

# Introduction to the theory of the QGP and the CGC

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**CEA / DSM / SPhT**

QGP

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Basic features of QCD

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Deconfinement transition

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Physics of the QGP

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QGP signatures

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CGC

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Parton model

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Saturation

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Color Glass Condensate

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CGC signatures

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## ■ Quark Gluon Plasma (QGP)

- ◆ Basic features of QCD
- ◆ Deconfinement phase transition
- ◆ Physics of the quark gluon plasma
- ◆ Signatures of the QGP

## ■ Color Glass Condensate (CGC)

- ◆ Parton model
- ◆ Saturation
- ◆ Color Glass Condensate
- ◆ Signatures of the CGC

**QGP**

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# QGP

# Quarks and gluons

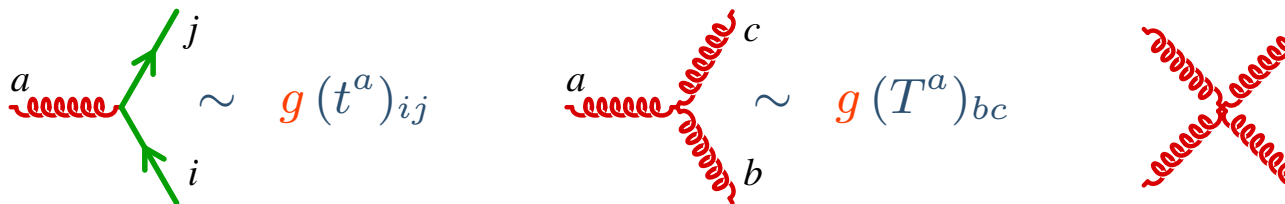
## ■ Electromagnetic interaction : Quantum electrodynamics

- ◆ Matter : **electron** , interaction carrier : **photon**
- ◆ Interaction :

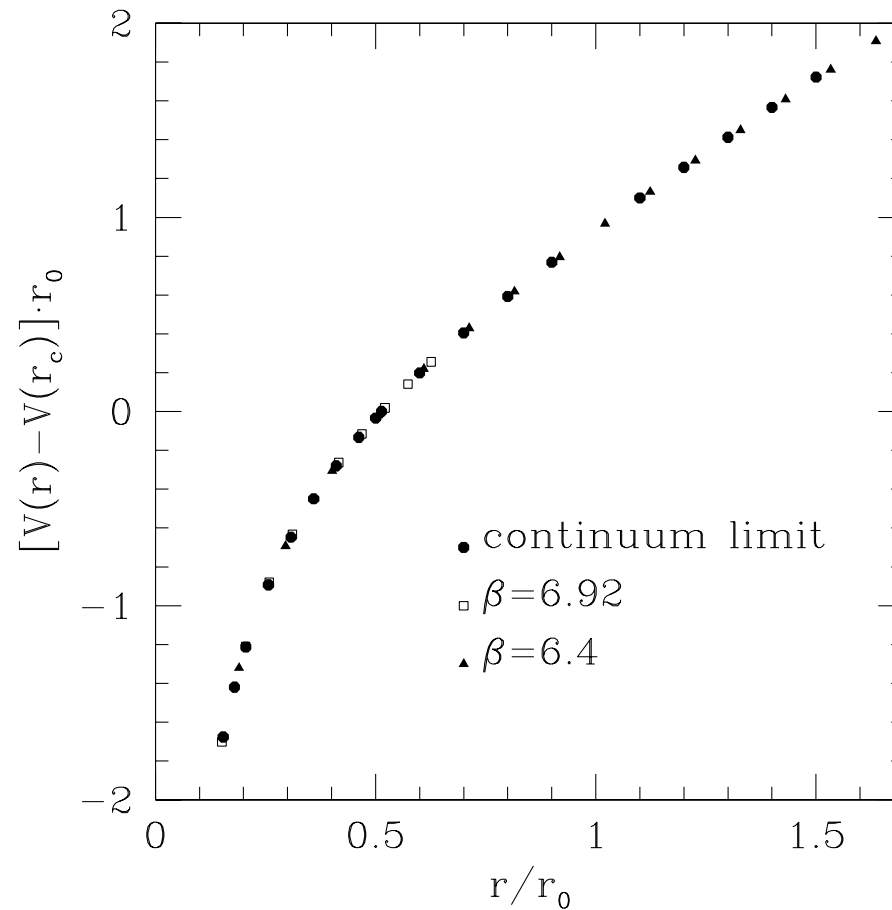


## ■ Strong interaction : Quantum chromodynamics

- ◆ Matter : **quarks** , interaction carriers : **gluons**
- ◆ Interactions :



- ◆  $i, j$  : colors of the quarks (3 possible values)
- ◆  $a, b, c$  : colors of the gluons (8 possible values)
- ◆  $(t^a)_{ij}$  :  $3 \times 3$  matrix ,  $(T^a)_{bc}$  :  $8 \times 8$  matrix

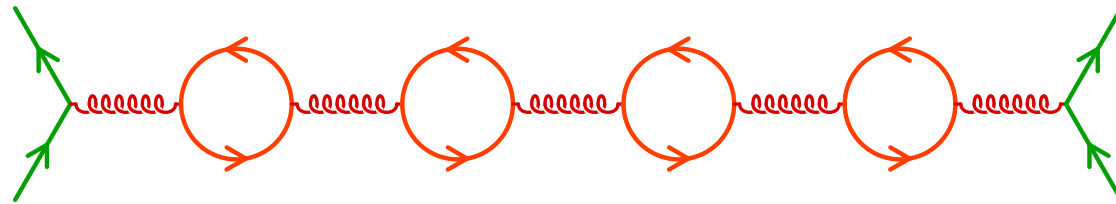


- The quark potential increases linearly with distance
- Quarks are confined into color singlet hadrons

# Asymptotic freedom

- Running coupling :  $\alpha_s = g^2/4\pi$

$$\alpha_s(r) = \frac{2\pi N_c}{(11N_c - 2N_f) \log(1/r\Lambda_{QCD})}$$

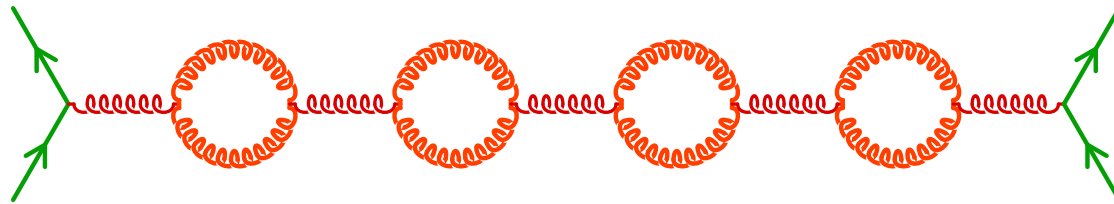


- The effective charge seen at large distance is screened by fermionic fluctuations (as in QED)

# Asymptotic freedom

- Running coupling :  $\alpha_s = g^2/4\pi$

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- The effective charge seen at large distance is screened by fermionic fluctuations (as in QED)
- But gluonic vacuum fluctuations produce an anti-screening (because of the non-abelian nature of their interactions)
- As long as  $N_f < 11N_c/2 = 16.5$ , the gluons win...

# Asymptotic freedom

QGP

Basic features of QCD

● Quarks and gluons

● Confinement

● Asymptotic freedom

Deconfinement transition

Physics of the QGP

QGP signatures

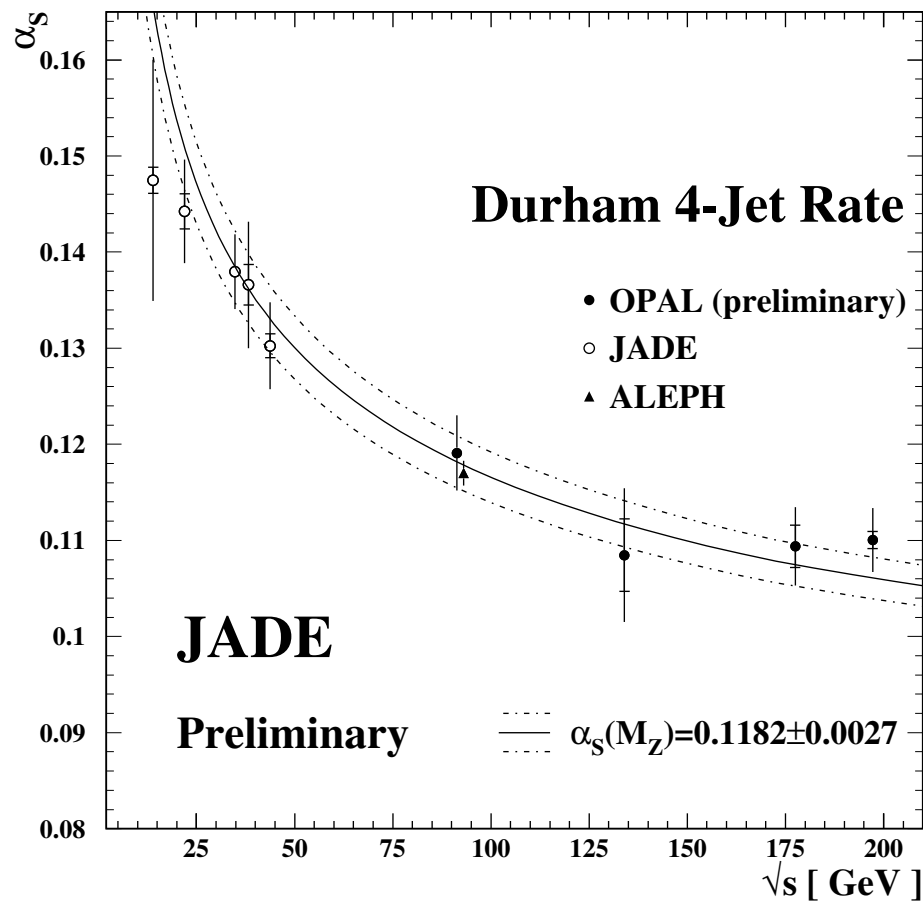
CGC

Parton model

Saturation

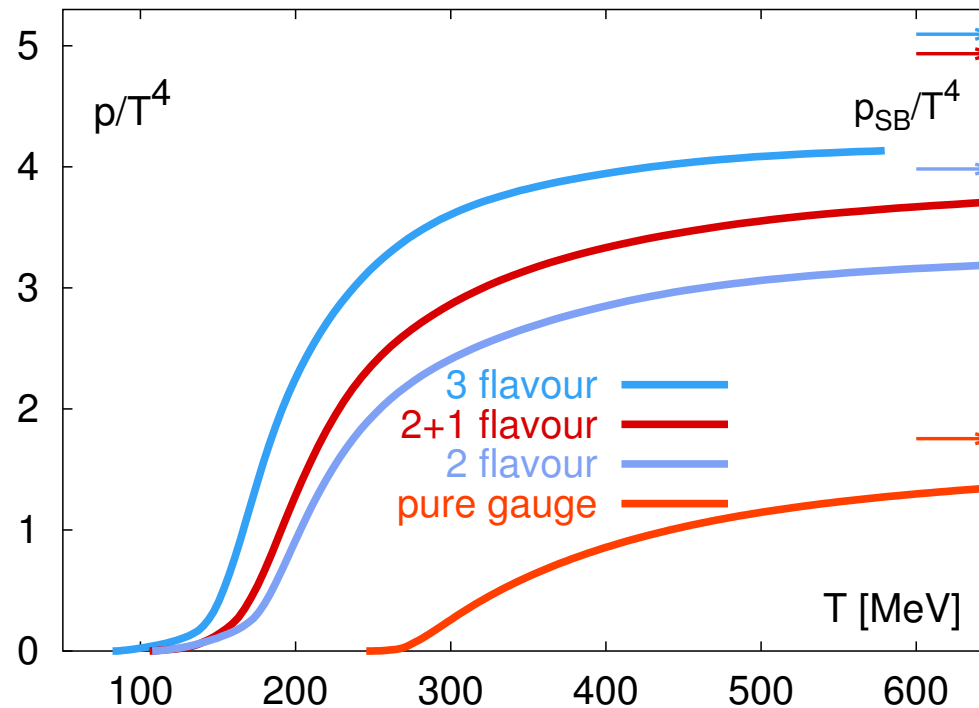
Color Glass Condensate

CGC signatures



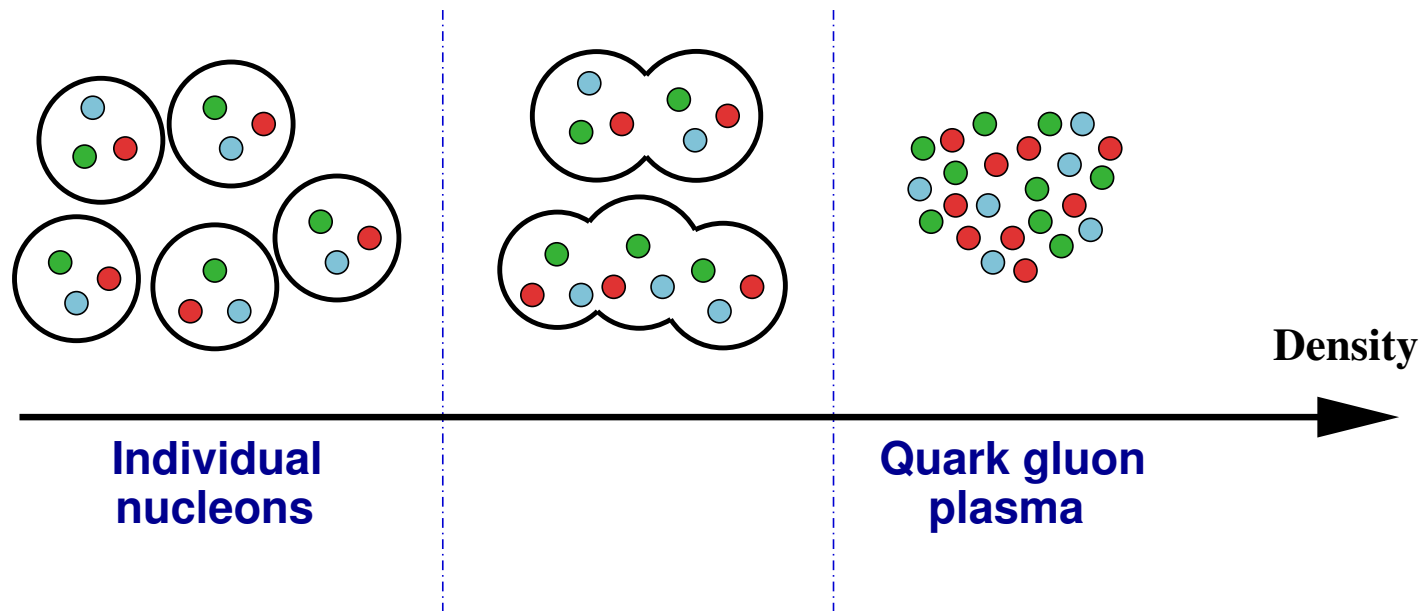
- The coupling constant is small at short distances
- At high density, a hadron gas may undergo deconfinement
  - ▷ quark gluon plasma





- Fast increase of the pressure :
  - ◆ at  $T \sim 270$  MeV, if there are only gluons
  - ◆ at  $T \sim 150\text{--}170$  MeV, depending on the number of light quarks

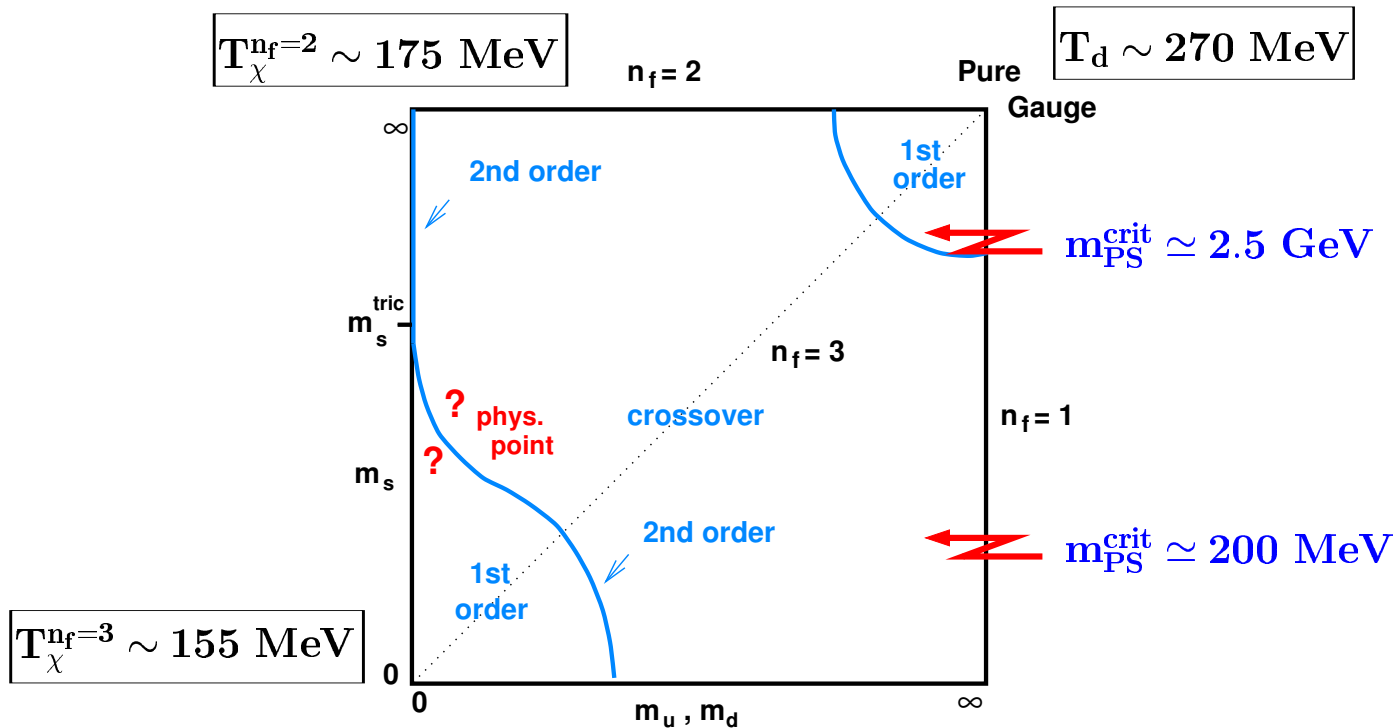
# Deconfinement



- When the nucleon density increases, they merge, enabling quarks and gluons to hop freely from a nucleon to its neighbors
- This phenomenon extends to the whole volume when the phase transition ends
- Note: if the transition is first order, it goes through a mixed phase containing a mixture of nucleons and plasma

