Theory @ HP2013

Sti CS, November 8th, 2013



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Meta-Summary

HP 2013 : a great week of



NUCLEAR PHYSICS

with sometimes a few bits of



UNCLEAR PHYSICS

But there were exciting moments that I will try to share with you

See also the talks by X-N. Wang and R. Vogt



• There are talks I could not attend



- There are talks I could not attend
- · There are talks I know I did not understand



- There are talks I could not attend
- There are talks I know I did not understand
- There are talks I think I understood, but probably did not





Old joke : A postdoc explains at length to a senior physicist the intricacies of a problem he is trying to solve. After listening for 30 minutes without saying a word, the senior physicist asks :

- Do you have a Hamiltonian?
- Well.. Yes I do.
- So, what is your problem exactly?





















Goal : understand the microscopic dynamics of QCD from whatever we can measure in the final state of heavy ion collisions

- Unfortunately, the outcome of a heavy ion collision also depends on a number of other rather mundane facts :
- i. Nuclei are approximately spherical
- ii. Their diameter is about 12 fermis
- iii. They contain $A \approx 200$ nucleons
- iv. The positions of these nucleons fluctuate event-by-event
 - These properties have all an incidence on some observables
 - None of them is interesting from the point of view of QCD
 - We need observables that are independent of these trivial aspects of nuclear physics, or we need good models for them

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 - None of them is interesting from the point of view of QCD
 - We need observables that are independent of these trivial aspects of nuclear physics, or we need good models for them
- The nucleons may not be as simple as hard discs (they may have "hotspots" that fluctuate themselves)

N_{part} is model dependent...



- May affect critically how we interpret "central" pA collisions...
- Simple remedy : show only "measured" quantities as much as possible (drawback : one looses a variable that gave us some intuition over the geometry of the collision in AA)

Defining centrality classes in pA collisions is a hard business

- Loose correlation between multiplicity and impact parameter
- Centrality classes much more "definition dependent" than in AA

Toy calculation in a CGC model [Borghini et al., 2006] :



Defining centrality classes in pA collisions is a hard business

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Theory talks by topic





Outline



1 Initial sate

- **2** Photons and dileptons
- **3** Jet Quenching
- **4** Heavy flavors and quarkonia

Initial State

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Many models...

Optical Glauber, MC Glauber, AMPT, NEXUS, MC-KLN, MC-rcBK, IP-GLasma

(ordered by the amount of QCD they contain...)



How to constrain them ?

- They differ in the spatial scales at which they have fluctuations
- · Look at event-by-event flow fluctuations :

initial shape harmonics : $\varepsilon_n \quad \rightarrow \quad \text{flow harmonics}: \nu_n$

- Requires a reliable hydro evolution
- Depends on the viscosity



DGLAP based studies

EKRT strikes back... [R. Paatelainen]

- Superposition of pp collisions + Minijet cross-section to NLO
- "Final state" saturation introduced via an infrared cutoff

Impact parameter dependent nPDFs [I. Helenius]

- Include some nuclear modifications in standard PDFs
- Inconsistent if multiple scatterings are important

- Based on EPS09
- Study the b-dependence of the nuclear modifications
- Compute π^0 and γ production in pA collisions







For rare processes (electroweak interactions, high P_⊥, large mass,...), standard pQCD (with nuclear PDFs) is sufficient BUT: LO is generally very crude, and serious things start at NLO



- For rare processes (electroweak interactions, high P_⊥, large mass,...), standard pQCD (with nuclear PDFs) is sufficient BUT: LO is generally very crude, and serious things start at NLO
- For the bulk of parton production, saturation effects become important ⇒ Color Glass Condensate

Color Glass Condensate

$$\begin{split} \mathcal{L} &= -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + A_{\mu} \cdot (J_{1}^{\mu} + J_{2}^{\mu}) \\ W_{1,2}[J] \qquad (\text{distribution of the currents } J_{1,2}) \\ \frac{\partial W}{\partial Y} &= \mathcal{H} W \qquad (\text{JIMWLK equation : energy dependence}) \end{split}$$



