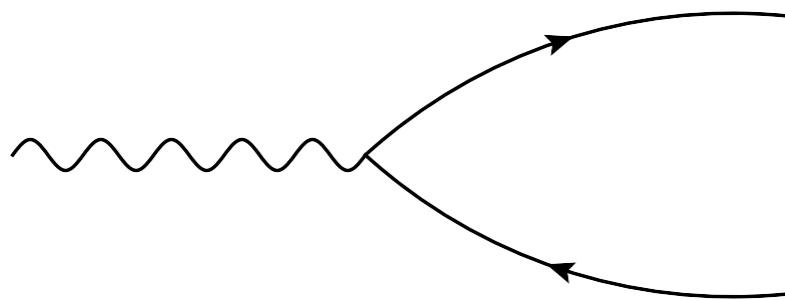


$$1 - U(x_1)U^\dagger(x_2)$$

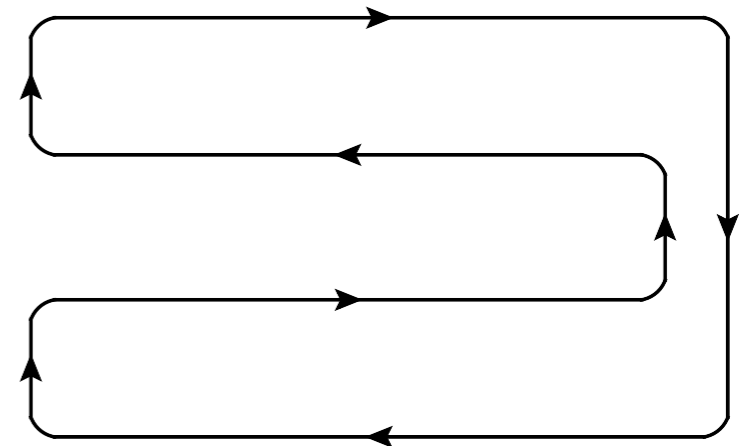
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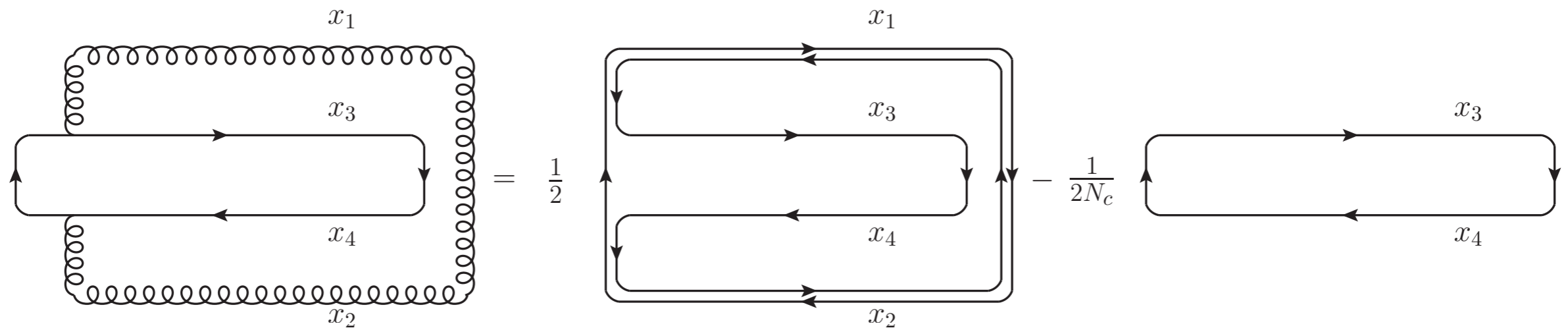
Di-hadron in DIS:



$$1 - U(x_1)U^\dagger(x_2)$$

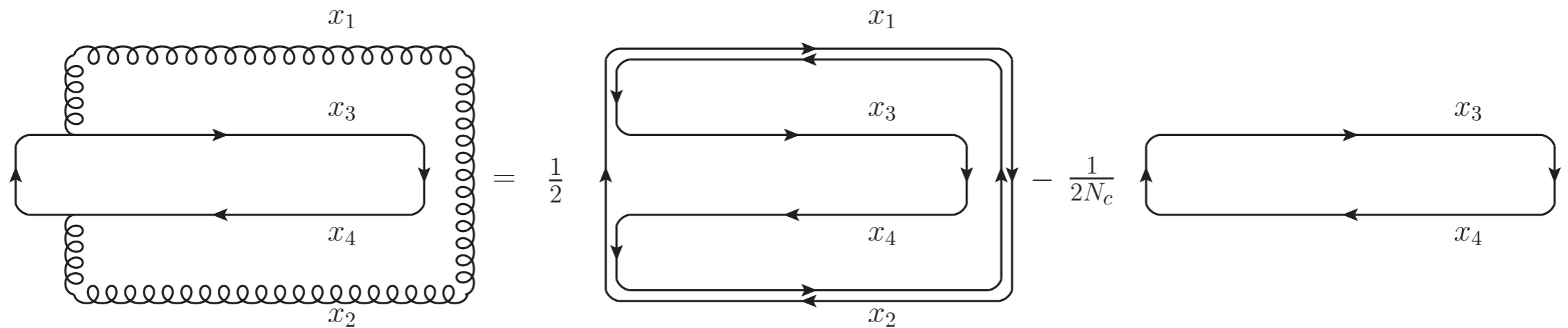


Di-hadron in pA



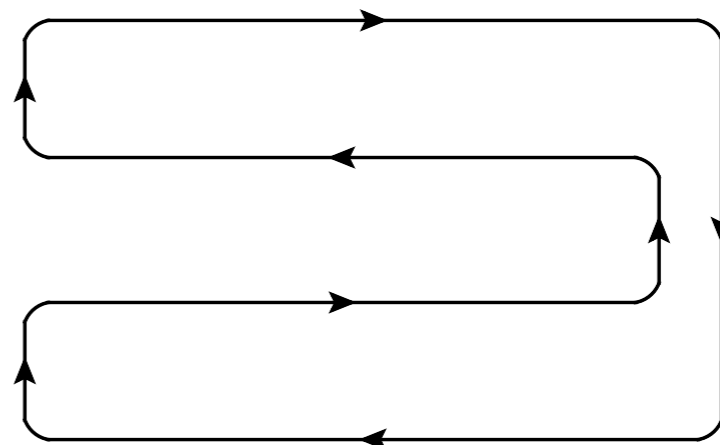
$$\text{Tr} \left(U_1 U_2^\dagger \right) \text{Tr} \left(U_1^\dagger U_3 U_4^\dagger U_2 \right)$$

Di-hadron in pA



$$\text{Tr} \left(U_1 U_2^\dagger \right) \text{Tr} \left(U_1^\dagger U_3 U_4^\dagger U_2 \right)$$