- Deconfinement
- QCD phase diagram
- Early universe
- Heavy ion collisions

## 3-flavour phase diagram



# QCD phase diagram

QGP

Basic features of QCD

Deconfinement transition

● Deconfinement

● QCD phase diagram

● Early universe

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Physics of the QGP

QGP signatures

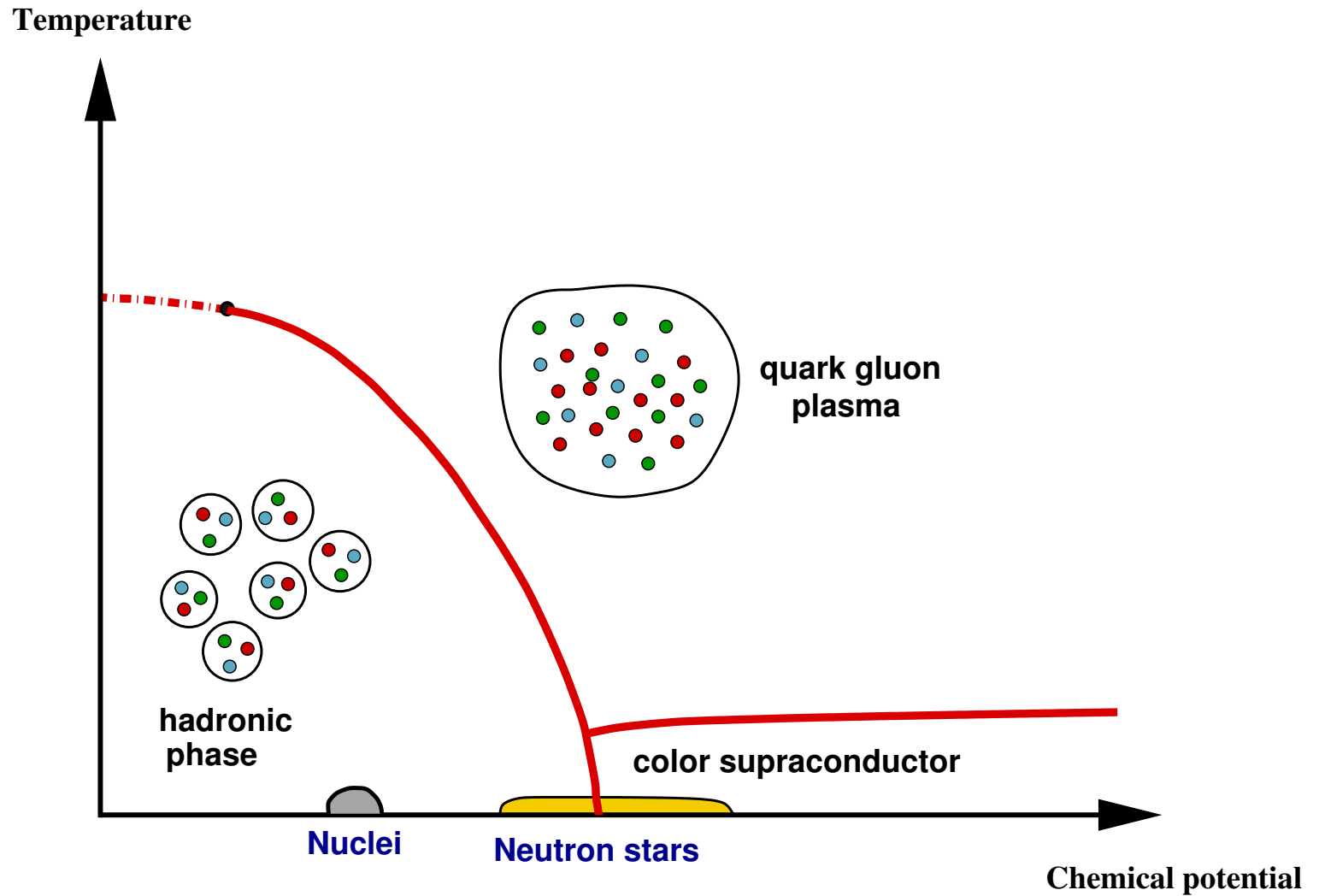
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# The QGP in the early universe

- QGP

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- Basic features of QCD

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- Deconfinement transition
  - Deconfinement
  - QCD phase diagram
  - **Early universe**
  - Heavy ion collisions

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- Physics of the QGP

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- QGP signatures

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- CGC

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- Parton model

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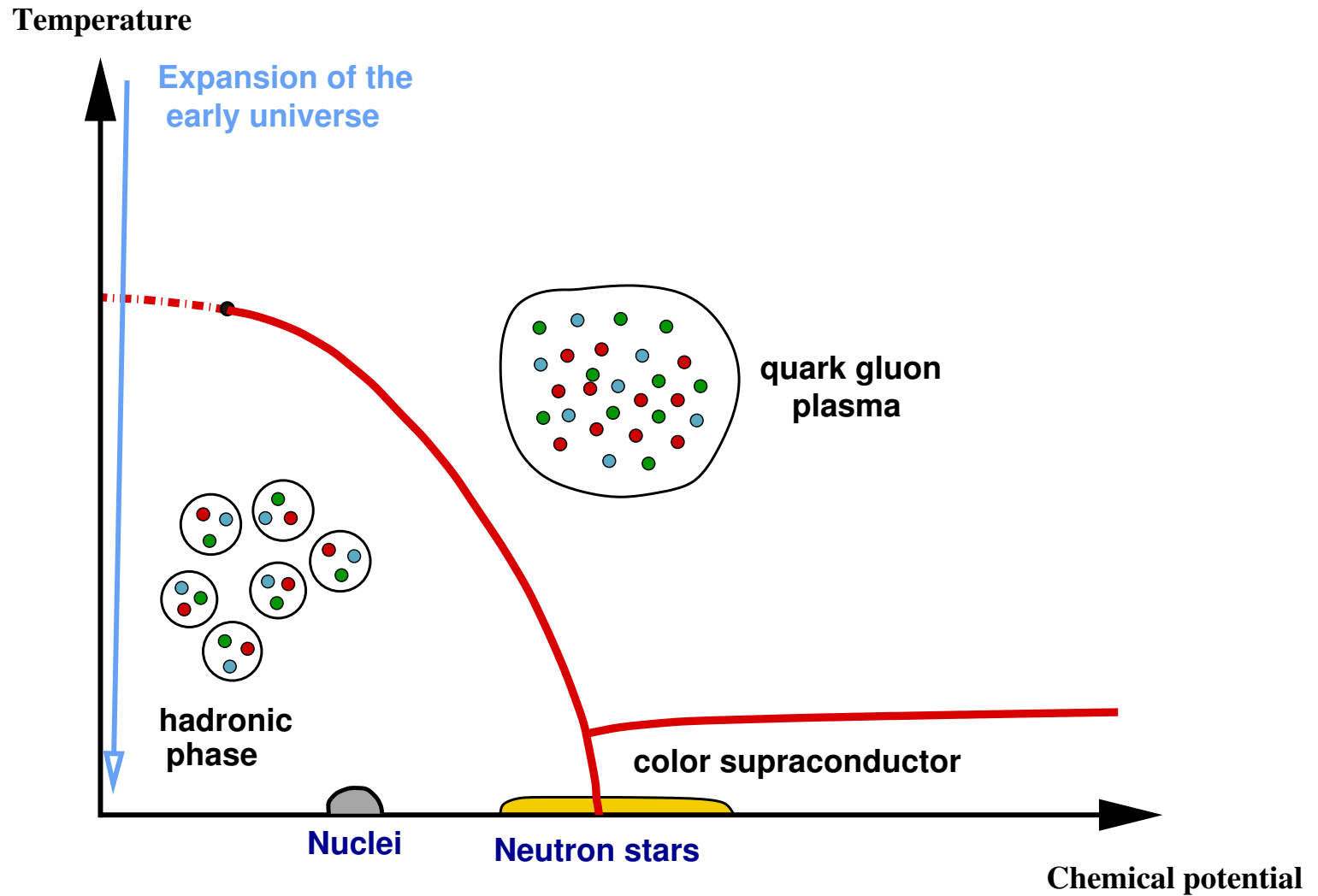
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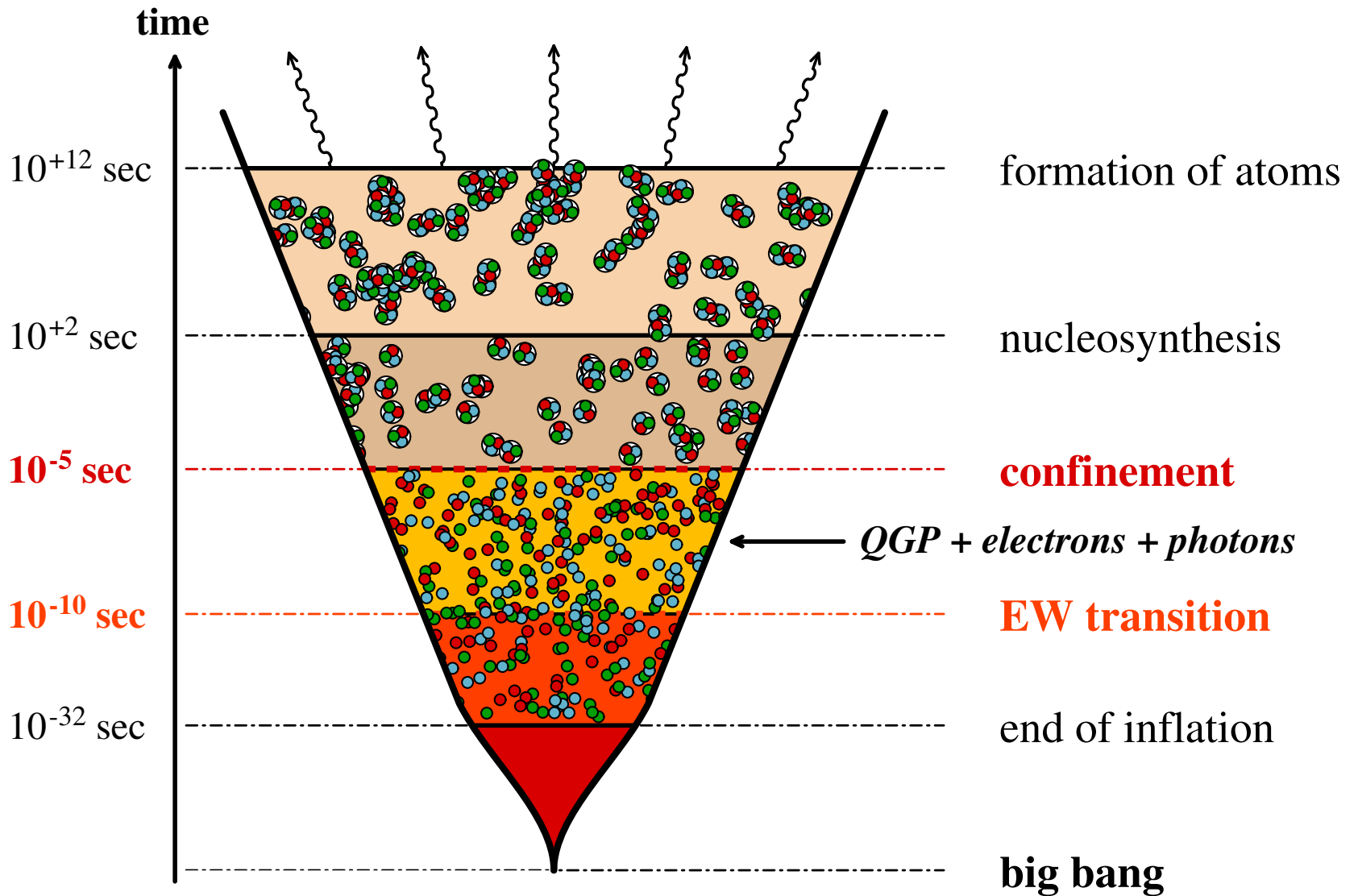
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# Heavy ion collisions