State of the art \sim 2012 :

- Evolution at Leading Log BK approximation used in practice BK approximation known up to NLO
- Calculations for AA : LO : classical field approximation Energy density, gluon spectrum Factorization for inclusive observables
- Calculations for pA : Particle spectra 2-particle correlations

Limitations / Shortcomings \sim 2012

In AA collisions, describes only the early stages



- Negligible longitudinal pressure at LO : $P_L/P_T \approx 0$ But : large NLO corrections expected due to the Weibel instability
- The Leading Log evolution has no running coupling : too fast

Numerical solution of JIMWLK [T. Lappi]

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JIMWLK \equiv diffusion equation

$$\frac{\partial W[U]}{\partial Y} = \int_{u,v} \frac{\delta}{\delta U_{u}} \eta_{uv} \frac{\delta}{\delta U_{v}} W[U]$$

Y = time, U_u = "spatial" coordinate

- Can be remapped into a random walk described by a Langevin equation ("straightforward" to solve numerically)
- Prescription to include running coupling effects : modify the noise correlation function

$$\left\langle \xi_{\mathbf{u}}\xi_{\boldsymbol{\nu}}\right\rangle \sim \alpha_{s}\delta(\mathbf{u}-\boldsymbol{\nu}) = \alpha_{s}\int \frac{d^{2}\mathbf{k}}{(2\pi)^{2}}e^{i\mathbf{k}\cdot(\mathbf{u}-\boldsymbol{\nu})} \rightarrow \int \frac{d^{2}\mathbf{k}}{(2\pi)^{2}} \,\,\alpha_{s}(\mathbf{k})\,\,e^{i\mathbf{k}\cdot(\mathbf{u}-\boldsymbol{\nu})}$$

- Note 1 : Next to Leading Log JIMWLK equation now derived [A. Kovner, M. Lublinsky], [S. Caron-Huot]
- Note 2 : Some kinematical improvements to the LO can account for a good part of NLO (shown in the case of BK by G. Beuf)

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2-gluon correlations in pA collisions

Rapidity evolution for the 2-gluon spectrum [E. lancu]

- Ridge calculation : inclusive 2-gluon spectrum for a wide separation in rapidity
- The standard JIMWLK evolution is fully inclusive : it integrates over virtual and real contributions for all the gluons in the rapidity evolution
- Idea : "tag" some gluons in the course of the evolution, that should be produced in the final state
- Expressible as a Langevin process But : computational cost scales as $\sim S_{\perp} \times S_{\perp}$

Initial state mechanisms for near-side correlations [A. Kovner]

- Without invoking any flow, there are several mechanisms by which one gets ridge correlations in pp and pA collisions
- The large N_c limit is tricky in a dense medium [M. Lublinsky]

J/Ψ production in eA collisions [A. Ramnath] [G. Jackson]





- Probe of the nuclear gluon distribution and its spatial distribution
- Controlled by a 4-point correlator, but mixes with a 6-point function in the rapidity evolution

Gaussian truncation

$$\left\langle \cdots \right\rangle_{\mathbf{y}} = \exp\left\{-\frac{1}{2}\int^{\mathbf{y}} d\mathbf{y} \int_{\mathbf{u},\mathbf{v}} G_{\mathbf{y},\mathbf{u}\mathbf{v}} \nabla_{\mathbf{u}} \nabla_{\mathbf{v}} \right\} \cdots$$

• Gives closed expressions for the n + 2-point function in the evolution equation for a n-point function

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CGC application to pA collisions

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Hybrid formalism : DGLAP + k_T-factorization [B. Xiao]

- · Use standard collinear factorization for the proton
- k_T-factorization + BK for the nucleus
- Factorization established up to Leading Log

k_T-factorization + BK evolution [H. Mantysaari]



- Constrain the source model on *ep* collisions in DIS
- Compute π^0 spectrum for pp and pA collisions
- Evolution done with the running coupling BK equation
- Assume k_T-factorization (OK for pp and pA collisions)
Pressure isotropization in AA collisions [T. Epelbaum]