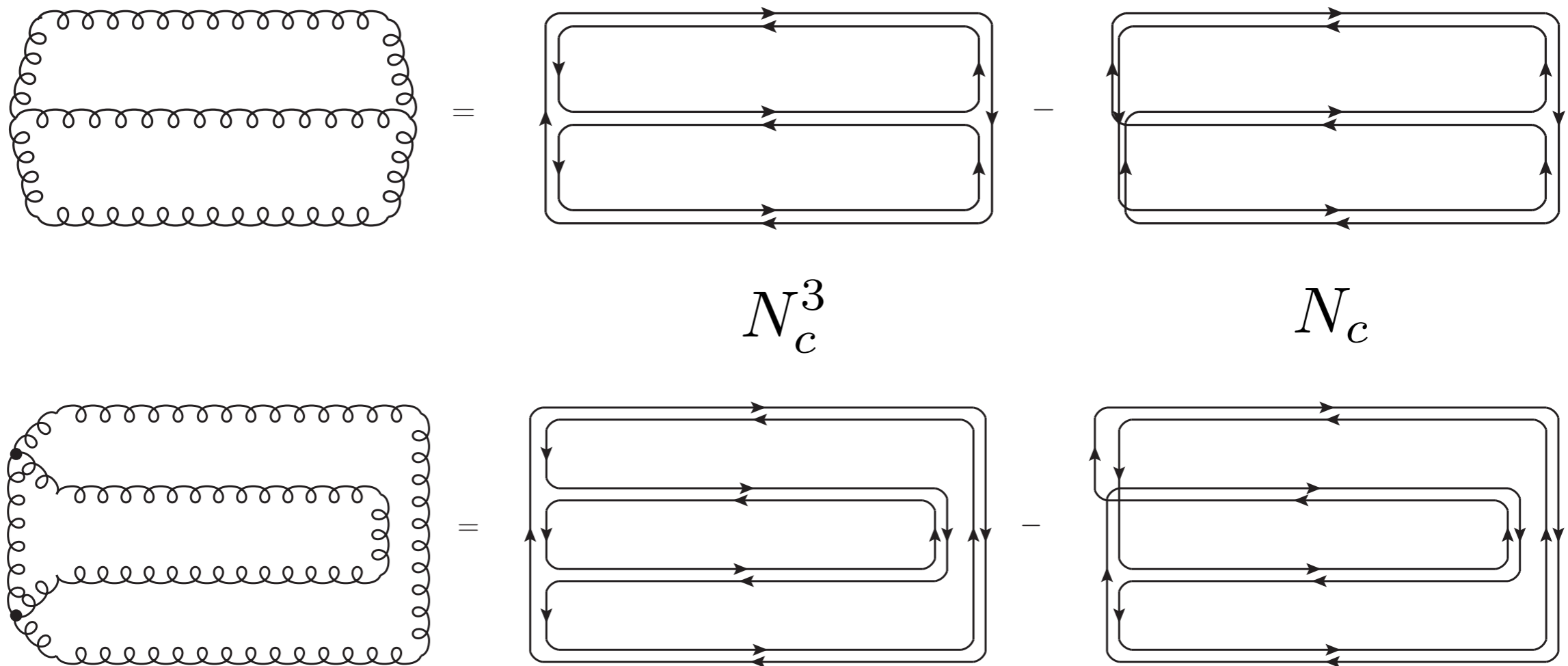
Quadrupole



Large- N_c Limit

- Replace gluon lines with quark-antiquark pairs
- Averages of products of traces of fundamental Wilson lines factorize
- Each trace gives a factor of N_c