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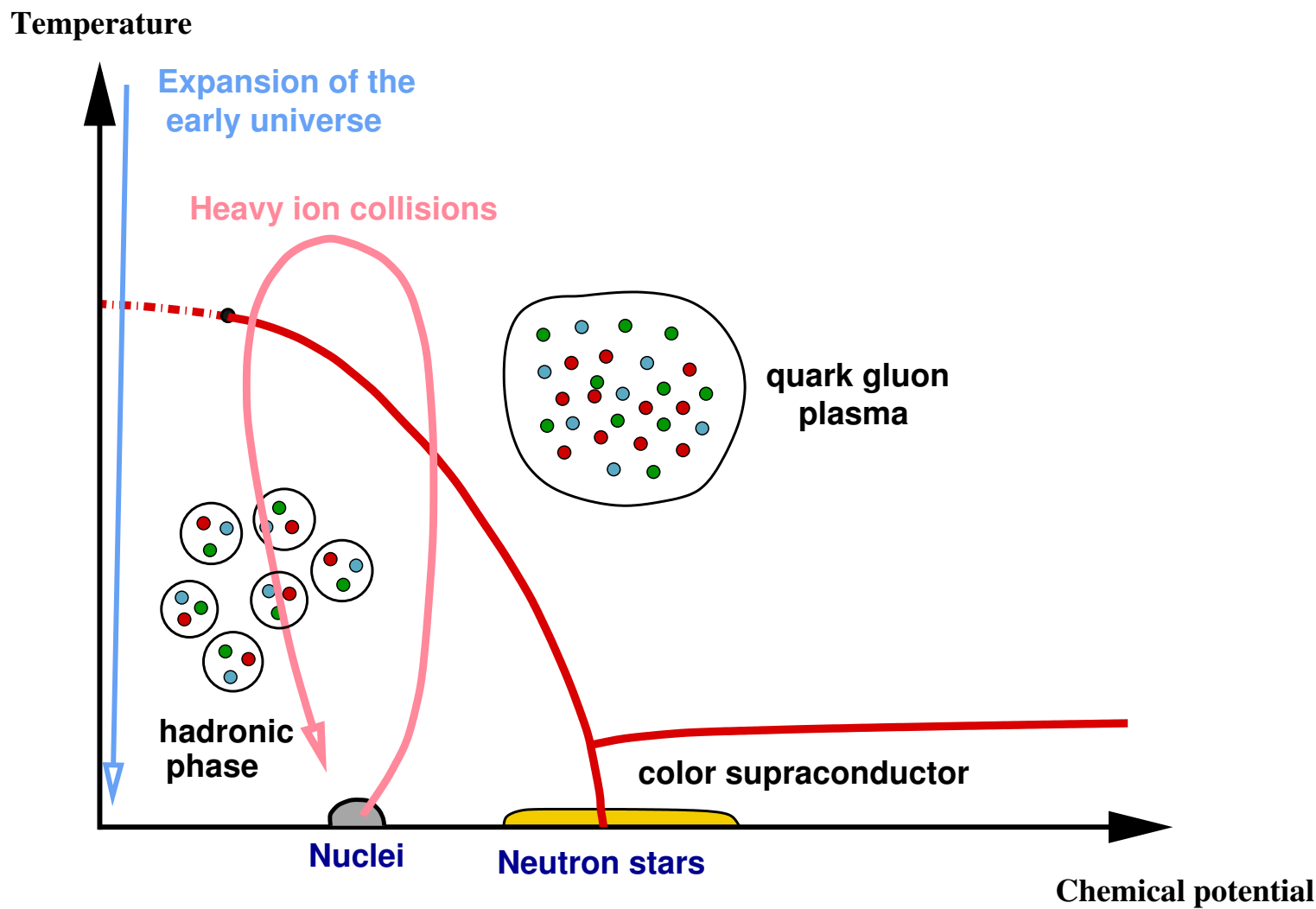
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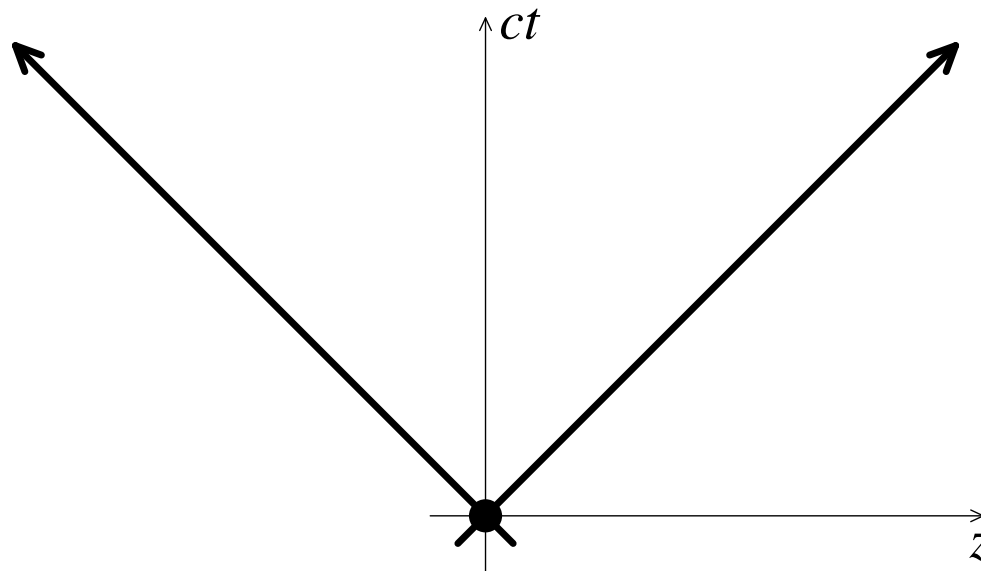
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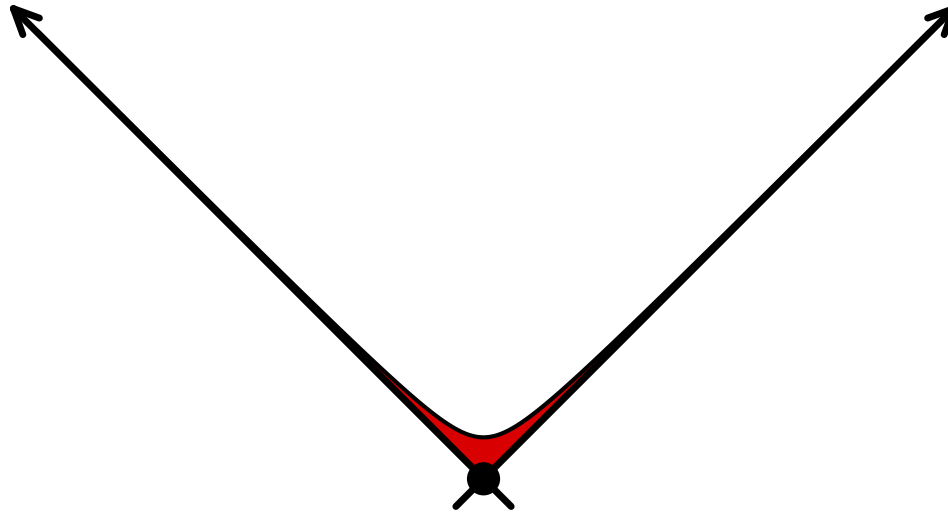


# Heavy ion collisions

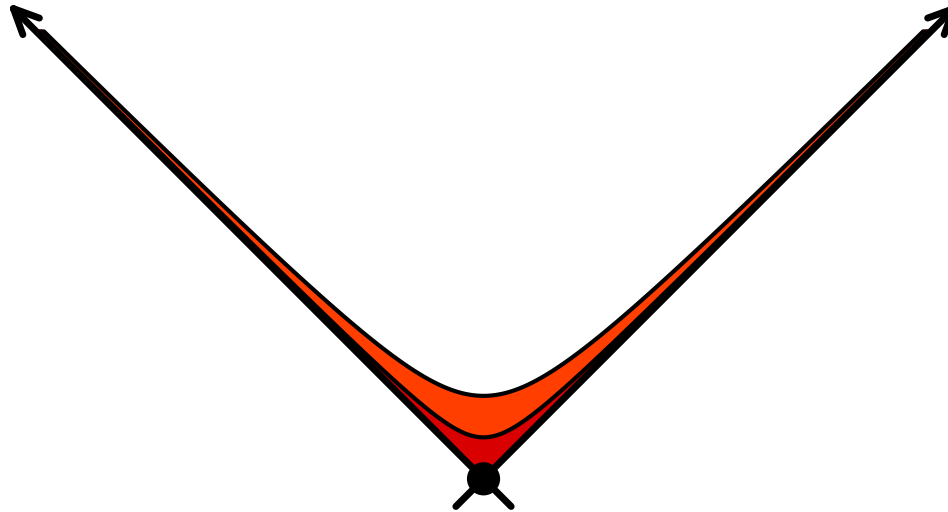


- $\tau \sim 0 \text{ fm}/c$
- Production of hard particles :
  - ◆ jets
  - ◆ heavy quarks
  - ◆ direct photons
- calculable with the tools of perturbative QCD



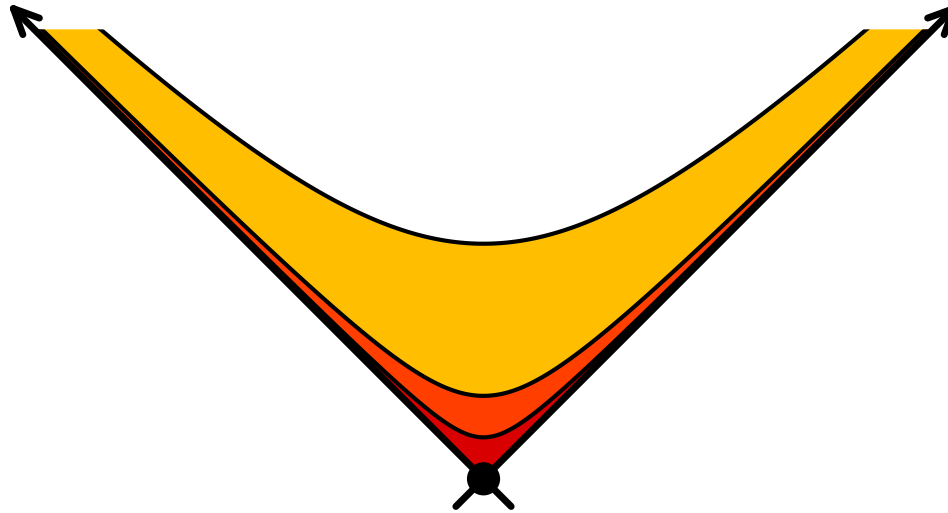


- $\tau \sim 0.2 \text{ fm/c}$
- Production of semi-hard particles :
  - ◆ gluons, light quarks
- relatively small momentum :  $p_{\perp} \lesssim 1\text{--}2 \text{ GeV}$
- make up for most of the multiplicity
- sensitive to the physics of saturation (CGC)



- $\tau \sim 1-2 \text{ fm}/c$
- Thermalization
  - ◆ experiments suggest a fast thermalization
  - ◆ but this is still not understood from QCD

# Heavy ion collisions



- $2 \leq \tau \lesssim 10 \text{ fm}/c$
- Quark gluon plasma

QGP

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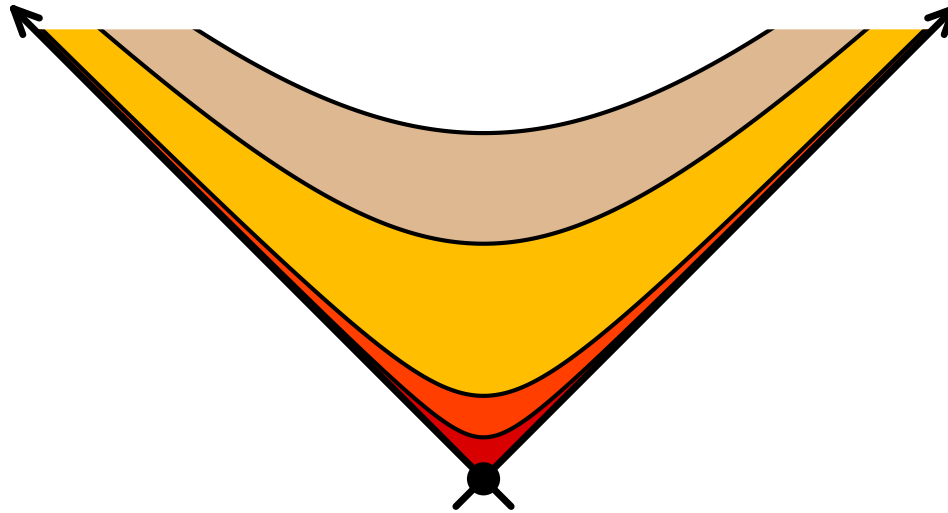
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# Heavy ion collisions



- $10 \lesssim \tau \lesssim 20 \text{ fm}/c$
- Hot hadron gas

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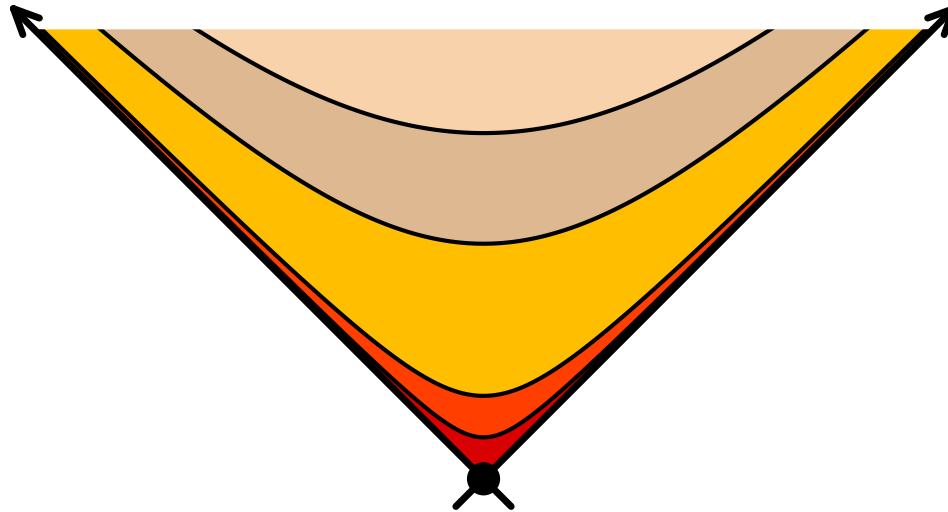
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# Heavy ion collisions



- $\tau \rightarrow +\infty$
- Chemical freeze-out :  
density too small to have inelastic interactions
- Kinetic freeze-out :  
no more elastic interactions

# Degrees of freedom

- Quarks : 2 (spin)  $\times$  3 (color) = 6 (per flavor)

$$\frac{dN_q}{d^3\vec{x}d^3\vec{k}} = \frac{1}{e^{\omega/T} + 1} \quad (\text{Fermi-Dirac})$$

- Gluons : 3 (spin)  $\times$  8 (color) = 24

$$\frac{dN_g}{d^3\vec{x}d^3\vec{k}} = \frac{1}{e^{\omega/T} - 1} \quad (\text{Bose-Einstein})$$

- Average energy per particle :  $\langle \omega \rangle \sim T$

- Particle density :  $\rho \sim T^3$

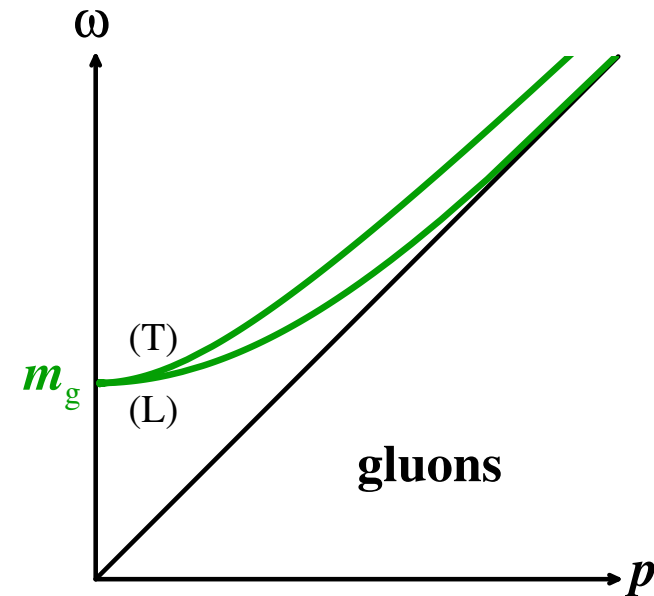
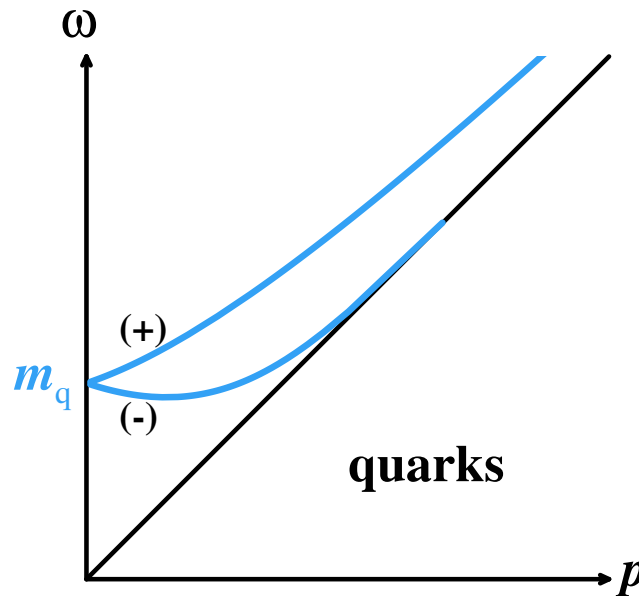
- Average distance between particles :  $\ell \sim 1/T$

- Degrees of freedom
- **Collective phenomena**
- Quasi-particles
- Debye screening
- Landau damping
- Collisional width
- Length scales
- Hydrodynamical regime
- Strongly coupled plasma

- Phenomena involving many elementary constituents
- Large wavelength compared to the typical distance between constituents
- Small frequency or energy
- The quantum numbers of collective excitations may not be related to those of the elementary constituents
  
- Major collective phenomena :
  - ◆ Quasi-particles
  - ◆ Debye screening
  - ◆ Landau damping
  - ◆ Collisional width

# Quasi-particles

- Dispersion curves of particles in the plasma :



- Thermal masses due to interactions with the other particles in the plasma :

$$m_q \sim m_g \sim gT$$

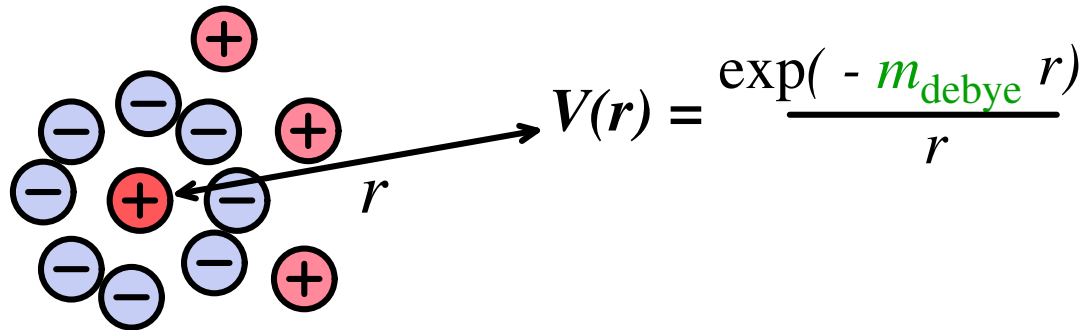
- One needs a non-zero energy to make a particle of the plasma move

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# Debye screening

- A test charge polarizes the particles of the plasma in its vicinity, in order to screen its charge :



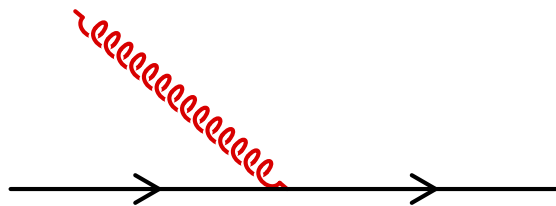
- The Coulomb potential of the test charge decreases exponentially at large distance. The effective interaction range is :

$$\ell \sim 1/m_{\text{debye}} \sim 1/gT$$

- Note : static magnetic fields are not screened by this mechanism (they are screened over length-scales  $\ell_{\text{mag}} \sim 1/g^2T$ )