- NLO included via fluctuations of the initial classical fields
- Spectrum of fluctuations calculated analytically at $Q_s \tau_0 \ll 1$
- 3+1 dim classical Yang-Mills simulation at $\tau > \tau_0$

Results

- Rapid increase of $P_{\rm I}/P_{\rm T}$
- Works at rather small couplings
- Small effective $\eta/s \leq 1$



Early flow from classical fields [R. Fries]

- When $\tau \rightarrow 0$, the Poynting vector is exactly zero (E, B are longitudinal)
- At small but non-zero τ , $T^{0i} \neq 0$:
 - rapidity even component ~ $\tau \partial^i \varepsilon$
 - rapidity odd component ~ $\tau \varepsilon^{ij} \left([D^j, B_z] E_z [D^j, E_z] B_z \right)$





Gauge-gravity duality

- Most QCD tools (except lattice) do not work at strong coupling
- Quantum Field Theory Gravity duality :



- On firm grounds for $\mathcal{N} = 4$ SUSY Yang-Mills theory
- Bulk calculation "simple" only in the limit $q^2 N_c \rightarrow \infty$

Shockwave collision in AdS/CFT [J. Casalderey-Solana]





• Two shockwaves with a Gaussian profile of width ω (mimics Lorentz contraction in a collision at $\sqrt{s} \sim \omega^{-1}$)

- Low energy, large width : strong stopping and Landau-like behavior
- High energy, narrow width : weak stopping, Bjorken-like



Photons and Dileptons

Photons and dileptons





- Thermal rates $\sim T^4$
- Sensitive to the early temperature

Photons and dileptons

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- Thermal rates ~ T⁴
- Sensitive to the early temperature
- But many other sources make the signal extraction difficult

Thermal photons potentially visible at low p_T They escape the medium without further interaction



Photon spectrum calculations



• Rate from kinetic approach :

$$\omega \frac{dN_{\gamma}}{dt dV d^{3} \vec{q}} \propto \int_{\binom{\text{unobserved}}{\text{particles}}} \left| \begin{array}{c} \omega \\ f(\omega_{1}) \cdots f(\omega_{n}) \times \\ (1 \pm f(\omega_{1}')) \cdots (1 \pm f(\omega_{p}')) \end{array} \right|^{2}$$

• Rate from QCD at finite temperature :

$$\omega \frac{dN_{\gamma}}{dt dV d^{3}\vec{q}} \propto \frac{1}{e^{\omega/T} - 1} \text{ Im } \underbrace{\prod^{\mu}_{\mu}(\omega, \vec{q})}_{\text{photon self-energy}}$$

Physics of photon/dilepton production



(the possibly singular t-exchange gives only a gentle log)



Physics of photon/dilepton production





Physics of photon/dilepton production





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2000 : LPM effect is important





- 2001 : full LO photon rate
- 2002 : LPM resummation for low mass dileptons

Dilepton rate at NLO [M. Laine]





- Dilepton rate at NLO (i.e. Im∏ at two loops), for invariant masses that are not too small
- NLO/LO becomes large for M/T <> 1 (new channels that open up at NLO?)
- Reasonable agreement of the imaginary time correlator with lattice calculations



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Stellenbosch, November 2013

Real photon rate at NLO [J. Ghiglieri]





- O(q) correction relative to the LO result
- LO+NLO remarkably close to LO (mostly accidental)
- Lots of goodies in terms of new tricks to perform these calculations
- Work in progress : extend to NLO the AMY model of energy loss



Digression on the collision kernel $\mathbb{C}(q_{\perp})$ (I)





Plays a role in :