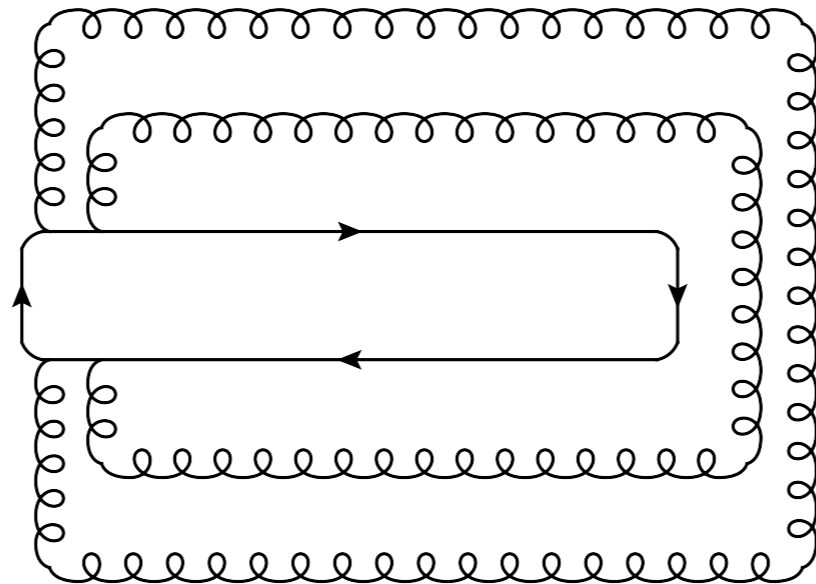
Di-Hadron in pA - Gluon Channel



Diagrams with only dipoles and quadrupoles dominate for large- N_c

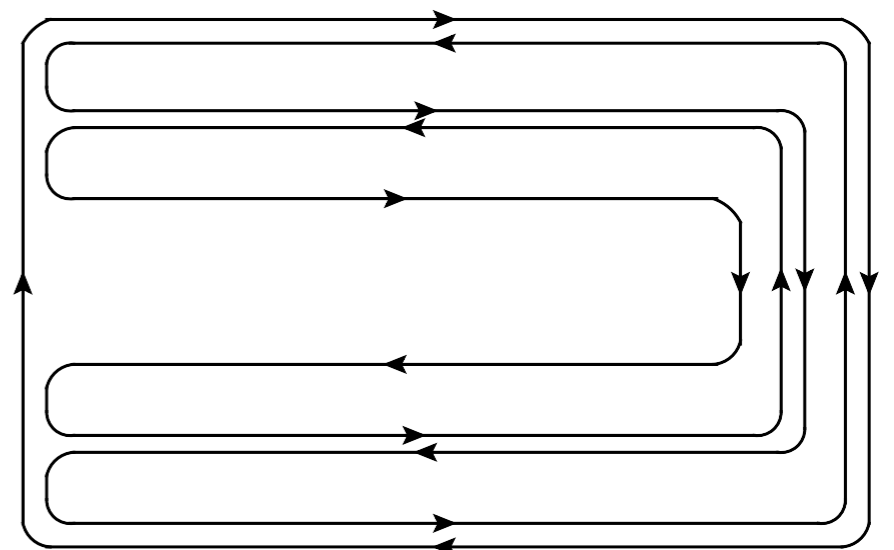
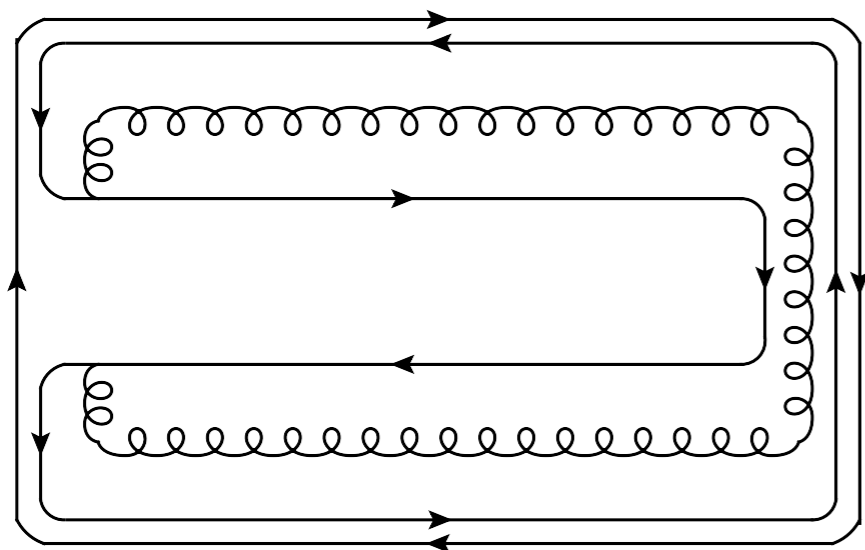
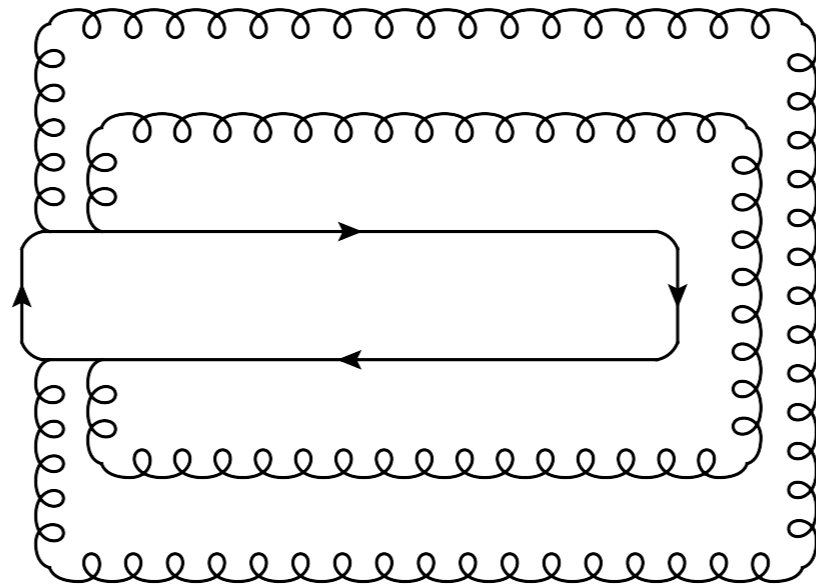
More Complicated Processes