# Landau damping

- A wave propagating through the plasma is damped because its quanta may be absorbed by particles of the plasma :



- The characteristic frequency of this damping is :

$$\omega_c \sim gT$$

## ■ Decay width :

$$\Gamma_{\text{decay}} = \left| \begin{array}{c} \text{diagram: wavy line decaying into two straight lines} \end{array} \right|^2 \sim g^4 T$$

## ■ Collisional width :

$$\Gamma_{\text{coll}} = \left| \begin{array}{c} \text{diagram: wavy line scattering off a wavy line with momentum p_perp} \end{array} \right|^2 \sim g^4 T^3 \int_{m_{\text{debye}}} \frac{d^2 \vec{p}_{\perp}}{p_{\perp}^4} \sim g^2 T$$

- $\lambda \equiv 1/\Gamma_{\text{coll}}$  is the **mean free path** between two small angle scatterings ( $\theta \sim g$ )
- Note : the mean free path between two large angle scatterings ( $\theta \sim 1$ ) is  $\sim 1/g^4 T$

QGP

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# Length scales

- $1/T$  : wavelength of particles in the plasma
- $1/gT$  : typical distance for collective phenomena
  - ◆ Thermal masses of quasi-particles
  - ◆ Screening phenomena
  - ◆ Damping of waves
- $1/g^2T$  : distance between two small angle scatterings
  - ◆ Color transport
  - ◆ Photon emission
- $1/g^4T$  : distance between two large angle scatterings
  - ◆ Momentum, electric charge transport
    - ▷ characteristic scale of hydrodynamic modes
- In the **weak coupling** limit ( $g \ll 1$ ), there is a clear hierarchy between these scales
- Distinct **effective theories** according to the characteristic scale of the problem under study

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# Length scales

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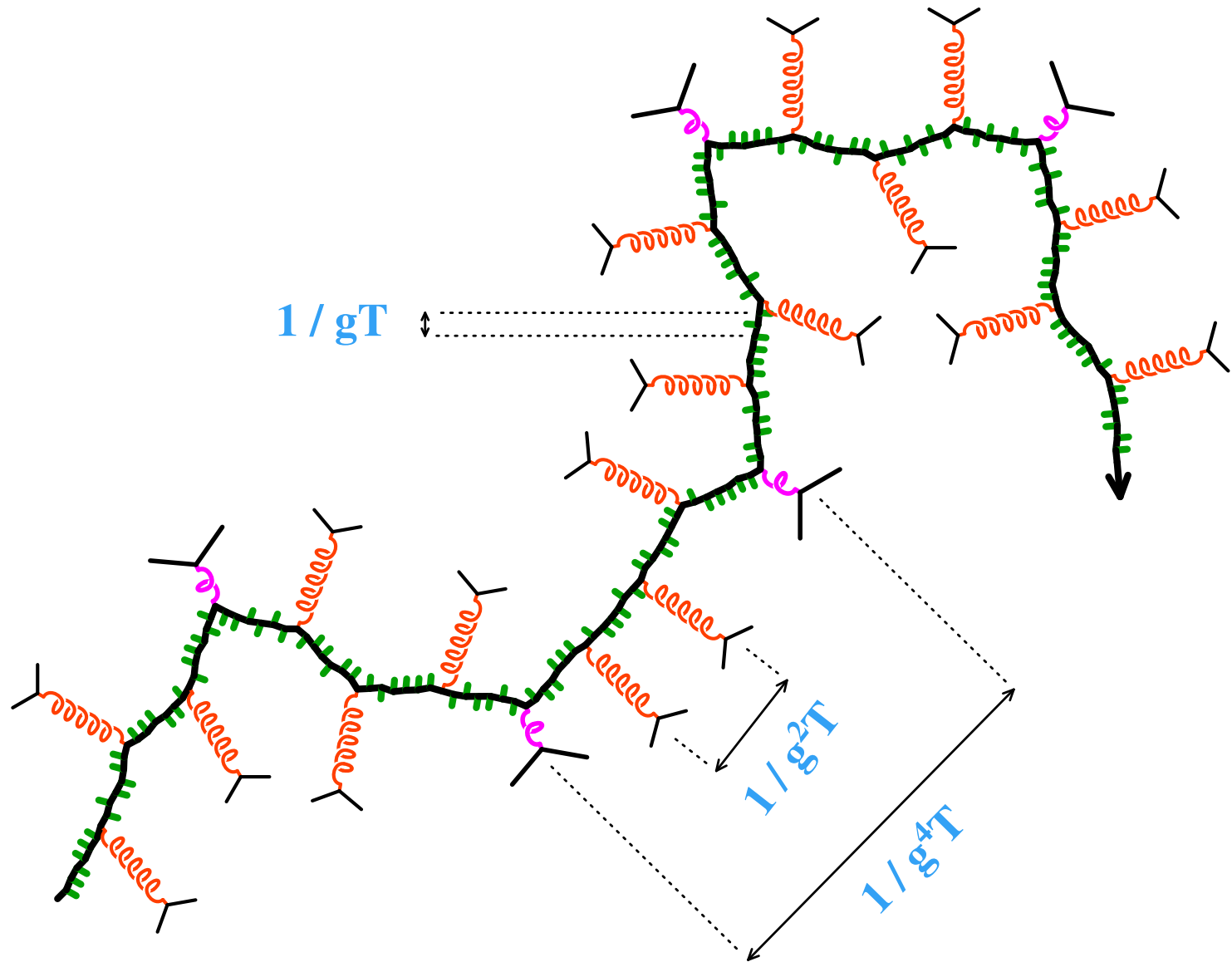
CGC

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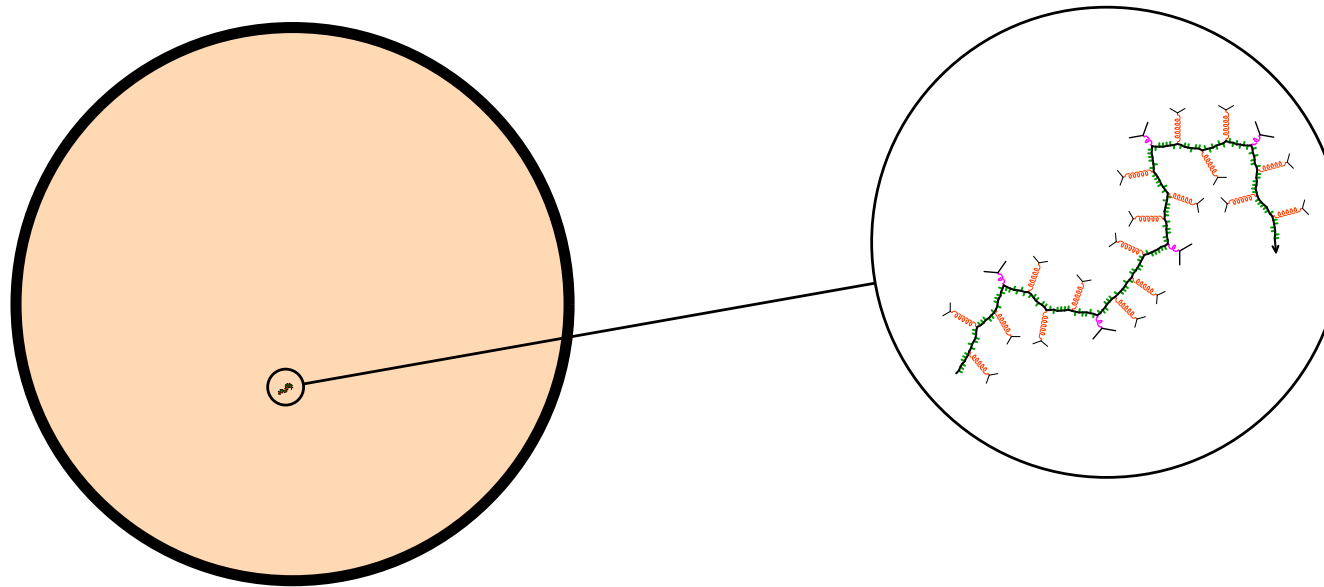
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# Hydrodynamical regime



- The hydrodynamical regime is reached when one considers length scales that are much larger than the mean free path of the plasma constituents :  $\lambda \ll R$
- In order to describe the system at such scales, one needs :
  - ◆ Hydrodynamical equations (**Euler**, **Navier-Stokes**)
  - ◆ Conservation equations for the various currents
  - ◆ **Equation of state**, **viscosity**

QGP

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# Strongly coupled plasma

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- In the real world,  $\alpha_s \sim 0.2-0.3$  (i.e.  $g \sim 2$ ). No clear hierarchy between the various length scales...

- Lattice QCD :  
very difficult to extract transport coefficients

- Alternate approach : **AdS/CFT correspondence**

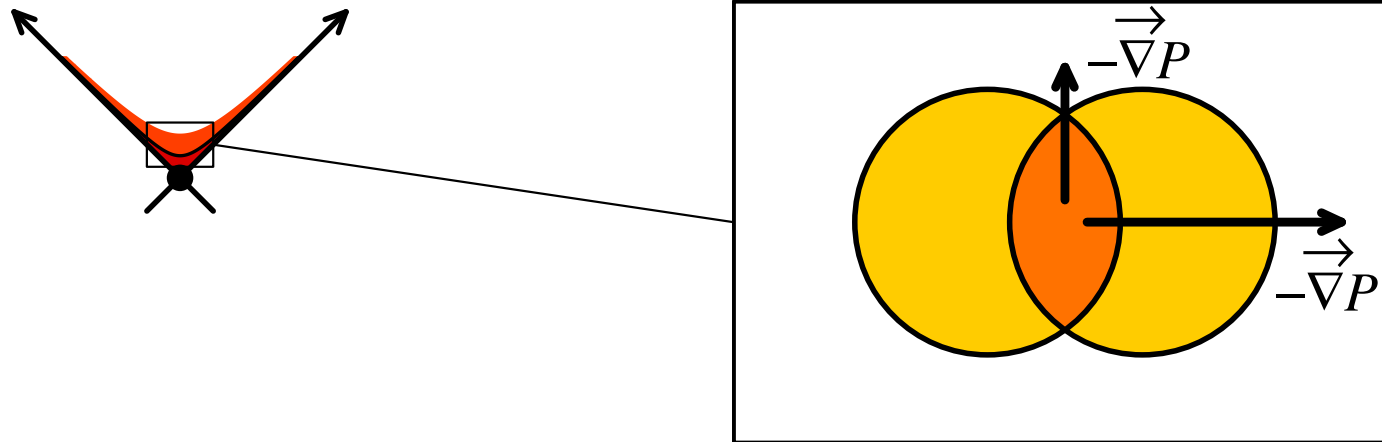
- ◆ **Maldacena conjecture :**

The strong coupling regime of a **super-symmetric Yang-Mills** theory (**very complicated...**) is equivalent to the weak coupling regime of a theory of **super-gravity** (**calculable**)

- ◆ Viscosity of a plasma in the super-YM theory :

$$\frac{\eta}{s} = \frac{1}{4\pi}$$

- ◆ **Major problem :** Super-symmetric QCD  $\neq$  QCD...



- In non-central collisions, pressure turns a **spatial anisotropy** into an anisotropy of the momenta
- Observable:  $2^{\text{nd}}$  harmonic of the azimuthal distribution

$$dN/d\varphi \sim 1 + 2v_1 \cos(\varphi) + 2v_2 \cos(2\varphi) + \dots$$

- **Note:** a large  $v_2$  implies a strong **transverse** pressure, but says very little on the longitudinal degrees of freedom  
 ▷ does not imply a tri-dimensional thermalization...



# Strangeness enhancement

QGP

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QGP signatures

● Collective flow

● **Strangeness enhancement**

● Statistical models

● J/Psi suppression

● Coalescence models

● Thermal photons

● Jet quenching

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CGC signatures

- In a nucleon, the distribution of strange quarks is smaller than that of  $u, d$  quarks (valence) by a factor of the order of  $\alpha_s \sim 0.2-0.3$ 
  - ▷ In  $pp$  collisions, less strange particles are produced than non-strange particles
- In the QGP, the average energy of  $u, d$  quarks and of the gluons is of the order of the temperature
  - ▷ if  $T$  is large enough (compared to the mass of the strange quark), then the processes  $u\bar{u} \rightarrow s\bar{s}$ ,  $d\bar{d} \rightarrow s\bar{s}$ ,  $gg \rightarrow s\bar{s}$  are not inhibited by the kinematical threshold due to the mass of the  $s$  quark
- In this case, the population of strange quarks will become identical to that of light quarks
  - ▷ the production of strange hadrons will be enhanced compared to proton-proton collisions
- The interpretation of data based on **statistical models** works also for strange particles at RHIC

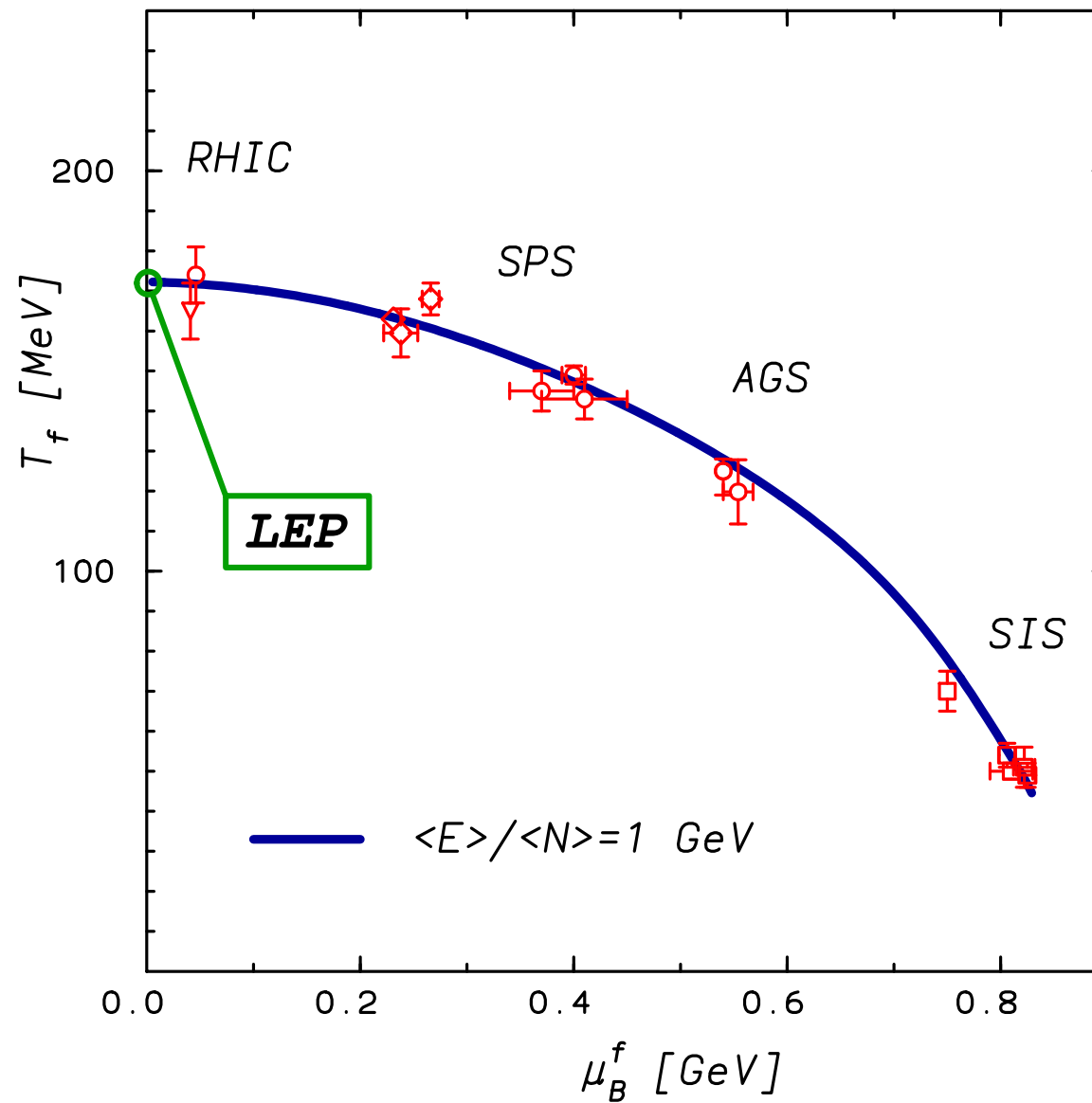
- Collective flow
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- **Statistical models**
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- One assumes that particles are produced by a thermalized system with temperature  $T$  and baryon chemical potential  $\mu_B$
- The number of particles of mass  $m$  per unit volume is :

$$\frac{dN}{d^3\vec{x}} = \int \frac{d^3\vec{p}}{(2\pi)^3} \frac{1}{e^{(\sqrt{p^2+m^2}-\mu_B Q)/T} \pm 1}$$

- These models reproduce the ratios of particle yields with **only two parameters**
- The same models also work for  $e^+e^-$  collisions
  - ◆ Standard explanation: randomly filling a phase space leads to exponential distributions
  - ◆ However, this argument alone does not explain why the value of  $T$  that comes out is the same as in nucleus-nucleus collisions
    - ▷ dynamical arguments (about the properties of the vacuum?) certainly play a role here...