- Photon/dilepton rates (LPM resummation)
 - In-medium broadening : $\Delta k_{\perp}^2 \text{ per collision} = \int \frac{d^2 q_{\perp}}{(2\pi)^2} q_{\perp}^2 \ \mathfrak{C}(q_{\perp})$
- Expression in terms of in-medium gluon spectral functions :

$$\mathfrak{C}(\mathbf{q}_{\perp}) = \int \frac{\mathrm{d}q_{0}\mathrm{d}q_{z}}{(2\pi)^{2}} \, 2\pi\delta(q_{0} - q_{z}) \, \widehat{\nu}_{\mu}\widehat{\nu}_{\nu} \, \left(\rho_{L}^{\mu\nu}(Q) + \rho_{T}^{\mu\nu}(Q)\right)$$

• Fourier transform given by a correlator of light-like Wilson lines :

$$e^{-\ell \mathcal{C}(\mathbf{r}_{\perp})} = \frac{1}{N_c} \operatorname{Tr} \left(U(\mathbf{0}_{\perp}) U^{\dagger}(\mathbf{r}_{\perp}) \right)$$

2002 : Leading Order

$$\label{eq:constraint} \mathfrak{C}(q_{\perp}) = \frac{1}{q_{\perp}^2} - \frac{1}{q_{\perp}^2 + m_D^2}$$

2009 : NLO [S. Caron-Huot]

2002 : Leading Order

$$\mathfrak{C}(\mathfrak{q}_{\perp}) = \frac{1}{\mathfrak{q}_{\perp}^2} - \frac{1}{\mathfrak{q}_{\perp}^2 + \mathfrak{m}_{L}^2}$$

2009 : NLO [S. Caron-Huot]

Lattice evaluation [M. Panero]



- Dimensional reduction : 3-dim Yang-Mills theory + adjoint A_0
- Parameter matching to • reproduce the QCD soft sector
- $\hat{q} \sim 6 \text{ GeV}^2/\text{fm}$ at RHIC temperatures

Modification to include magnetic screening [M. Djordjevic] $\frac{1}{q_{\perp}^2} - \frac{1}{q_{\perp}^2 + m_{\scriptscriptstyle D}^2} \quad \rightarrow \quad \frac{1}{q_{\perp}^2 + m_{\scriptscriptstyle M}^2} - \frac{1}{q_{\perp}^2 + m_{\scriptscriptstyle D}^2}$

- m_{M} = magnetic screening mass ~ q^2T (non perturbative)
- · Seems to help with the energy loss of heavy quarks

NO KELLEROOD

Modification to include magnetic screening [M. Djordjevic] $\frac{1}{q_{\perp}^2} - \frac{1}{q_{\perp}^2 + m_p^2} \quad \rightarrow \quad \frac{1}{q_{\perp}^2 + m_M^2} - \frac{1}{q_{\perp}^2 + m_p^2}$

- m_{M} = magnetic screening mass ~ q^2T (non perturbative)
- Seems to help with the energy loss of heavy quarks
- Warning : when one starts playing with the g²T scale, things may become really horrible ...

because one is considering interactions whose range is as large as the soft mean free path

Folding into hydrodynamics [U. Heinz] [C. Shen] [G. Vujanovic]



- Main steps :
 - compute the rate with the T of the fluid cell
 - · boost the local rate by the fluid velocity
 - integrate the rate over space and time
- T extracted by a fit $\sim exp(-p_{\perp}/T)$ IS NOT the QGP temperature
- Interplay with viscous hydrodynamics : non zero $\pi^{\mu\nu} \Leftrightarrow f \neq f_{equi}$ The rates must be calculated with non-equilibrium distributions consistent with the shear tensor. Done for $2 \rightarrow 2$ processes, in progress for the LPM resummation (to have the full LO rate)

Some sensitivity of the photon v_2 to the viscous relaxation time

Persistent disagreements with data :

• Yield too small, ν_2 too small (by a large factor \sim 4)

Seems to suggest that photon production may be underestimated in the later stages of the fireball evolution (where flow is most developed) [W. Cassing] : hadron gas model that improves on this

Jet Quenching

The big picture [C. Salgado]





Beyond BDMPS

Basic facts for a single emission

Soft and collinear divergences $dP \sim \alpha_s C_R \frac{dx}{x} \frac{d^2 k_\perp}{k_\perp^2}$

