# Parton Energy Loss in QCD Medium 

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## Piercing the Wall

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The Hope :

## Clarity out of <br> Mess

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again ...

Asymptotic Freedom and

QCD Partons

## Running coupling

The strong coupling, $\alpha_{\mathrm{s}}$, runs:

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& Q^{2} \frac{\partial \alpha_{s}}{\partial Q^{2}}=\beta\left(\alpha_{\mathrm{s}}\right), \quad \beta\left(\alpha_{\mathrm{s}}\right)=-\alpha_{\mathrm{s}}^{2}\left(b_{0}+b_{1} \alpha_{\mathrm{s}}+b_{2} \alpha_{\mathrm{s}}^{2}+\ldots\right), \\
& b_{0}=\frac{11 N_{c}-2 n_{f}}{12 \pi}, \quad b_{1}=\frac{17 N_{c}^{2}-5 N_{c} n_{f}-3 C_{F} n_{f}}{24 \pi^{2}} ; \quad\left(C_{F}=\frac{N_{c}^{2}-1}{2 N_{c}}\right)
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- At high scales $Q$, coupling is weak
$\Leftrightarrow$ quarks and gluons are almost free, their interactions stay under the perturbation theory control
- At low scales, coupling becomes (catastrophically) large $\Rightarrow$ quarks and gluons interact strongly - they are confined into hadrons. Perturbation theory should fail.
- It seems natural to expect the effective interaction strength to decrease at large distances.
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So, why does this most general argument fail in non-Abelian QFT ?

To address questions starting from what or why we better talk physical degrees of freedom; use the Hamiltonian language. Then, we have gluons of two sorts: 'physical' transverse gluons and the Coulomb gluon field mediator of the instantaneous interaction between colour charges.

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Instantaneous Coulomb interaction


$$
=-\mathbf{N}_{\mathrm{c}} * \frac{1}{3}-\mathrm{n}_{\mathrm{f}} * \frac{2}{3}
$$

Transverse gluons (and quarks)

## $\Delta$ <br> I <br> screening

Consider Coulomb interaction between two (colour) charges :
ANTI screening

$$
\begin{gathered}
1 \\
1 \\
\sqrt{7}
\end{gathered}
$$

Instantaneous Coulomb interaction


## Autopsy of Asymptotic Freedom

## Consider Coulomb interaction between two (colour) charges :



Combine into the QCD $\beta$-function:

$$
\beta\left(\alpha_{s}\right)=\frac{\mathrm{d}}{\mathrm{~d} \ln Q^{2}} 4 \pi \alpha_{s}^{-1}\left(Q^{2}\right)
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$=\left[4-\frac{1}{3}\right] * N_{c}-\frac{2}{3} * n_{f}$


Vacuum fluctuations of transverse fields

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=+N_{c} * 4
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The origin of antiscreening deepening of the ground state under the 2nd order perturbation in NQM:

$$
\Delta E_{0}=\sum_{n} \frac{|\langle 0| \delta V| n\rangle\left.\right|^{2}}{E_{0}-E_{n}}<0
$$

Vacuum fluctuations of transverse fields

Solve $Q^{2} \frac{\partial \alpha_{s}}{\partial Q^{2}}=-b_{0} \alpha_{s}^{2}$

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- Perturbative calculations valid for large scales $Q \gg \Lambda$.
- Not an obvious statement: we deal with hadrons in nature, while applying QCD to quarks and gluons


## Running coupling (cont.)

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Hit hard to see what is it there inside (a childish but productive idea)

Hit hard to see what is it there inside

Heat the Vacuum

- $e^{+} e^{-}$annihilation into hadrons : $e^{+} e^{-} \rightarrow q \bar{q} \rightarrow$ hadrons.

Hit hard to see what is it there inside

Hit the proton (with an electromagnetic/electroweak probe)

- $e^{+} e^{-}$annihilation into hadrons : $e^{+} e^{-} \rightarrow q \bar{q} \rightarrow$ hadrons.
- Deep Inelastic lepton-hadron Scattering (DIS) : $e^{-} p \rightarrow e^{-}+X$.