# Freeze-out parameters



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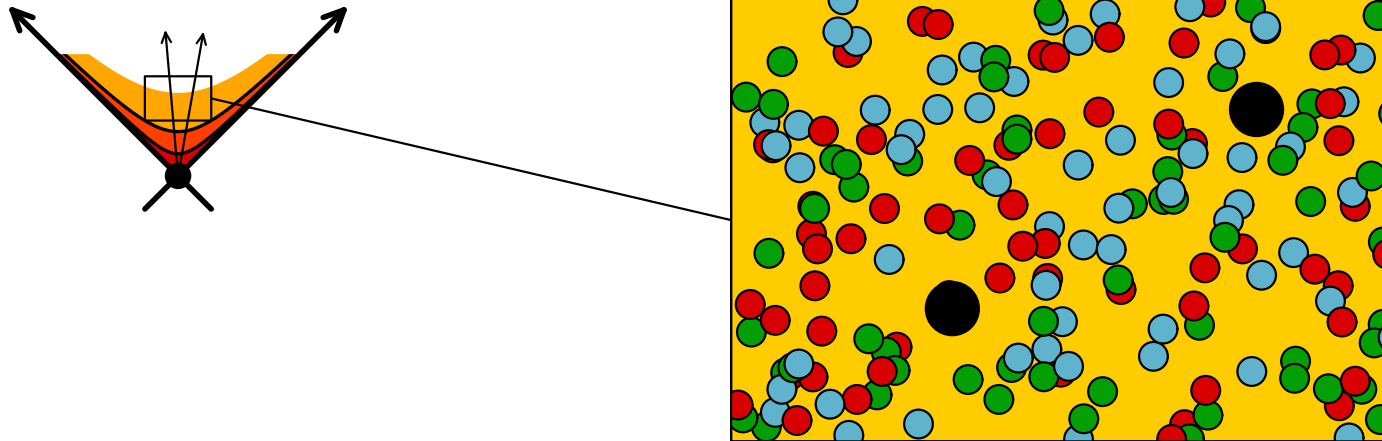
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# J/Psi suppression



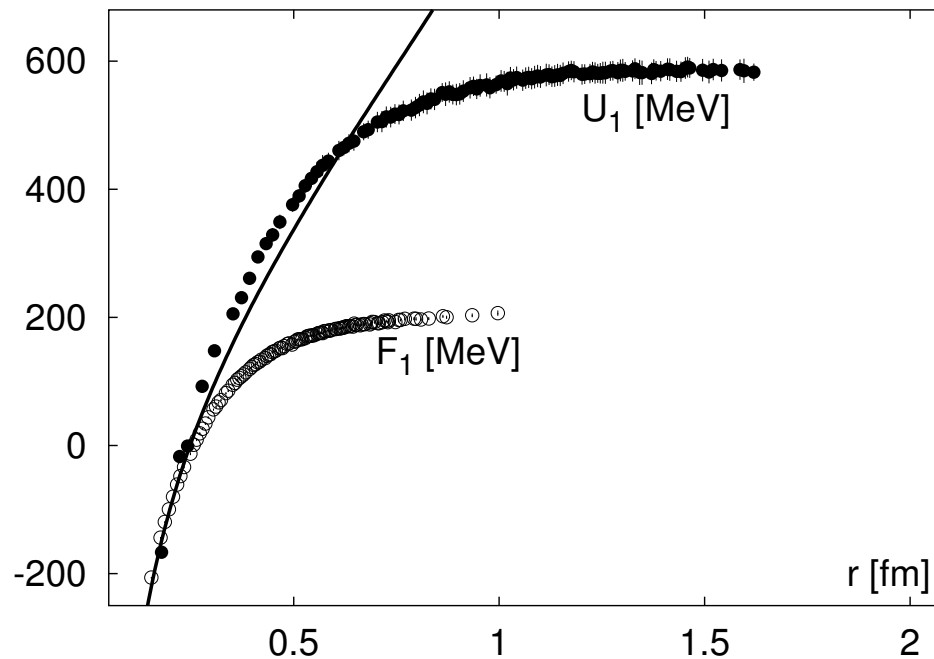
- Debye screening prevents the  $Q\bar{Q}$  pair from forming a bound state Matsui, Satz (1986)
  - ◆ each heavy quark pairs with a light quark in order to form a  $D$  meson
- The inter-quark potential can be calculated using lattice QCD
- Possible observable :  $[J/\psi] / [\text{Open charm}]$ 
  - ▷ complication : there is also a suppression in proton-nucleus collisions, due to multiple scattering

# J/Psi suppression

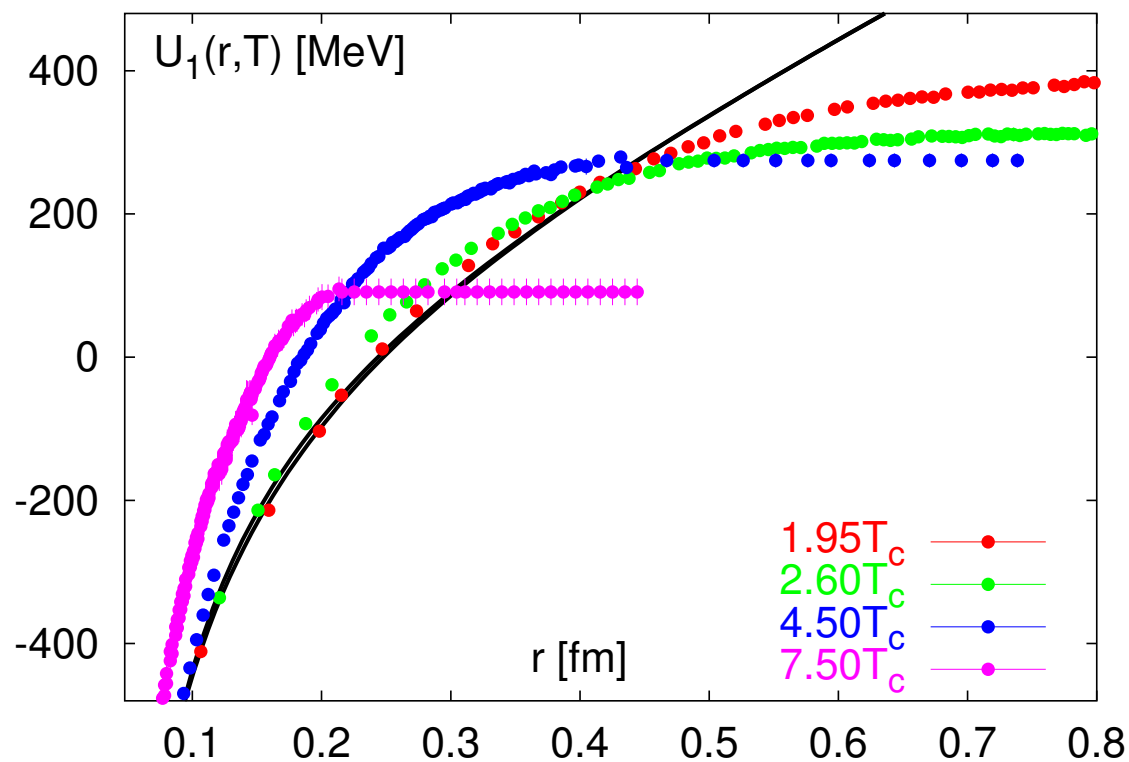
- The free energy of a  $Q\bar{Q}$  pair can be calculated on the lattice, and then converted into a potential by taking into account the entropy :

$$F = U - TS \quad , \quad S = - \frac{\partial F}{\partial T}$$

- Result for  $T/T_c = 1.5$  :



■  $T$  dependence of the potential :



- Collective flow
- Strangeness enhancement
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- J/Psi suppression
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## ■ What do we do with this potential?

- ◆ Shrödinger equation for a  $Q\bar{Q}$  bound state :

$$\left[ 2m_Q + \frac{1}{m_Q} \vec{\nabla}^2 + U_1(r, T) \right] \Psi = M(T) \Psi$$

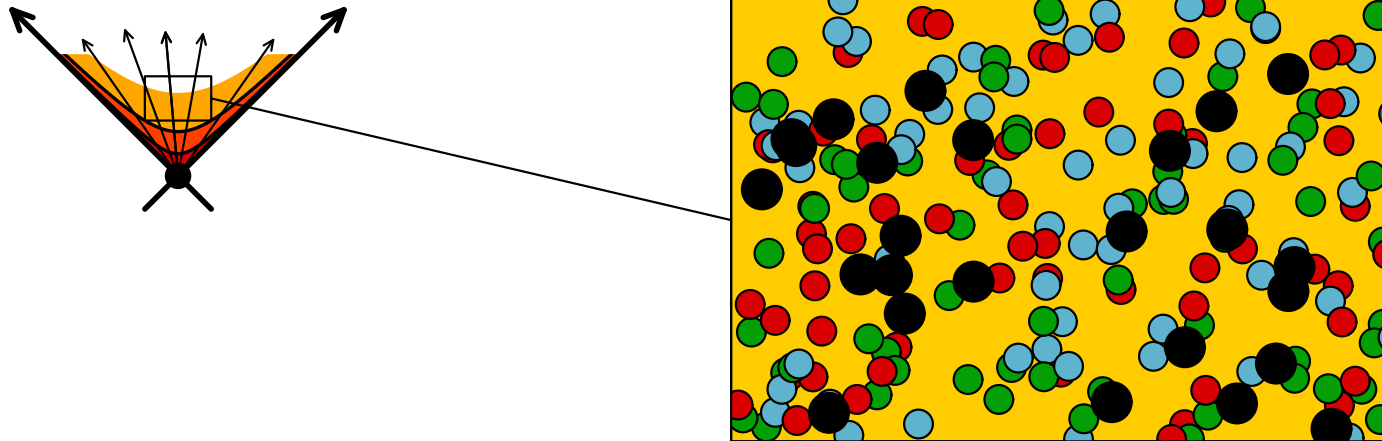
- ◆ Non-relativistic
- ◆ Assumes that there are only two-body interactions

## ■ Dissociation temperatures :

state	$J/\psi$	$\chi_c$	$\psi'$	$\Upsilon$	$\chi_b$	$\Upsilon'$
$T_d/T_c$	2.0	1.1	1.1	4.5	2.0	2.0

▷ the  $Q\bar{Q}$  states are not dissolved immediately above the critical temperature

# ... or enhancement ?



- Many  $Q\bar{Q}$  pairs may be produced in each  $AA$  collision  
Braun-Munzinger, Stachel (2000)  
Thews, Schroedter, Rafelski (2001)
  - ◆ A  $Q$  from one pair may recombine with a  $\bar{Q}$  from another pair
- Avoids the conclusion of Matsui and Satz's scenario, provided that the average distance between heavy quarks is smaller than the Debye screening length
- May lead to an enhancement of  $J/\psi$  production

- Collective flow
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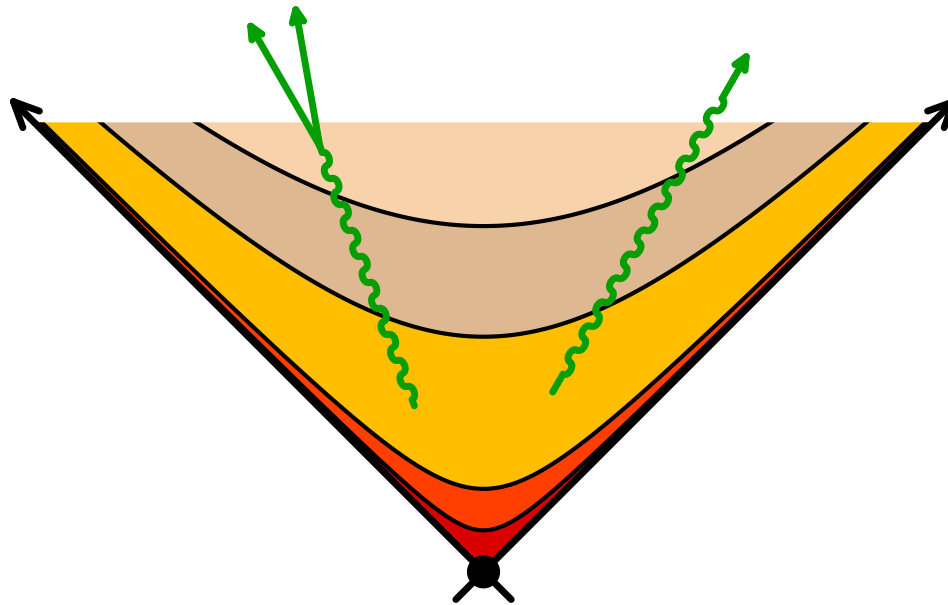
- In proton-proton collisions, hadronization is described via **fragmentation functions** :

$$\frac{dN_H}{d^3\vec{p}} = \sum_i \int_0^1 dz F_{i \rightarrow H}(z) \left. \frac{dN_i}{d^3\vec{q}} \right|_{\vec{q}=\vec{p}/z}$$

- ◆  $F_{p \rightarrow H}(z)$  is the probability that a parton  $p$  gives the hadron  $H$  (accompanied by any other fragments), the hadron carrying the fraction  $z$  of the momentum of the parton
- ◆ This formulation forbids that several partons combine into the same hadron

- In an environment having a **large parton density**, hadronization can occur via the coalescence of several partons (Note: present models are very primitive, and take into account only the valence quark)
- These models can explain some differences between baryons and mesons observed in RHIC data

# Thermal photons



- Photons produced by the QGP :
  - ◆ Rate determined by physics at the scale  $g^2 T$
  - ◆ Very sensitive to the temperature :  $dN_\gamma/dtd^3\vec{x} \sim T^4$

QGP

Basic features of QCD

Deconfinement transition

Physics of the QGP

QGP signatures

- Collective flow
- Strangeness enhancement
- Statistical models
- J/Psi suppression
- Coalescence models
- Thermal photons
- Jet quenching

CGC

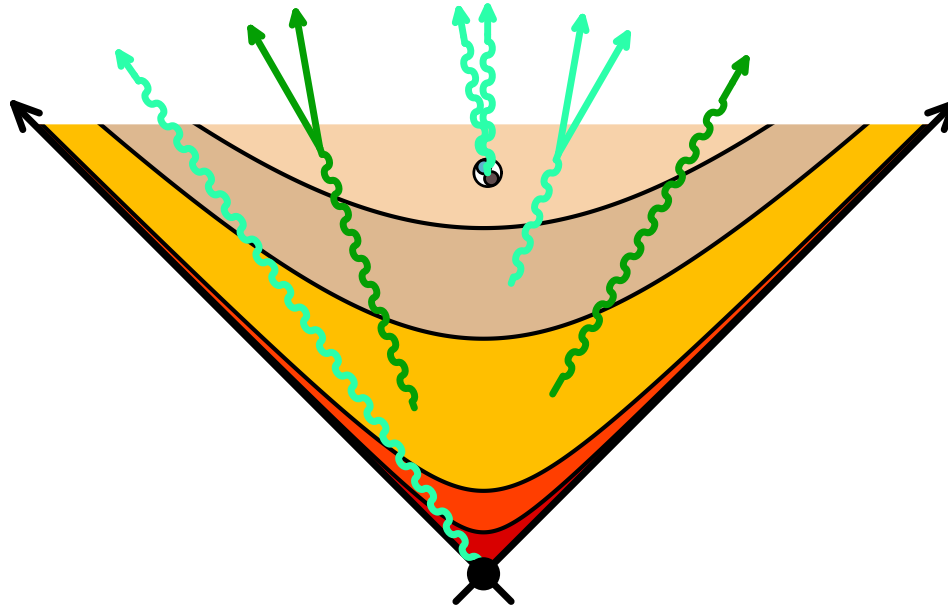
Parton model

Saturation

Color Glass Condensate

CGC signatures

# Thermal photons



- Photons produced by the QGP :
  - ◆ Rate determined by physics at the scale  $g^2 T$
  - ◆ Very sensitive to the temperature :  $dN_\gamma / dt d^3 \vec{x} \sim T^4$
- But very important background...
  - ◆ initial photons
  - ◆ photons produced by in-medium jet fragmentation
  - ◆ photons produced by the hadron gas
  - ◆ meson decays