BDMPS-Z theory

- Momentum broadening : $k_{\perp}^2 \sim \widehat{q} \, t_f$
- Formation time : $t_f \sim \frac{\omega}{k_\perp^2} \quad \Rightarrow \quad t_f \sim \sqrt{\frac{\omega}{\widehat{q}}}$
- t_f must be less than L. No emission if : $\omega > \omega_c = \widehat{q} L^2$
- Emission angle : $\theta \sim \frac{k_{\perp}}{\omega} \sim \left(\frac{\widehat{q}}{\omega^3}\right)^{1/4}$
- Mean energy lost in a single emission : $\langle \omega \rangle \sim \alpha_s \omega_c \sim \alpha_s \widehat{q} L^2$ Dominated by ω close to the upper limit ω_c . The energy stays in a small cone : does not explain dijet asymmetries Soft gluons are emitted at large angle, but many emissions are needed to lose a lot of energy



Coherence effects in multiple emissions [C. Salgado]

Vacuum antenna effects

- Gluons emitted at large angle have a large transverse wavelength $\lambda_{\perp} \sim \frac{1}{\theta_{ex}}$
- The emitting system has a size $r_{\perp} \sim \Theta t_f \sim \frac{\Theta}{\theta^2 \, \omega}$
- In-cone $(\theta < \Theta) \ : \ \lambda_\perp < r_\perp \ :$ independent emission by each quark
- Out-of-cone $(\theta > \Theta)$: $\lambda_{\perp} > r_{\perp}$: coherent emission by $q + \bar{q}$ system



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What happens in medium?

- The above geometric argument remains valid
- If the color field of the medium varies over r⊥, then the q and the q lose their color coherence

Probabilistic description [E. lancu] [Y. Mehtar-Tani]

- Decoherence time : $t_{decoh} \sim \frac{1}{(\widehat{a} \theta^2)^{1/3}}$ Comparable to the formation time
- Soft emissions out-of-cone are not suppressed
- Emissions separated by $\Delta t \gg t_f$ are incoherent \Rightarrow probabilistic

Democratic branchings

- Vacuum : $dP \sim \alpha_s \frac{dx}{x}$ In medium : $dP \sim \alpha_s \frac{dx}{x} \sqrt{\frac{\omega_c}{x \omega_{parent}}}$
- Probability ~ 1 regardless of x if $\omega_{\text{parent}} \sim \alpha_s^2 \omega_c$
- Out of cone, the energy is rapidly degraded into many soft gluons that carry $\omega \sim T$





Anomalous L-dependence of the energy loss [Y. Mehtar-Tani]

- Gluon emissions contribute to the accumulated k₁ of the emitter
- Effectively, as if q was larger
- Effect suppressed by α_s but enhanced by double logs
- If resummed, modifies the power of L in $\langle \omega \rangle$

$$\left<\omega\right>\sim\alpha_{s}\widehat{q}_{0}\,L^{2}\left(\frac{\widehat{q}_{0}L}{m_{_{\rm D}}^{2}}\right)^{\sqrt{4\alpha_{s}N_{\rm c}/\pi}}$$

Between the plain BDMPS result and strong coupling results

• BDMPS : L^2

Various technical improvements

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Mass effect on the decohence of a Qg dipole [M. Calvo]

- The mass of the heavy quark enhances the decoherence
- Effect more pronounced for Qg than $Q\overline{Q}$
- Implies a larger energy loss (still needs to be quantified)



Energy loss and AdS/CFT

Test of generic E-loss models with jet tomography [B. Betz]

- Assume : $\frac{dE}{dz} = -\kappa E^{a} z^{b} T^{2-a+b}$
 - b = 1 : radiative
 - b = 0 : elastic
 - b = 2 : AdS/CFT
- Embedded in viscous hydro (VISH2+1 or Romatschke-Luzum)
- b = 1 seems to fit best the data both at RHIC and LHC (standard AdS/CFT has too strong quenching)

AdS/CFT still alive... [A. Ficnar]

- Use finite endpoint momentum strings ("more realistic description of an energetic guark")
- Result that interpolates from collisional (b = 0) to "old AdS" (b = 2) behavior

Hybrid weak/strong coupling approach [D. Pablos]

The devil is in the details...