- Adding more particles increases the complexity of the correlators?

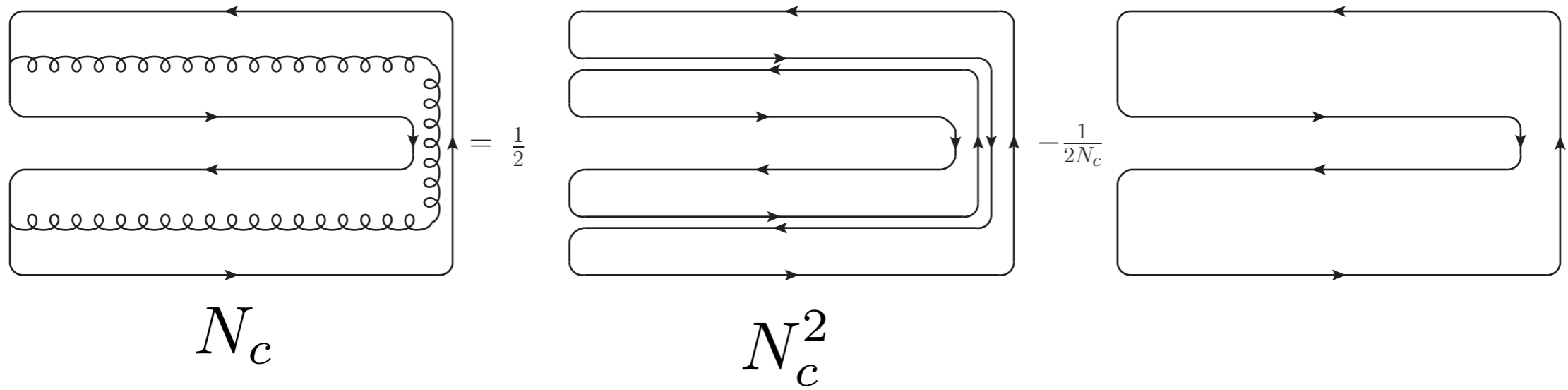


More Complicated Processes

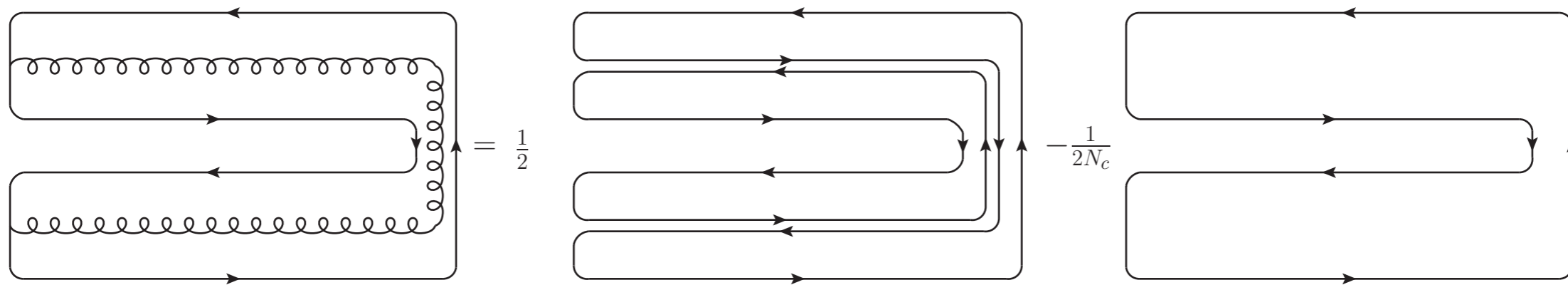
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Adding More Gluons