QGP

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Parton model

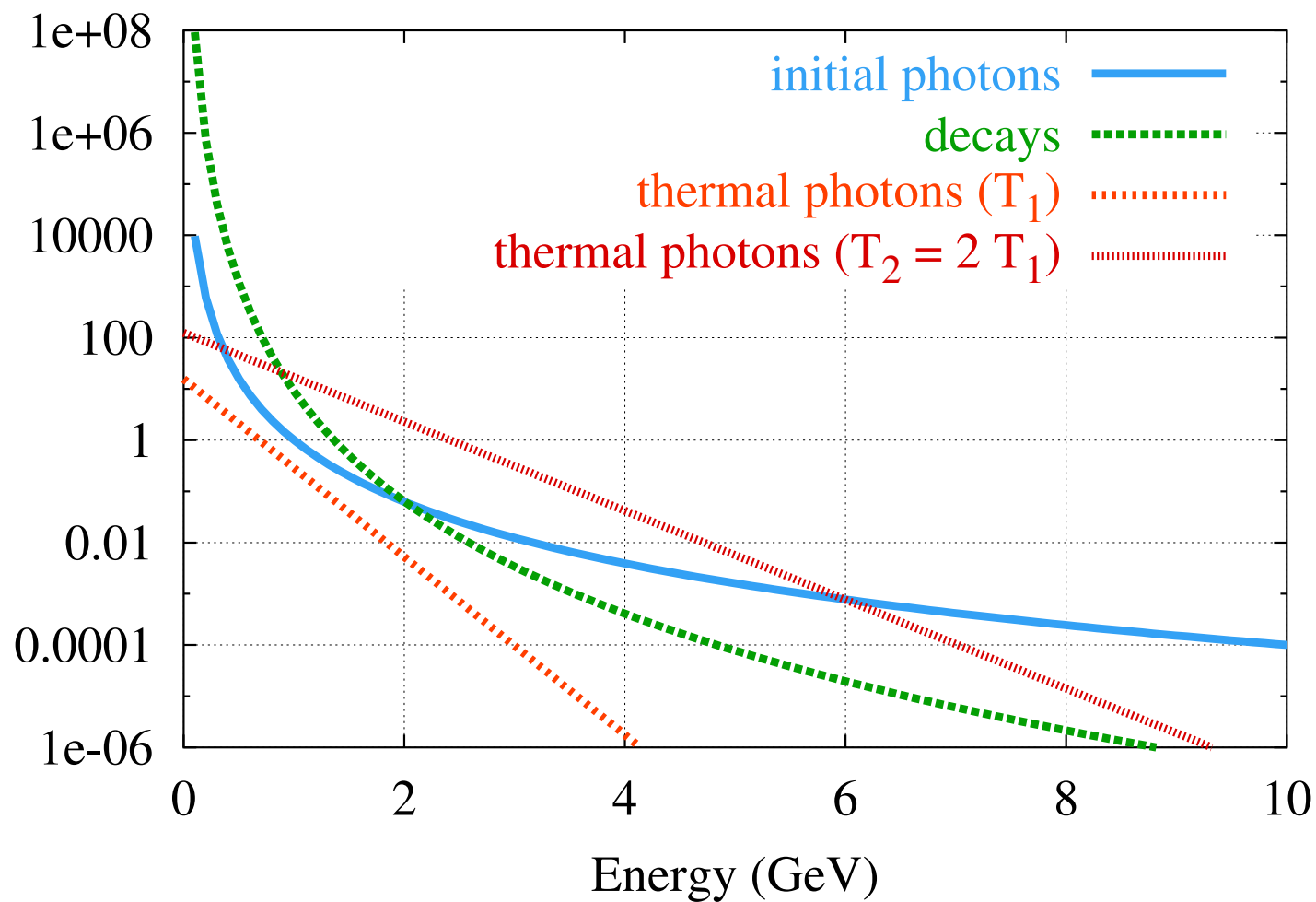
Saturation

Color Glass Condensate

CGC signatures

# Thermal photons

Photon spectrum (arbitrary units)



- QGP
- Basic features of QCD
- Deconfinement transition
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- QGP signatures
  - Collective flow
  - Strangeness enhancement
  - Statistical models
  - J/Psi suppression
  - Coalescence models
  - **Thermal photons**
  - Jet quenching
- CGC
- Parton model
- Saturation
- Color Glass Condensate
- CGC signatures

# Variant: thermal dileptons

QGP

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- Jet quenching

CGC

Parton model

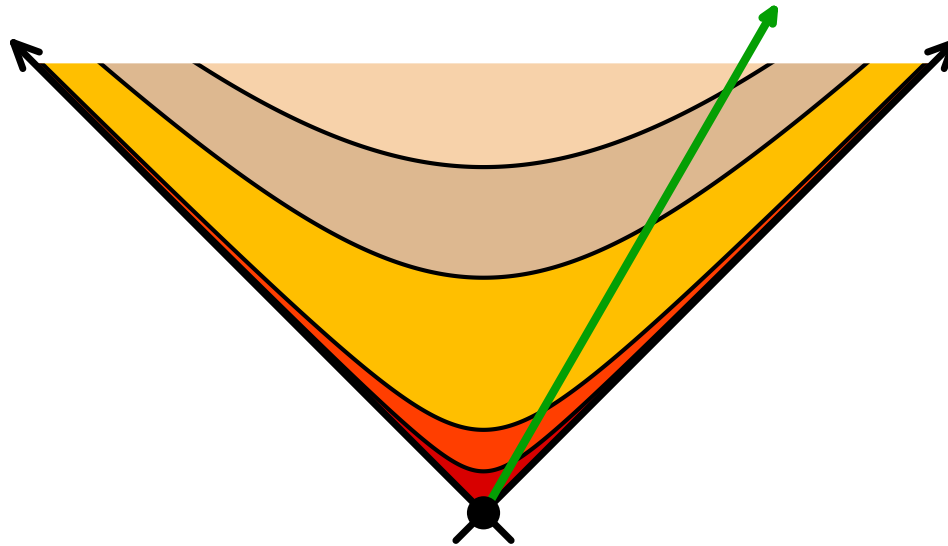
Saturation

Color Glass Condensate

CGC signatures

- Look for **virtual** photons, in the channel  $l^+ l^-$
- Chose the invariant mass of the lepton pair in a region which is not too contaminated by resonance decays
- Note : if the invariant mass of the virtual photon is small, then the production mechanisms are the same as for the production of real photons
- Difficulty : the decay  $\gamma^* \rightarrow l^+ l^-$  brings another power of the electromagnetic coupling  $\alpha_{em} \approx 1/137$  in the production rate  
▷ problem of statistics

# Jet quenching



- Jets are produced at the initial impact
  - ◆ Not very interesting by themselves...

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CGC

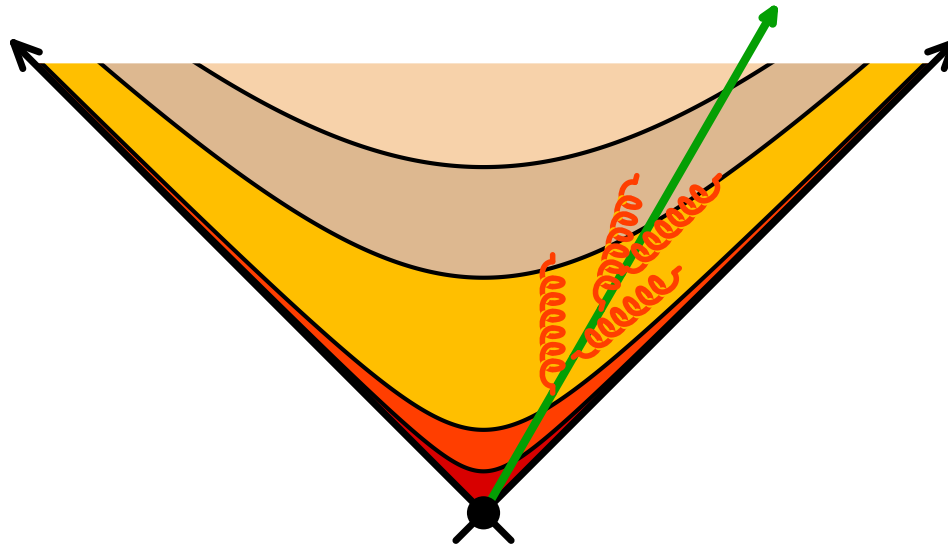
Parton model

Saturation

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CGC signatures

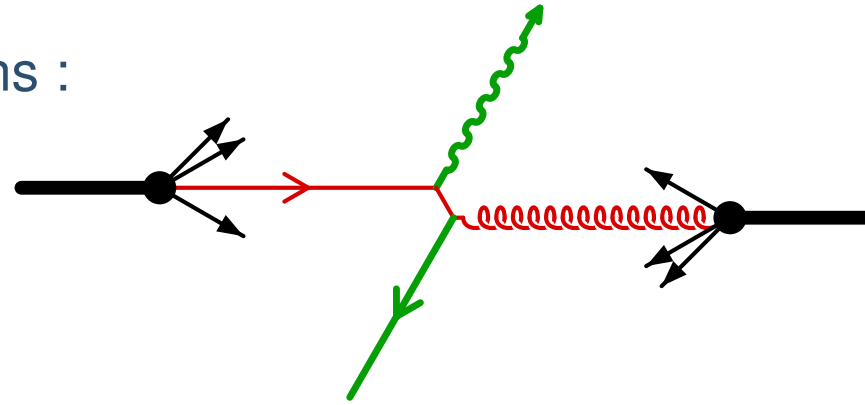
# Jet quenching



- Jets are produced at the initial impact
  - ◆ Not very interesting by themselves...
- Radiative energy loss when they travel through the QGP
  - ◆ Sensitive to the energy density of the medium
  - ◆ Depends on the path length as  $L^2$
  - ◆ Important modification of the azimuthal correlations (at RHIC, complete absorption of the opposite jet)

- Collective flow
- Strangeness enhancement
- Statistical models
- J/Psi suppression
- Coalescence models
- Thermal photons
- Jet quenching

## ■ Photon-jet correlations :



- ◆ At leading order, **the photon and the jet have opposite  $\vec{p}_\perp$ 's**
- ◆ The photon escapes without any energy loss, and gives a reference for the energy of the jet  $\triangleright$  one can compare the properties of jet after going through the medium to those of a jet of the same  $\vec{p}_\perp$  which has been produced in the vacuum

## ■ Complications due to higher order corrections :

- ◆ Final state with **photon + two jets**
- ◆ Photon produced by **fragmentation of a quark**
  - $\triangleright$  in both cases, the momentum of the photon is not directly related to the initial momentum of a jet



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**CGC**

Parton model

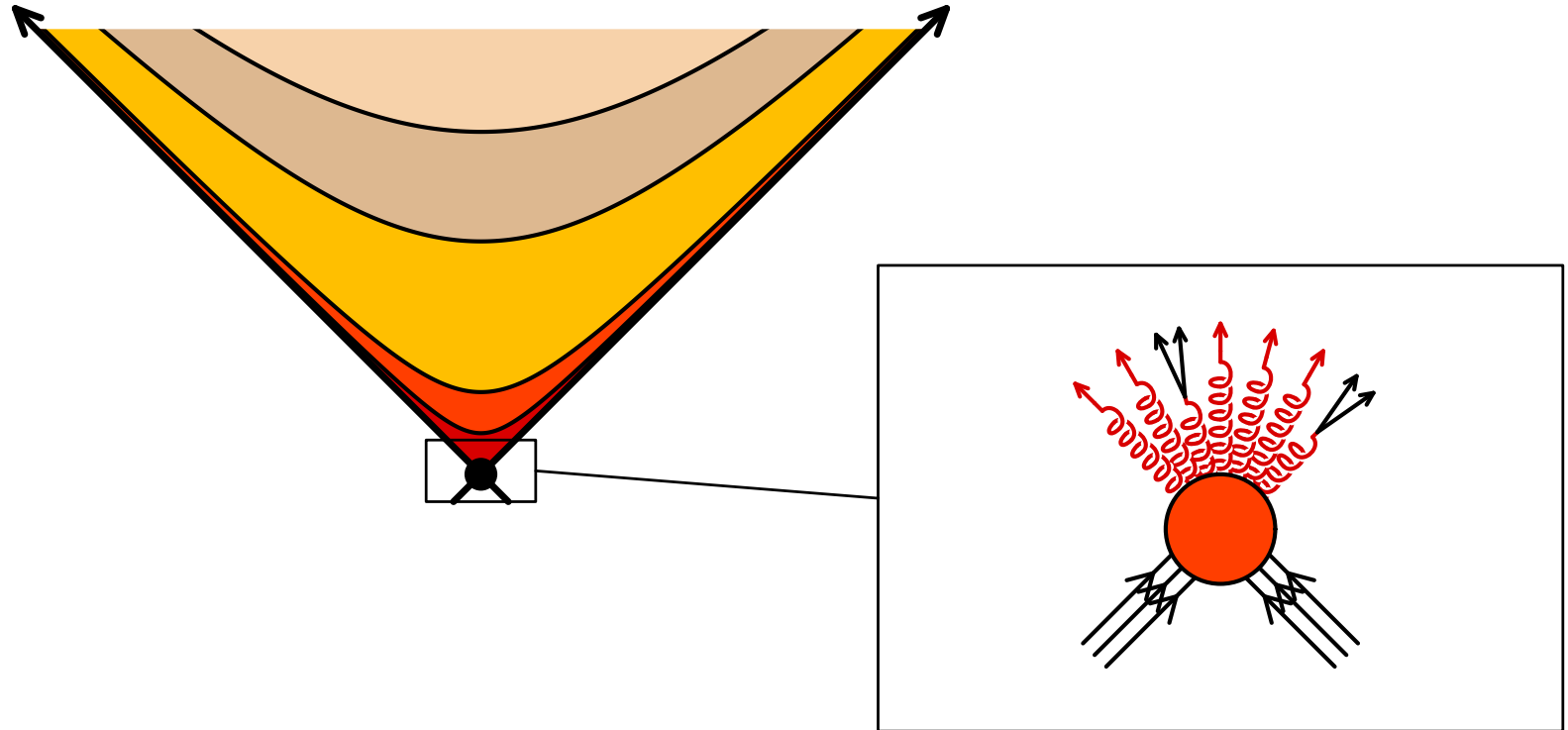
Saturation

Color Glass Condensate

CGC signatures

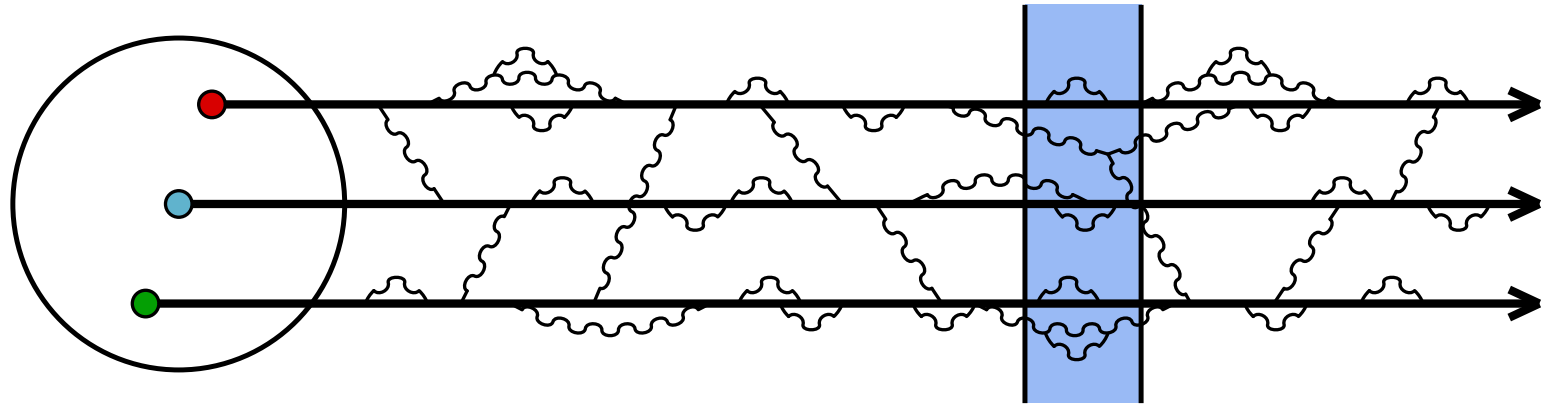
# CGC

# Where does the CGC stand ?



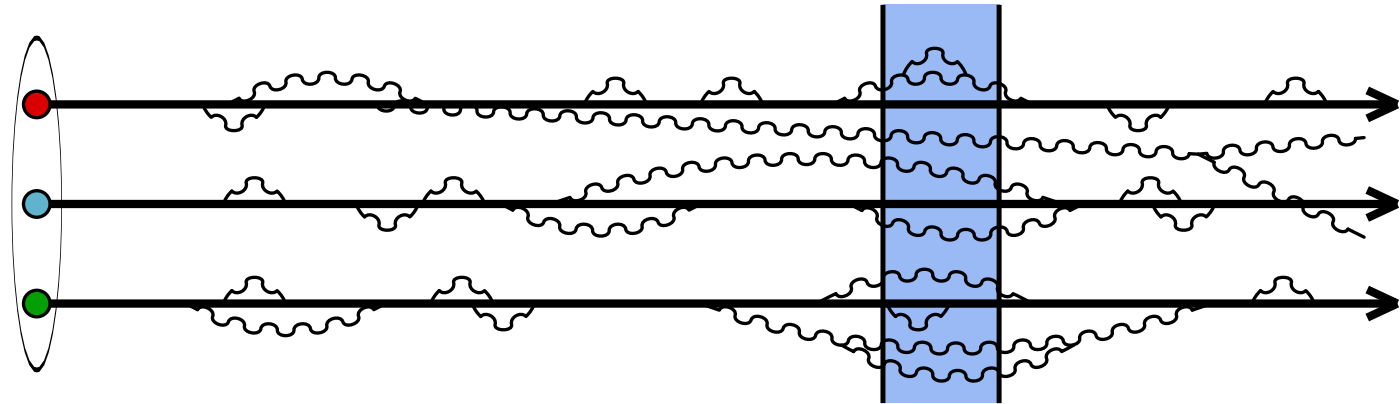
- describes the content of nucleons and nuclei at small  $x$
- framework to calculate the production of semi-hard particles
- provides initial conditions for the subsequent evolution