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Make two hadrons hit each other hard

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$\Rightarrow$ lepton pairs ( $\mu^{+} \mu^{-}$, the Drell-Yan process),
$\Rightarrow$ electroweak vector bosons $\left(Z^{0}, W^{ \pm}\right)$,
$\Rightarrow$ Higgs boson(s)
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Momentum transfer $=$ measure of "hardness"

## Lecture I (9/40) <br> - Hard Processes LDIS <br> Deep Inelastic lepton-proton Scattering



Bit of kinematics: invariant mass of final hadrons
$W^{2}-M_{P}^{2}=(P+q)^{2}-M_{P}^{2}$
$=2(P q)\left(1-\frac{-q^{2}}{2(P q)}\right) \equiv 2(P q) \cdot(1-x)$


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What to expect for elastic and inelastic proton Form Factors $F^{2}\left(q^{2}\right)$ ?

Two plausible and one crazy scenarios for the $\left|q^{2}\right| \rightarrow \infty$ (Bjorken) limit Smooth electric charge distribution:

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Conclusion: Proton is a loosely bound system (of 3 quarks + glue $+\cdots$ )

Bjorken scaling: Partons

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## Equate

Inelastic electron-proton scattering
elastic electron-quark scattering

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\begin{aligned}
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$$
F_{\text {inelastic }}^{2}\left(q^{2}, x\right)=D_{P}^{q}(x) ; \quad\left|q^{2}\right| \rightarrow \infty, x=\text { const }
$$

constitutes the Bjorken scaling hypothesis.


Particle virtualities/transverse momenta in QFT are not limited. In particular, in a DIS process, "partons" (quarks and gluons) may have transverse momenta up to

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As a result, the number of particles turns out to be large in spite of small coupling :

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Such - "collinear" - enhancement is typical for QFTs with dimensionless coupling - "logarithmic" Field Theories.

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As a result, the number of particles turns out to be large in spite of small coupling :

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\int d w \propto \int^{Q^{2}} \frac{\alpha_{s}}{\pi} \frac{d k_{\perp}^{2}}{k_{\perp}^{2}} \sim \frac{\alpha_{s}}{\pi} \ln Q^{2}=\mathcal{O}(1)
$$

Such - "collinear" - enhancement is typical for QFTs with dimensionless coupling - "logarithmic" Field Theories.
Physically, a QFT particle is surrounded by a virtual coat; its visible content depends on the resolution power of the probe $\lambda=\frac{1}{Q}=\frac{1}{\sqrt{-q^{2}}}$

Thus we learned that in QCD the probability to find a parton $q$ inside the target $h$ must depend on the resolution, $Q^{2}$

$$
D_{h}^{q}=D_{h}^{q}\left(x, \ln Q^{2}\right) .
$$

the Feynman-Bjorken picture of partons employed the classical (probabilistic) language:
$\square$

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## Long-living partons fluctuations

## Kinematics of the parton splitting $A \rightarrow B+C$

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This inequality has a transparent physical meaning:

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\frac{z \cdot E_{A}}{\left|k_{B}^{2}\right|} \ll \frac{E_{A}}{\left|k_{A}^{2}\right|}
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strongly ordered lifetimes of successive parton fluctuations !


So long as probability of one extra parton emission is large, one has to consider and treat arbitrary number of parton splittings
-Parton cascades


$$
\frac{P}{\mu^{2}} \gg t_{1} \gg t_{2} \gg t_{3} \gg t_{4} \gg t_{5} \gg \frac{P}{Q^{2}}
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Four basic splitting processes:


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Four basic splitting processes:
$\begin{aligned} & q \rightarrow q(z)+g \\ & \Phi_{q}^{q}(z)=C_{F} \cdot \frac{1+z^{2}}{1-z},\end{aligned}$
$z=k_{5} / k_{4}$


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$$
z=k_{2} / k_{1}
$$

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\Phi_{q}^{g}(z) & =C_{F} \cdot \frac{1+(1-z)^{2}}{z}, \\
\Phi_{g}^{q}(z) & =T_{R} \cdot\left[z^{2}+(1-z)^{2}\right]
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$$
\mu^{2} \ll k_{1 \perp}^{2} \ll k_{2 \perp}^{2} \ll k_{3 \perp}^{2} \ll k_{4 \perp}^{2} \ll k_{5 \perp}^{2} \ll Q^{2}
$$

Four basic splitting processes :
"Hamiltonian" for parton cascades

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\end{aligned}
$$

Logarithmic "evolution time" $\quad d \xi=\frac{\alpha_{s}}{2 \pi} \frac{d k_{\perp}^{2}}{k_{\perp}^{2}}$

## Relating parton splittings

Nowadays we cannot predict, from the first principles, parton content ( $B$ ) of a hadron ( $h$ ). However, perturbative QCD tells us how it changes with the resolution of the DIS process - momentum transfer $Q^{2}$.