Other things that matter in practice

Influence of the details of the bulk evolution [D. Molnar]

- R_{AA} not very sensitive to the details, v_2 much more sensitive
- Using a Lorentz covariant formulation is probably a good idea...

Trigger biases [T. Renk]

- By triggering on certain conditions, one may bias the event sample in several ways :
 - Kinematics
 - Geometry (location of the hard scattering)
 - Chemistry (flavor of the original parton)
 - Details of the shower mechanism
- Good news : use this to one's advantage to select specially interesting situations
- Bad news : much more work when comparing with data

Real-world implementations

CUJET (rcDGLV + 2+1-dim hydrp) [J. Xu]

Jets embedded in hydro expansion [Y. Tachibana] [R. Andrade]

Collisional energy loss via Boltzmann transport [J. Tan] [Y. Zhu]

- Leading parton = small perturbation $\delta f(p)$ of the distribution
- Linearized Boltzmann equation for $\delta f(p)$

Medium cascade with partial decoherence [K. Tyvoniuk]

Based on ideas in [C. Salgado], [E. lancu], [Y. Mehtar-Tani]

JEWEL [K. Zapp]

- Medium seen by the jet is a collection of quasi-free partons
- · Matrix elements (non-eikonal kinematics) + parton shower
- LPM effect

Heavy flavors and and Quarkonia


Heavy quark energy loss

Recent history :

- Dead cone effect : no emission in a cone that grows with the quark mass $\theta_{excluded}=M/E$

Naively, one thus expected less energy loss for heavy quarks

- Data showed that they are almost as suppressed as light partons
- Triggered a lot of interest for strong coupling approaches
- Revived interest in collisional energy loss, that turned out to be important

Ingredient list

- · Initial momentum distribution for the heavy quarks
- Parton energy loss (collisional and radiative)
- Fragmentation functions (assumed to take place in vacuum)
- Decay of D and B mesons

Collisions

- Non-static scattering centers
- Finite size medium
- Magnetic screening
- Running coupling



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Collisions

- Non-static scattering centers
- Finite size medium
- Magnetic screening
- Running coupling



A bit frustrating

- · Not easy to pinpoint what caused the improvement
- · Seems like an addition of several little changes

Parton transport – BAMPS [C. Greiner] [J. Uphoff]

- Parton cascade with $2 \rightarrow 2, 2 \rightarrow 3$ and $3 \rightarrow 2$ processes
- LPM effect : interference effect \Rightarrow not included in transport models. Can be modeled by vetoing rescatterings during formation time of the emitted gluon
- Improvement over the Gunion-Bertsch approximations for the inelastic cross-sections (used in previous versions)
- Faster thermalization
- Reasonable R_A
- Tension between R_{AA} and v_2 for heavy guarks





running α_{c} , $\kappa=1$, X=1 running α_s, κ=0.2, X=0.2

running α_e , $\kappa=0.2$, only $2\rightarrow 2$, K=3.5 0-7.5% (ALICE)

1.4

1.2

More transport or transport-like ideas



MC@sHQ + EPOS [M. Nahrgang] [P.B. Gossiaux]

- Born cross-sections, with HTL effects + K-factor
- Running α_s
- Boltzmann transport
- EPOS background



Langevin + radiative energy loss [S. Cao]

Modified Langevin equation to include radiative energy loss :

$$\frac{d\mathbf{p}}{dt} = -\eta_{\rm D}\,\mathbf{p} + \boldsymbol{\xi} + \mathbf{f}_{g}$$

Langevin + viscous hydro [M. Nardi]

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AdS/CFT [M. Lekaveckas]