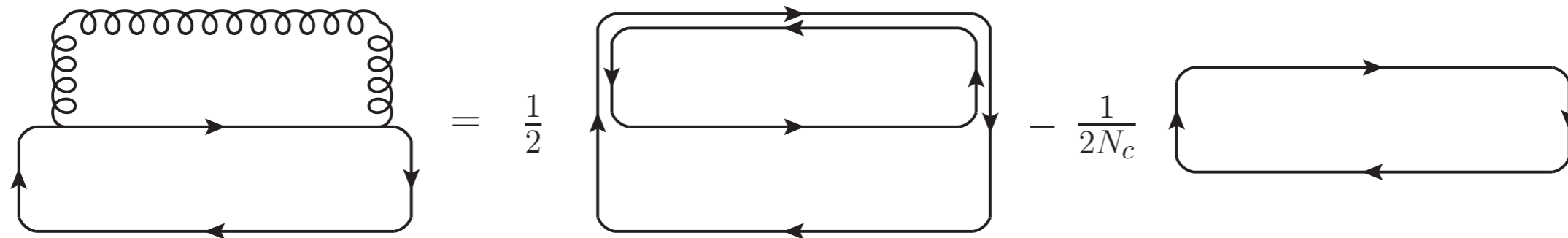


Adding More Gluons



N_c

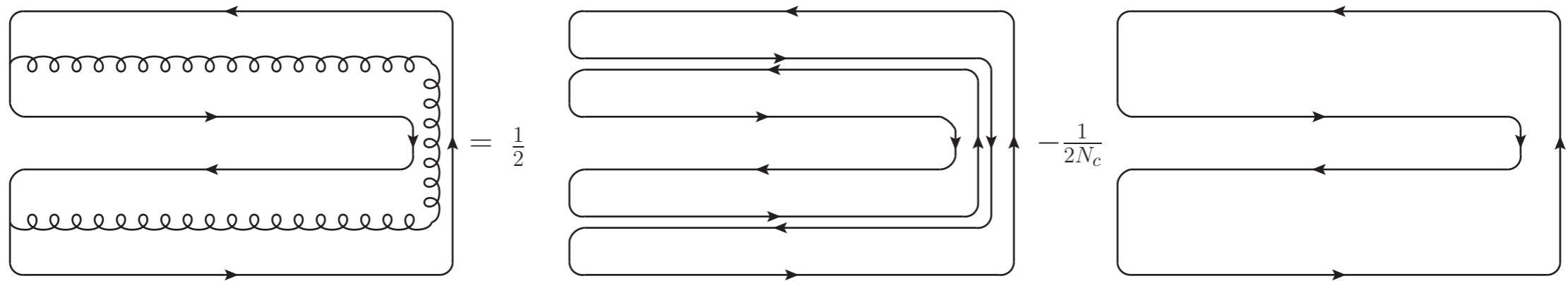
N_c^2



$\frac{1}{2}$

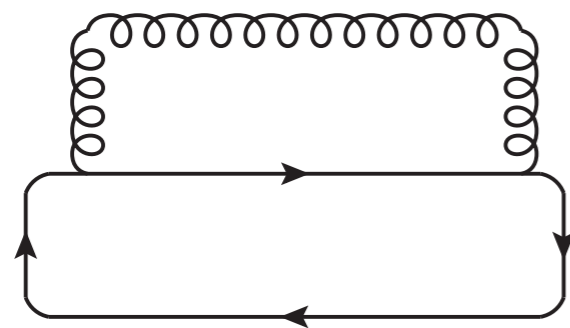
$\frac{1}{2N_c}$

Adding More Gluons

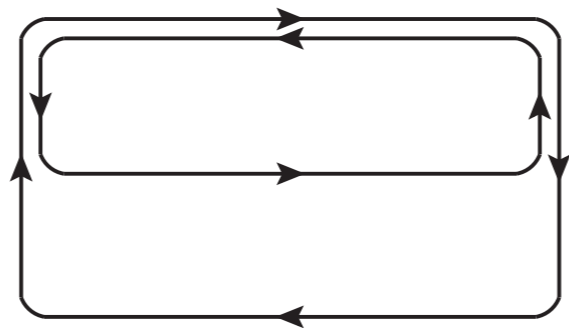


N_c

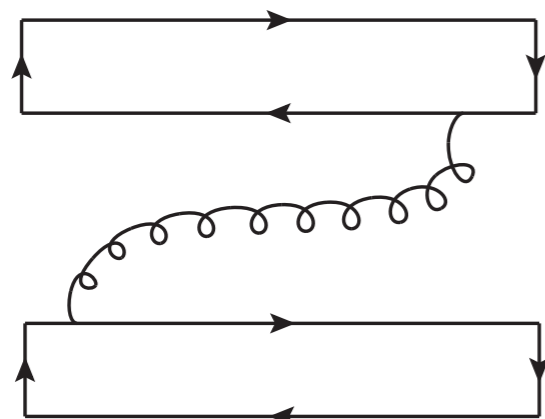
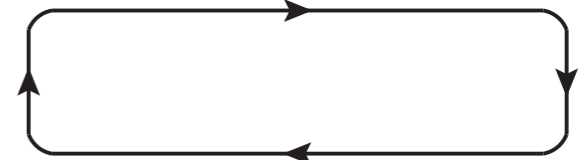
N_c^2



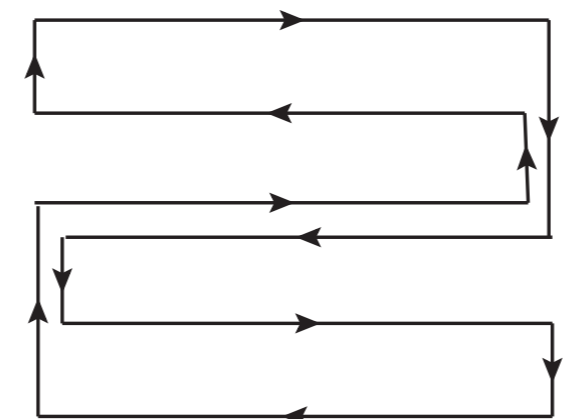
$= \frac{1}{2}$



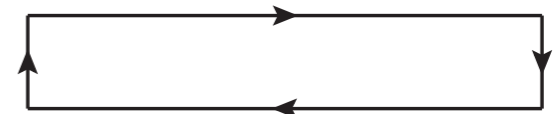
$-\frac{1}{2N_c}$



$= \frac{1}{2}$



$-\frac{1}{2N_c}$



N_c^2

N_c

N_c

Higher Orders

- Diagrammatic analysis does not distinguish between particles in the amplitude and conjugate amplitude
- Most complicated correlators come from diagrams where a maximal number of particles participate in the interaction with the background field
- Additional gluons can be virtual

Summary

- Only dipole and quadrupole amplitudes are necessary for an arbitrary number of particles
- Still valid at higher orders (additional gluons can be virtual fluctuations)
- This property is not affected by evolution in rapidity (see also Kovner and Lublinsky, 2006)
- Valid for any rapidity values of the final particles

Additional Comments

- Even though the analysis was performed under the CGC framework, the same conclusion is valid for any process involving a fast moving parton in a background field (e.g. a hot medium)
- In order to have higher correlators at leading N_c one has to impose restrictions on the final color state (such as bound states forming a singlet - quarkonia)