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\frac{d}{d \ln Q^{2}} D_{h}^{B}\left(x, Q^{2}\right)=\frac{\alpha_{s}\left(Q^{2}\right)}{2 \pi} \sum_{A=q, \bar{q}, g} \int_{x}^{1} \frac{d z}{z} \Phi_{A}^{B}(z) \cdot D_{h}^{A}\left(\frac{x}{z}, Q^{2}\right)
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## "wave function"

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"Hamiltonian"

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$$

Parton Dynamics turned out to be extremely simple.
Have a deeper look at parton splitting probabilities

- our evolution Hamiltonian -
to fully appreciate the power of the probabilistic interpretation of parton cascades


$$
=T_{R} \cdot\left[z^{2}+(1-z)^{2}\right]
$$



$$
=C_{F} \cdot \frac{1+(1-z)^{2}}{z}
$$



$$
=N_{c} \cdot \frac{1+z^{4}+(1-z)^{4}}{z(1-z)}
$$

Four "parton splitting functions"

$$
{\underset{q}{q}[g]}^{[g),} \quad{\underset{q}{g}[q]}^{[z)}(z), \quad \quad_{g}^{q[\bar{q}]}(z), \quad{\underset{g}{g}}_{g[g]}(z)
$$



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- Exchange the decay products : $z \rightarrow 1-z$

$$
{ }_{q}^{q[g]}(z) \quad{ }_{q}^{g[q]}(z) \quad{ }_{g}^{q[\overline{q]}(z)} \quad{ }_{g}^{g[g]}(z)
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$$


$\sum^{z}$

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Three (QED) "kernels" are inter-related; gluon self-interaction stays put :


Z

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- The story continues, however :

All four are related!

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- The story continues, however :

All four are related! (over-constrained system [+ conformal symm. etc])

Collinear (mass) and soft (infrared) singularities make multi-parton configurations probable, in spite of the smallness of the coupling constant $\alpha_{s}$, thus forcing us to analyze internal structure of small-distance Hard QCD Processes in all orders in perturbation theory.

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## Feynman-Bjorken Partons

Quarks inside proton.
They are point-like.
Bjorken scaling.
Probabilistic picture.

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YES.
NO. They interact, radiate gluons, acquire (double logarithmic) form factors.
NO. $\quad\left(D=D\left(\ln Q^{2}\right)\right)$
YES. And a rich one in that.

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"How do we see and study QCD partons in nature?"

## Hadron Jets

 and
## QCD Radiophysics

## Quarks $\rightarrow$ jets of hadrons



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Repeating, one gets the "Feynman Plateau":
"One" hadron per $\frac{\Delta \omega}{\omega} ; \quad$ Hadron multiplicity $\propto \ln Q$.

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The key features of the Lund hadronization model:

- Uniformity in rapidity: $d N_{h}=$ const $\times \frac{d \omega_{h}}{\omega_{h}}$
- Limited $k_{\perp}$ of hadrons
- Quark combinatorics at work: $\left\{\begin{array}{l}\text { u,d vs. } s \\ \text { mesons vs. baryons }\end{array}\right.$

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The crucial step: Stress on the rôle of colour in multiple hadroproduction

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Moreover,
In $10 \%$ of $e^{+} e^{-}$annihilation events
— striking fluctuations!


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No surprise : (Kogut \& Susskind, 1974)

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The first QCD analysis was done by J.Ellis, M.Gaillard \& G.Ross (1976)

- Planar events with large $k_{\perp}$;
- How to measure gluon spin ;
- Gluon jet - softer, more populated.

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Gluon $\simeq$ quark-antiquark pair:
$3 \otimes \overline{3}=N_{c}^{2}=9 \simeq 8=N_{c}^{2}-1$.
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Lund model interpretation of a gluon -
Gluon - a "kink" on the "string" (colour tube) that connects the quark with the antiquark

Look at hadrons produced in a $q \bar{q}+$ photon $e^{+} e^{-}$annihilation event.
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The hot-dog of hadrons that was "cylindric" in


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Now substitute a gluon for the photon in the same kinematics.


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 quark pair is repainted into octet colour state.