- Heavy guark = endpoint on the boundary of a string that dives into the bulk
- Drag force in a static plasma :

$$\frac{d\vec{\mathbf{p}}}{dt} = \frac{\sqrt{\lambda}}{2\pi} (\pi T)^2 \frac{\beta}{\sqrt{1-\beta^2}}$$

This work : drag force in a plasma with anisotropic $T^{\mu\nu}$



- Drag force slightly different from what one would get from the transverse or longitudinal components alone
- But comparable in magnitude
- Delay time for the drag to establish, proportional to the boost factor of the quark

Quarkonia Suppression



· When the Debye screening radius becomes smaller than the bound state radius, expect suppression



- When the Debye screening radius becomes smaller than the bound state radius, expect suppression
- However, if many $Q\overline{Q}$ pairs are produced, they may recombine (at LHC ~ 100 $c\overline{c}$ pairs in central collisions)
- For $J/\psi,$ feed down by decay of higher lying states

Singlet free energy of a static $Q\overline{Q}$ pair





- Very clean successive suppression pattern for $\Upsilon\sp{s}$ s
- No recombination effects
- No feed down from anywhere

Spectral function on the lattice [H.T. Ding]

- On the lattice, calculate G₁ at a discrete set of points $\tau = na_{\star}$
- Invert the spectral integral (ill posed problem without extra constraints...)
- Maximum Entropy Method : input prior knowledge about $\sigma(\omega, \mathbf{p})$ to make the inversion possible
- Additional difficulty : G_r is not very sensitive to changes of σ



Other applications



Heavy quark diffusion constant

$$D \sim \lim_{\omega \to 0} \frac{\sigma(\omega, \mathbf{0})}{\omega}$$

- So far, only quenched QCD
- Same method for electrical conductivity and dilepton rates



Spatial correlators [A. Mocsy]



$$G(z) \equiv \int_0^\beta d\tau \int dx dy \langle J(\tau, x) J(0, 0) \rangle$$

- z not limited by 1/T
- Related to the spectral function :

$$G(z) = \int dz \, e^{ip_z z} \int_0^\infty d\omega \, \frac{\sigma(\omega, (0, 0, p_z))}{\omega}$$



Clear evidence of a change with the temperature

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pNRQCD and potential models

• pNRQCD = effective theory for heavy quarks :

$$\mathcal{L} = \underbrace{-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \overline{q} \not\!D q}_{\text{light quarks and shape}} + \mathbf{S}^{\dagger} \left[i \partial_{t} - \frac{(i \nabla)^{2}}{M} - V_{s}(r) \right] \mathbf{S} + \cdots$$

light quarks and gluons

- $S = singlet Q\overline{Q}$ field
- V_s(r) = potential. Generally complex The real and imaginary parts of V_s are related to peak shift and broadening of the spectral function
- Tree level dynamics for S: Schroedinger equation

$$\left[i\partial_{t} - \frac{(i\boldsymbol{\nabla})^{2}}{M} - V_{s}(r)\right]\boldsymbol{S} = \boldsymbol{0}$$

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Where do we get the potential from ? [P. Petreczky]

- In the past, the singlet free energy F_1 was used as $V_{\rm s}$
- · No imaginary part

Potential from lattice (based on [Rothkopf, 2009])

Spectral representation of Wilson loops

$$W(\tau, \mathbf{r}) = \int d\omega \, \sigma(\omega) \, e^{-\omega\tau}$$

• Re V_s and $\operatorname{Im} V_s$ obtained as peak position and width of $\sigma(\omega)$



Role of the imaginary part [A. Mocsy]





Role of the imaginary part [A. Mocsy]





Most discussed plots

The most "Textbook-Like" plot



The most "Intriguing" plot



The most "Mind-Boggling" plot



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Runner up for the most "Mind-Boggling" plot award



Summary of the Summary

- Progress in many areas since the previous Hard Probes Both in the "hardcore" theory, and in the modeling of the collisions
- Some things are even starting to be fully understandable from a QCD perspective
- Lots of new data that will take a while to digest A lot of confusion related to pA results Not the controlled situation we had imagined...