# Nucleon at rest



- Very complicated **non-perturbative** object...
- Contains **fluctuations at all space-time scales** smaller than its own size
- Only the fluctuations that are longer lived than the external probe participate in the interaction process
- The only role of short lived fluctuations is to renormalize the masses and couplings
- Interactions are very complicated if the constituents of the nucleon have a non trivial dynamics over time-scales comparable to those of the probe

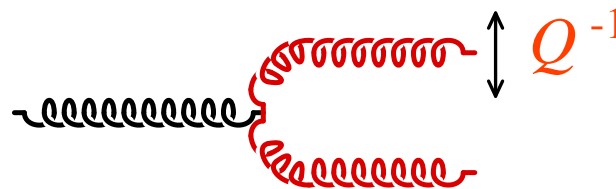
# Nucleon at high energy



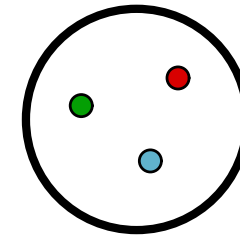
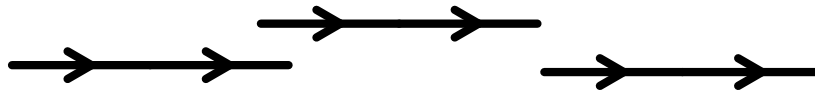
- Dilation of all internal time-scales of the nucleon
- Interactions among constituents now take place over time-scales that are longer than the characteristic time-scale of the probe
  - ▷ the constituents behave as if they were free
- Many fluctuations live long enough to be seen by the probe. The nucleon appears denser at high energy (it contains more gluons)
- Pre-existing fluctuations are totally frozen over the time-scale of the probe, and act as static sources of new partons

# Parton model

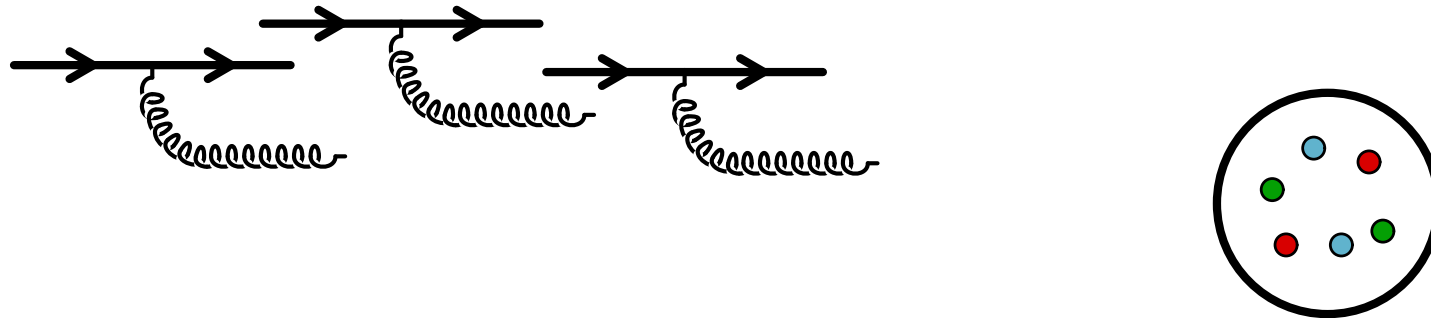
- At the time of the interaction, the nucleon can be seen as a collection of **free constituents**, called **partons**
- The nucleon content is described by **parton distributions**, that depend on the momentum fraction  $x$  of the parton
- One needs only to calculate the **cross-section** between the probe and the partons. If the parton density is low, only one parton interacts
- One can separate the **hard diffusion, perturbative**, from the **non-perturbative parton distributions**, because the strong interactions responsible for these non-perturbative effects act on much longer time-scales (“**factorization**”)
- Note: parton distributions also depend on a “**transverse resolution scale**”,  $Q$  :



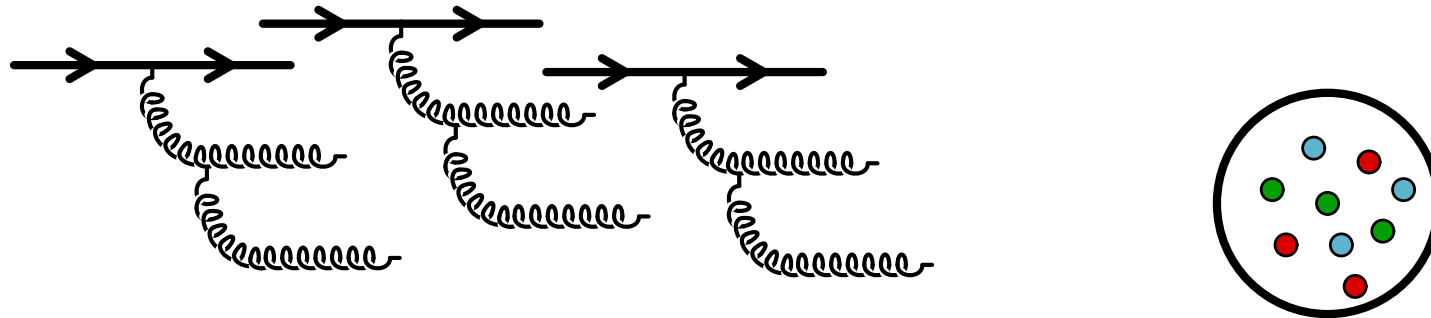
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- Parton model
  - Nucleon at rest
  - Nucleon at high energy
  - Parton model
- Saturation
- Color Glass Condensate
- CGC signatures



▷ at low energy, only valence quarks are present in the hadron wave function



- ▷ when energy increases, new partons are emitted
- ▷ the emission probability is  $\alpha_s \int \frac{dx}{x} \sim \alpha_s \ln\left(\frac{1}{x}\right)$ , with  $x$  the longitudinal momentum fraction of the gluon
- ▷ at small- $x$  (i.e. high energy), these logs need to be resummed



▷ as long as the density of constituents remains small, the evolution is **linear**: the number of partons produced at a given step is proportional to the number of partons at the previous step (BFKL)

QGP

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Saturation

● Linear evolution

● Non-linear evolution

● Saturation criterion

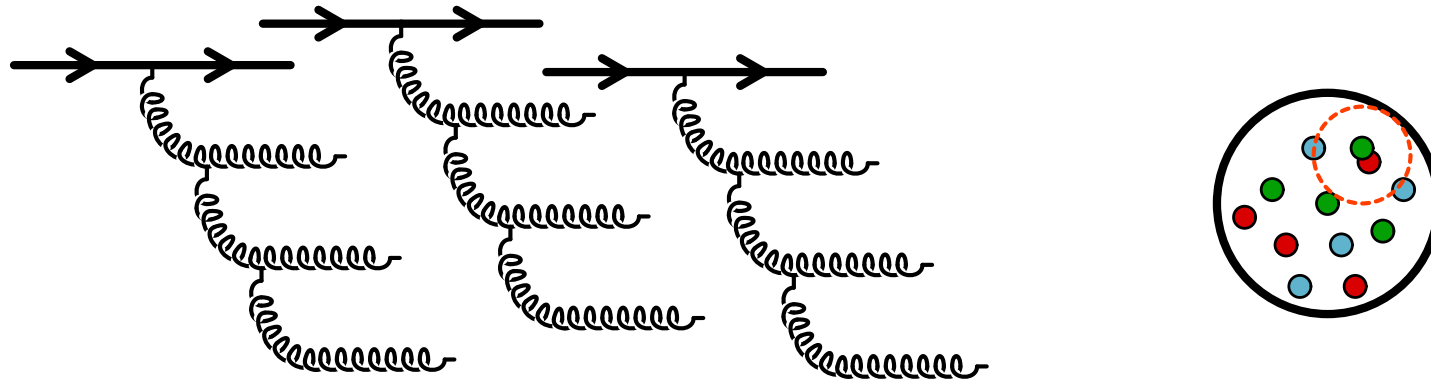
● Saturation domain

Color Glass Condensate

CGC signatures

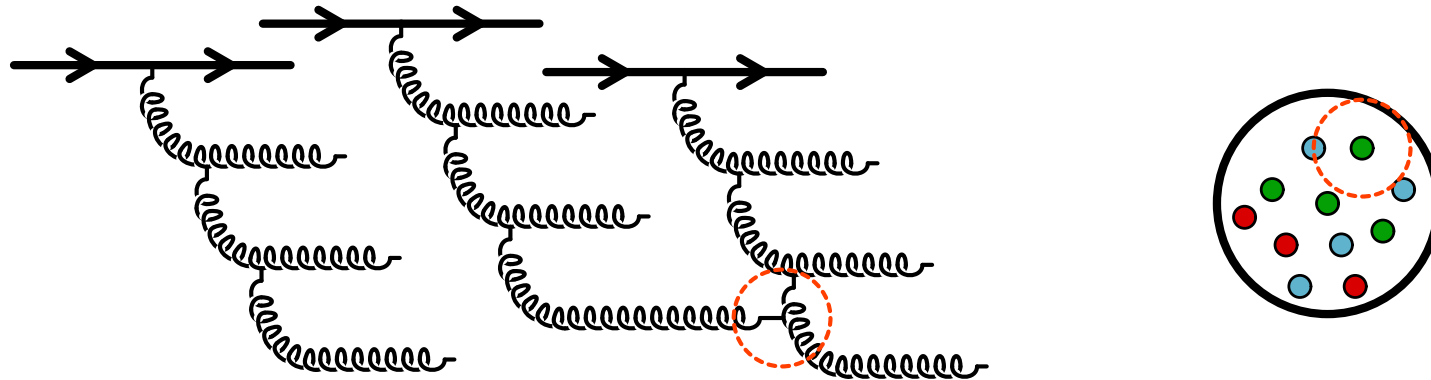


- Linear evolution
- **Non-linear evolution**
- Saturation criterion
- Saturation domain



▷ eventually, the partons start overlapping in phase-space

- Linear evolution
- **Non-linear evolution**
- Saturation criterion
- Saturation domain



▷ parton recombination becomes favorable

▷ after this point, the evolution is **non-linear**:  
the number of partons created at a given step depends non-linearly  
on the number of partons present previously

Gribov, Levin, Ryskin (1983)

- Number of gluons per unit area:

$$\rho \sim \frac{xG(x, Q^2)}{\pi R^2}$$

- Recombination cross-section:

$$\sigma_{gg \rightarrow g} \sim \frac{\alpha_s}{Q^2}$$

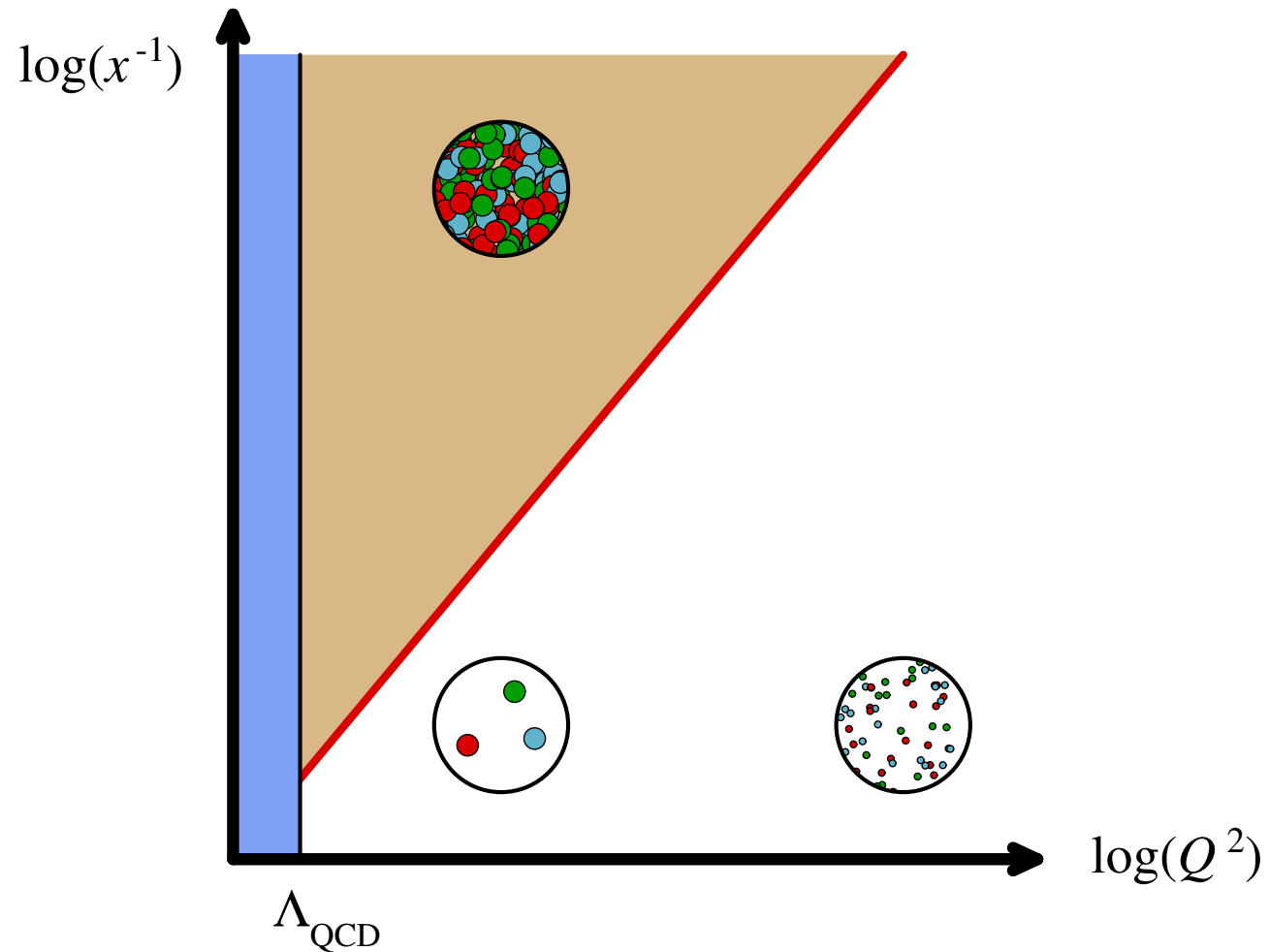
- Recombination happens if  $\rho \sigma_{gg \rightarrow g} \gtrsim 1$ , i.e.  $Q^2 \lesssim Q_s^2$ , with:

$$Q_s^2 \sim \frac{\alpha_s xG(x, Q_s^2)}{\pi R^2}$$

- At saturation, the phase-space density is:

$$\frac{dN_g}{d^2 \vec{x}_\perp d^2 \vec{p}_\perp} \sim \frac{\rho}{Q^2} \sim \frac{1}{\alpha_s}$$

# Saturation domain



- Boundary defined by  $Q^2 = Q_s^2(x)$

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CGC signatures

McLerran, Venugopalan (1994)

Iancu, Leonidov, McLerran (2001)

- Small  $x$  modes have a large occupation number
  - ▷ they can be described by a **classical color field**  $A^\mu$
- Large  $x$  modes, slowed down by time dilation, are described as **static color sources**  $\rho$
- The classical field obeys Yang-Mills equations :

$$D_\nu F^{\nu\mu} = J^\mu = \delta^{\mu+} \delta(x^-) \rho(\vec{x}_\perp)$$

- The color sources  $\rho$  are **random**, and described by a **statistical distribution**  $W_{x_0}[\rho]$ , where  $x_0$  is the separation between “small  $x$ ” and “large  $x$ ”
- An evolution equation (JIMWLK) controls the changes of  $W_{x_0}[\rho]$  with  $x_0$  (generalizes BFKL to the saturated regime)

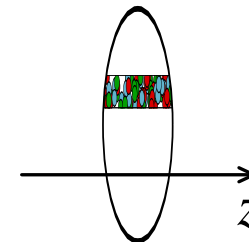
## McLerran (mid 2000)

- **Color** : more or less obvious...
- **Glass** : the system has degrees of freedom whose time-scale is much larger than the typical time-scales for interaction processes. Moreover, these degrees of freedom are stochastic variables, like in “spin glasses” for instance
- **Condensate** : the soft degrees of freedom are as densely packed as they can (the density remains finite, of order  $\alpha_s^{-1}$ , due to repulsive interactions between gluons)

# McLerran-Venugopalan model

- The JIMWLK equation must be completed by an initial condition, given at some  $x_0$
- As with DGLAP, the initial condition is in general non-perturbative
- The **McLerran-Venugopalan** model is often used as an initial condition at moderate  $x_0$  for a large **nucleus** :

- ◆ partons are randomly distributed
- ◆ many partons in each “tube”
- ◆ absence of correlations at different  $\vec{x}_\perp$