Lund: hadrons $=$ the sum of two independent (properly boosted) colorless substrings, made of

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## The first immediate consequence :

Double Multiplicity of hadrons in fragmentation of the gluon


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- $\frac{d N_{g}}{d N_{q}}=\frac{N_{c}}{C_{F}}=\frac{2 N_{c}^{2}}{N_{c}^{2}-1}=\frac{9}{4} \simeq 2$ ( $\Longrightarrow$ bremsstrahlung gluons add to the hadron yield; QCD respecting parton cascades)


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Now let's look at a more subtle consequence of Lund wisdom


Lund: final hadrons are given by the sum of two independent substrings made of

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Let's look into the inter-quark valley and compare the hadron yield with that in the $q \bar{q} \gamma$ event.
The overlay results in a magnificent
"String effect" - depletion of particle production in the $q \bar{q}$ valley!



QCD prediction :
$\frac{d N_{q \bar{q}}^{(q \bar{q} \gamma)}}{\left.d N_{q}^{q \bar{q}} \bar{q} g\right)} \simeq \frac{2\left(N_{c}^{2}-1\right)}{N_{c}^{2}-2}=\frac{16}{7}$
(experiment: $2.3 \pm 0.2$ )

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Destructive interference from the QCD point of view

Ratios of hadron flows between jets in various multi-jet processes - example of non-trivial CIS (collinear-and-infrared-safe) QCD observable

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Recall an amazing historical example: Cosmic ray physics (mid 50's); conversion of high energy photons into $e^{+} e^{-}$pairs in the emulsion

Charged particle leaves a track of ionized atoms in photo-emulsion. electron track


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$t \simeq \frac{(p+k)_{0}}{(p+k)^{2}} \simeq \frac{p_{0}}{2 p_{0} k_{0}(1-\cos \vartheta)} \simeq \frac{1}{k_{0} \vartheta^{2}} \simeq \frac{1}{k_{\perp}} \cdot \frac{1}{\vartheta}=\lambda_{\perp} \cdot \frac{1}{\vartheta}$

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(DGLAP)

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It was predicted that, due to coherence, "Feynman plateau" $d N / d \ln x$ must develop a hump at

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while the softest particles (that seem to be the easiest to produce) should not multiply at all !

First confronted with theory in $e^{+} e^{-} \rightarrow h+X$.

CDF (Tevatron)
$p p \rightarrow 2$ jets
Charged hadron yield as a function of $\ln (1 / x)$ for different values of jet hardness, versus (MLLA) QCD prediction.

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One free parameter overall normalization (the number of final $\pi$ 's per extra gluon)


Position of the Hump as a function of $Q=M_{j j} \sin \Theta_{c}$ (hardness of the jet)


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Mark Universality:
same behaviour seen in $e^{+} e^{-}$, DIS (ep), hadron-hadron coll.

## Soft Confinement

So, the ratios of particle flows between jets (intERjet radiophysics), as well as the shape of the inclusive energy spectra of secondary particles (intRAjet cascades) turn out to be formally calculable (CIS) quantities. Moreover, these perturbative QCD predictions actually work.

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We should rather feel puzzled than satisfied.

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Both Inter-Jet and Intra-Jet phenomena fully reveal colour coherence in QCD parton multiplication. Their solid imprint upon the angular and energy spectra of relatively soft hadrons are sending us a powerful message ( - a free lunch that we have not found enzymes yet to devour)

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For the time being, we are exploiting this gift: hadron flow practitioners developing smart tools for triggering on new physics, colour glass brewers, small-x BFKL lovers, - no-one would hesitate to put gluons and hadrons into (more or less) one-to-one correspondence.
There is nothing wrong with this. In so doing we simply follow the opportunists' motto "ain't broken - don't fix it".

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- what is it,
- what do we know about it,
- and, more importantly, what we don't


## BRIGHT IDEA



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Explore collisions with, and of, nuclei to study non-perturbative - large - colour fields

## EXTRAS

We spoke about the Collinear enhancement in $1 \rightarrow 2$ parton splittings.

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 characteristic for small-energy vector fields (photons, gluons), $z \ll 1$.
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Ain't any "catastrophe" but a simple consequence of the fact that any charged particle is always surrounded by a long-range Coulomb field which gets shaken off when the charge is accelerated.
As a result,

$$
w_{A} \sim C_{A} \frac{\alpha_{s}}{\pi} \ln ^{2} Q^{2} . \quad[\text { parton multiplicities, form factors, etc. }]
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An important remark :
soft gluon radiation has a classical nature (celebrated F.Low theorem).

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## An important remark :

soft gluon radiation has a classical nature.
This statement has rather dramatic consequences which still remain to be properly digested by the theoretical community ...


[^0]:    "time derivative"