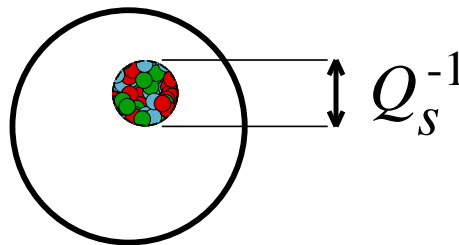
- The MV model assumes that the density of color charges  $\rho(\vec{x}_\perp)$  has a **gaussian** distribution :

$$W_{x_0}[\rho] = \exp \left[ - \int d^2 \vec{x}_\perp \frac{\rho(\vec{x}_\perp) \rho(\vec{x}_\perp)}{2\mu^2(\vec{x}_\perp)} \right]$$

# Correlation length

- In a nucleon at low energy, the typical correlation length among color charges is of the order of the nucleon size, i.e.  $\Lambda_{QCD}^{-1} \sim 1 \text{ fm}$ . Indeed, at low energy, color screening is due to confinement, controlled by the non-perturbative scale  $\Lambda_{QCD}$

- At high energy (small  $x$ ), partons are much more densely packed, and it can be shown that color neutralization occurs in fact over distances of the order of  $Q_s^{-1} \ll \Lambda_{QCD}^{-1}$

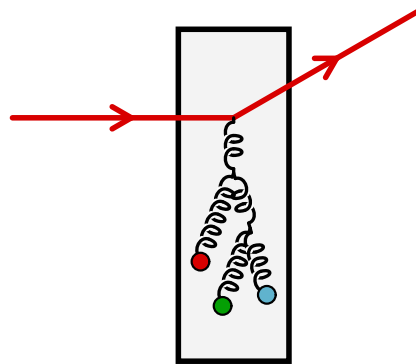


- This implies that all hadrons, and nuclei, behave in the same way at high energy. In this sense, the small  $x$  regime described by the CGC is universal



# Leading twist shadowing

- Interactions between the partons of the target :



- ◆ At small  $x$ , the wave function of a parton “spreads” outside of the nucleon it belongs to, so that it can interact with partons from other nucleons. This implies :

$$xG_{\text{noyau}}(x, Q^2) < A xG_{\text{nucleon}}(x, Q^2)$$

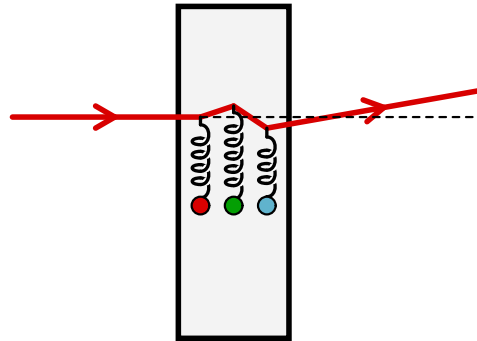
- ◆ At small  $x$ , one has a suppression of cross-sections :

$$d\sigma_{pA}/d^2\vec{p}_\perp \sim A^\alpha \quad \text{with} \quad \alpha < 1$$

- ◆ Note: these interactions are the same as those involved in saturation

# Multiple scatterings

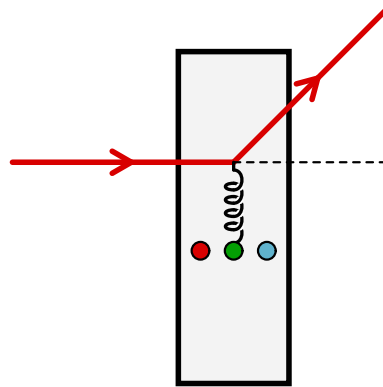
- Because of the large parton density at small  $x$  in the target, the external probe can interact several times :



- ◆ One of the scatterings “produces” the final state, and the others merely change its momentum (“higher twist” shadowing)
- ◆ Each additional scattering brings a correction  $\alpha_s A^{1/3} \Lambda^2 / p_\perp^2$ 
  - ▷ important effect at small  $p_\perp$ , despite the  $\alpha_s$  suppression
- ◆ At leading order, multiple scattering only affect the momentum distribution of the final particles, but not their total number. The suppression at small  $p_\perp$  is compensated by an increase at larger  $p_\perp$  (**Cronin effect**)

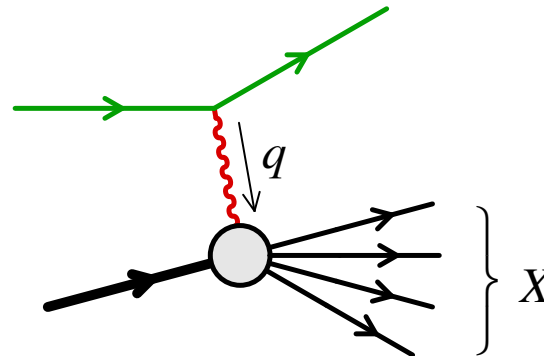
# Multiple scatterings

- At high  $p_{\perp}$ , a single scattering dominates :

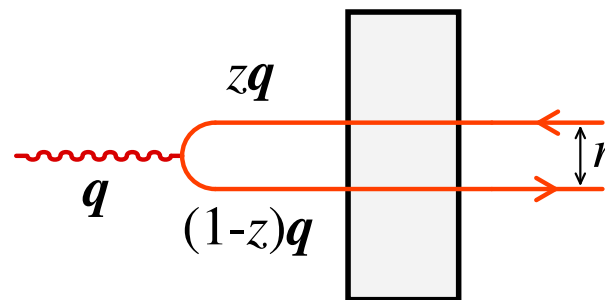


- ◆ Standard result for a random walk in an external potential, when the potential does not decrease fast at large momentum (“intermittency”)
  - ◆ Differential cross-sections scale like the atomic number  $A$  at high  $p_{\perp}$
- Note : the MV model describes correctly multiple scatterings, but does not contain any “leading twist” shadowing at small  $x$

# Deep Inelastic Scattering



- In a frame in which the virtual photon has a large energy :



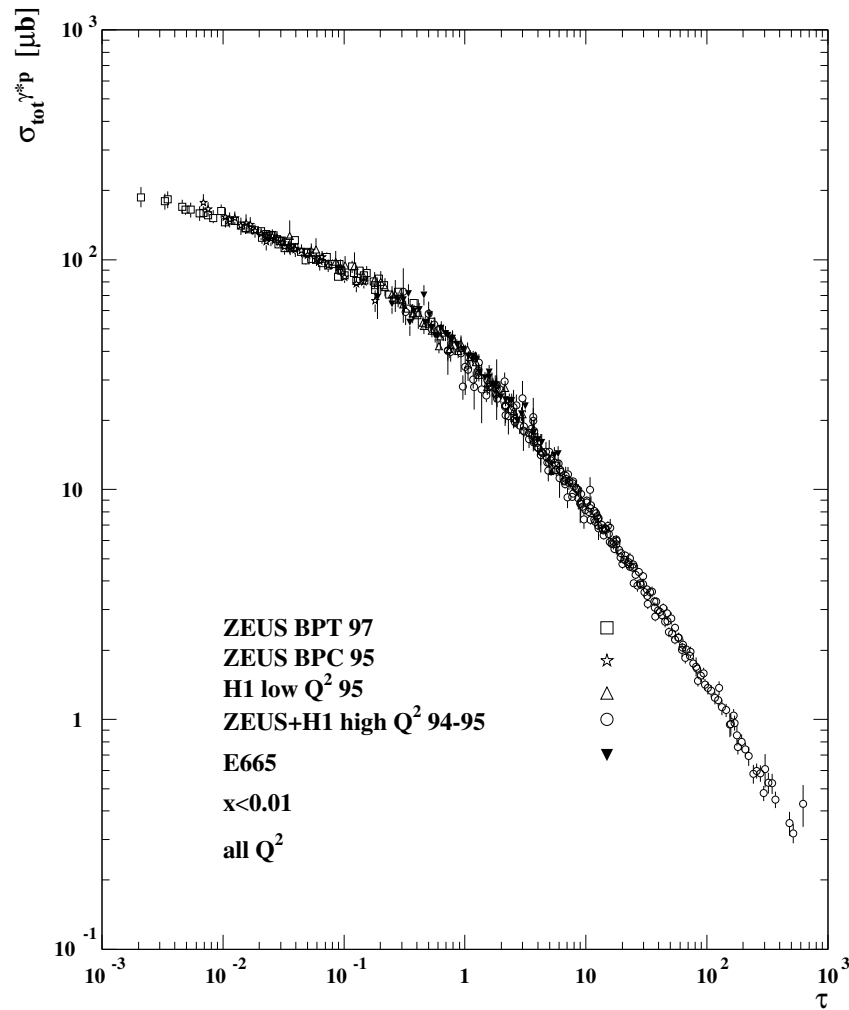
- The structure function  $F_2$  can be expressed in terms of the “dipole” cross-section :

$$F_2 \sim \sigma_{\gamma^* p}(x, Q^2) = \int_0^\infty r dr \int_0^1 dz |\psi(z, r, Q^2)|^2 \sigma_{\text{dipole}}(x, r)$$

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  - Deep Inelastic Scattering
  - Nucleus-nucleus collisions
  - Proton-nucleus collisions

# Deep Inelastic Scattering

- “Geometrical” scaling :  $F_2(x, Q^2) = F_2(\tau \equiv Q^2 / Q_s^2(x))$



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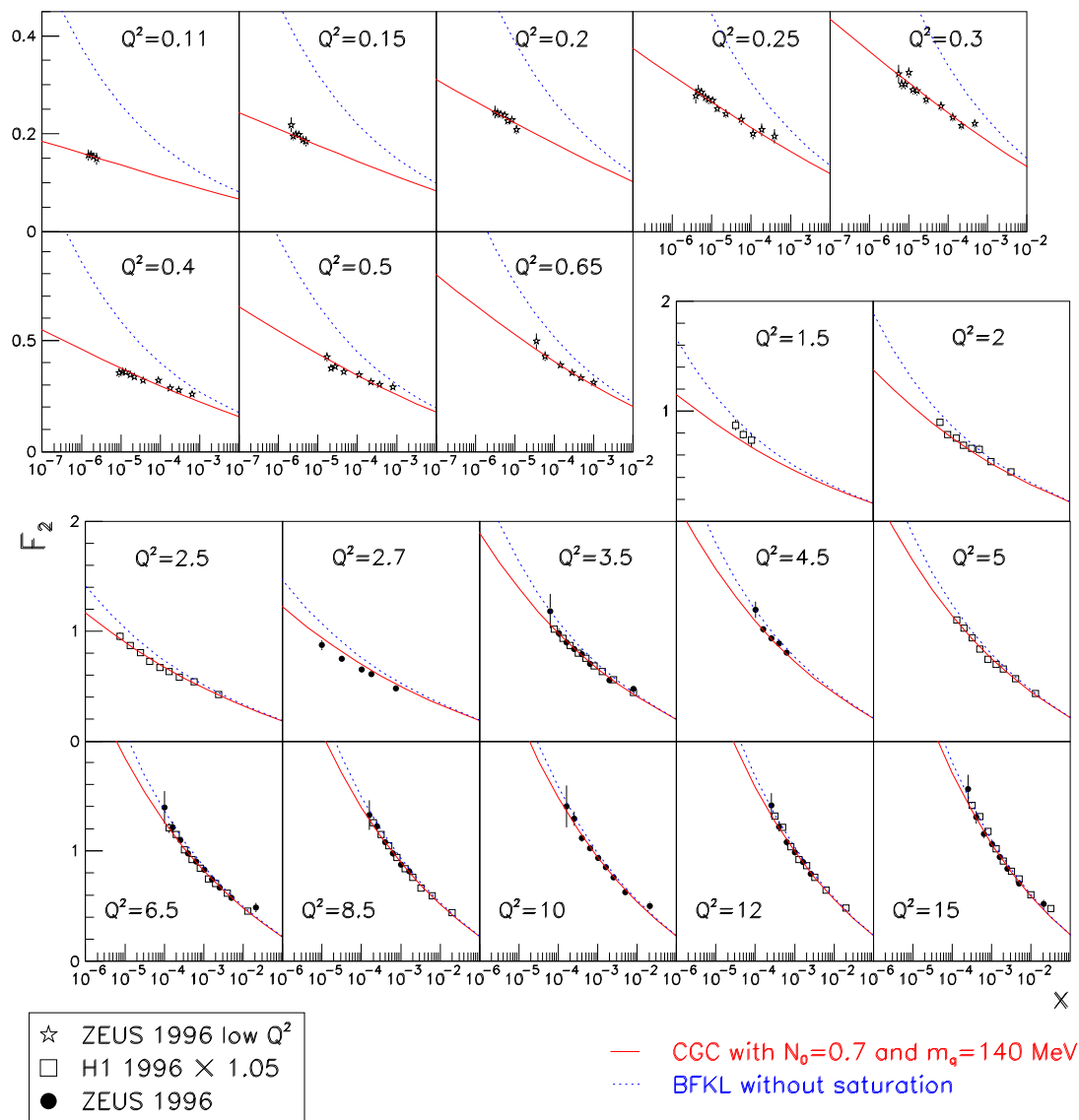
CGC signatures

● Deep Inelastic Scattering

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● Proton-nucleus collisions

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# Nucleus-nucleus collisions

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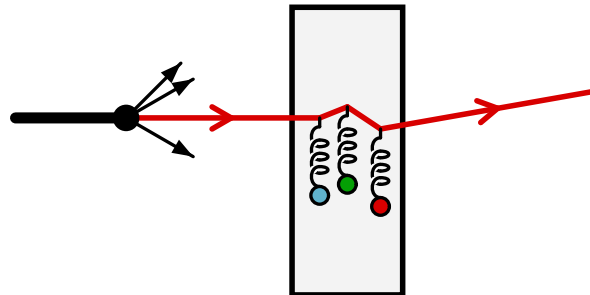
● Nucleus-nucleus collisions

● Proton-nucleus collisions

- The major problem is that the CGC only describes the very first instants after the collision ( $\tau \lesssim 0.2$  fm/c), while most of the observables undergo important modifications due to their interactions with the plasma
- In fact, by definition, **thermalization** (if it happens) implies that the system “forgets” all about the details of its initial state...
- Only inclusive quantities, like the multiplicity, have a chance of staying unchanged until the end
  
- The dependence of the total multiplicity at RHIC on the center of mass energy  $\sqrt{s}$  and on the centrality of the collision is correctly predicted by the CGC
- Some hydrodynamical descriptions of the evolution of the system have successfully used “CGC inspired” initial conditions

# Proton-nucleus collisions

- The produced particles escape without having to go through an extended dense medium
  - ▷ the phenomena predicted in the CGC framework can be measured rather directly
- The proton is much less dense than the nucleus, and can be described with the standard structure functions :

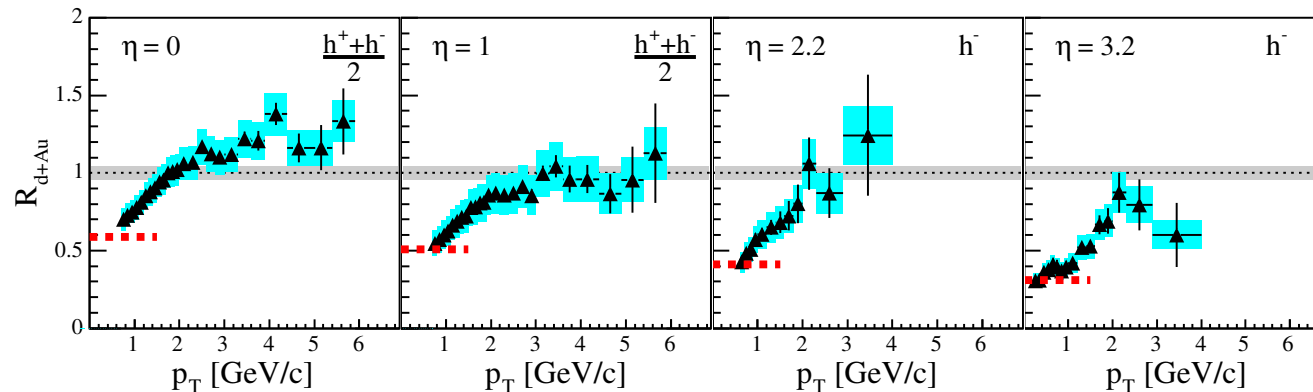


- The matrix elements that enter in cross-sections are directly calculable in the CGC framework (they are known for a number of processes, like gluon or quark production)
- Note : contrary to DIS, one does not know exactly the momentum of the incoming parton



- Results of the BRAHMS experiment at RHIC for deuteron-gold collisions :

$$R_{dAu} \equiv \frac{1}{N_{\text{coll}}} \frac{\left. \frac{dN}{dp_{\perp} d\eta} \right|_{dAu}}{\left. \frac{dN}{dp_{\perp} d\eta} \right|_{pp}}$$



- ◆ At small rapidity, suppression at low  $p_{\perp}$  and enhancement at high  $p_{\perp}$  (multiple scatterings – Cronin effect)
- ◆ At large rapidity, suppression at all  $p_{\perp}$ 's (shadowing)